The Reliability Design and Its Direct Effect on the Energy Efficiency

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1. Introduction

Reliability refers to the ability of system or component to perform a required function under stated environmental and operational conditions for a specified period of time. Traditionally, the reliability over the product life can be illustrated by a bathtub curve that has three regions: a decreasing rate of failure, a constant rate of failure, and an increasing rate of failure, as shown in Figure 1(a). As the reliability of a product (or part) improves, failure of the part becomes less frequent in the field. The bathtub curve may change into a straight line with the slope angle β . In a straight line there are two variables to be measured: product life L_B (or mean time between failures) and failure rate λ , as shown in Eq. (1):

(a) The bathtub curve and straight line with slope β

(b) System life and failure rate consisting of unit #1, unit #2 and unit #3

Figure 1. System life and failure rate

$$R(L_B) = e^{-\lambda L_B} \cong 1 - \lambda L_B \quad (1)$$

We can thus establish the reliability growth plan of parts with a constant failure rate.

A company generally designs its new products to (1) minimize initial failures, (2) reduce random failures during the expected product working period, and (3) lengthen product life. Such aims are met through the use of robust design techniques, including statistical design of experiment (SDE) and the Taguchi methods [1]. The Taguchi methods describe the robustness of a system for evaluation and design improvement, which is also known as quality engineering [2-3] or robust engineering [4]. Robust design processes include concept design, parameter design, and tolerance design [5]. Taguchi's robust design methods place a design in an optimum position where random "noise" does not cause failure, which then and helps in determining the proper design parameters [6].

However, for a simple mechanical structure, the Taguchi methods' robust design processes need to consider a large number of design parameters. They also have difficulty in predicting the product life, L_B (or MTBF).

In this study we present a new method for the reliability design of mechanical systems. This new method takes into account the fact that products with missing or improper design parameters can result in recalls and loss of brand name value. Based on the analysis of a failed refrigerator drawer and handle systems, we demonstrated our new reliability design method. The new method uses ALT; the new concept of product life, L_B ; and sample size, as a novel means of determining proper design parameters [7-14].

1.1. Targeting the refrigerator B_x life and failure rate λ

The multi-unit refrigerator used as a case study for this method consists of a compressor, a drawer, a door, a cabinet, and other units. For the drawer, the B_1 life of the new design is targeted to be over 10 years with a yearly failure rate of 0.1%. The entire refrigerator's B_x life can be obtained by summing up the failure rates of each refrigerator unit. The refrigerator's B_{12} life with the new design is targeted to be over 10 years with a yearly failure rate of 1.2 % (Table 1) [19].

No	Units	Market Data Failure Rate	B_x Life	Design	Conversion	Expected Failure Rate	Target B_x Life	B_x Life	Based B_x
1	Compressor	0.34	5.3	New	x5	1.70	0.10	10	B1.0
2	Door	0.35	5.1	Given	x1	0.35	0.15	10	B1.5
3	Cabinet	0.25	4.8	Modified	x2	0.50	0.10	10	B1.0
4	Drawer	0.20	6.0	New	x2	0.40	0.10	10	B1.0
5	Heat exchanger	0.15	8.0	Given	x1	0.15	0.10	10	B1.0
6	etc	0.50	12.0	Given	x1	0.50	0.50	10	B6.0
Sum	R-Set	1.79	7.4	-	-	3.60	1.10	10	B12.0

Table 1. Total parametric ALT plan of refrigerator

1.2. Analysis of the problems identified in field samples (loads analysis)

In the field, certain components in these refrigerators had been failing or making noise, causing consumers to replace their refrigerators. Data from the failed products in the field showed how common used the refrigerators under common usage conditions. Refrigerator reliability problems in the field occur when the parts cannot endure repetitive stresses due to internal or external forces over a specified period of time. The energy flow in a refrigerator (or other mechanical) system can generally be expressed as efforts and flows (Table 2) [15]. Thus, the stresses come from the efforts.

Refrigerator Units (or Parts)	Effort, $e(t)$	Flow, $f(t)$
Mechanical translation (draws, dispenser lever)	Force component, $F(t)$	Velocity component, $V(t)$
Mechanical rotation (door, cooling fan)	Torque component, $\tau(t)$	Angular velocity component, $V(t)$
Compressor	Pressure difference, $\Delta P(t)$	Volume flow rate, $Q(t)$
Electric (PCB, condenser)	Voltage, $V(t)$	Current, $i(t)$

Table 2. Effort and flow in the multi-port system

For a mechanical system, the time-to-failure approach employs a generalized life model (LS model) [16], such as:

$$T_f = A(S)^{-n} \exp \frac{E_a}{kT} = A(e)^{-n} \exp \frac{E_a}{kT} \quad (2)$$

Repetitive stress can be expressed as the duty effect that carries the on/off cycles and shortens part life [17]. Under accelerated stress conditions, the acceleration factor (AF) can be described as:

$$AF = \left(\frac{S_1}{S_0} \right)^n \left[\frac{E_a}{k} \left(\frac{1}{T_0} - \frac{1}{T_1} \right) \right] = \left(\frac{e_1}{e_0} \right)^n \left[\frac{E_a}{k} \left(\frac{1}{T_0} - \frac{1}{T_1} \right) \right] \quad (3)$$

And n can be determined by multiple testings with different stress levels.

1.3. Parametric ALT with B_x life and sample size

Traditionally, the characteristic life is defined as:

$$\eta^\beta \equiv \frac{\sum t_i^\beta}{r} \equiv \frac{n \cdot h^\beta}{r} \quad (4)$$

As the reliability of a product (or part) improves, failures of the product become less frequent in laboratory tests. Thus, it becomes more difficult to evaluate the characteristic life using Equation (4). The distribution of failed samples should follow the Poisson distribution for small samples [18]. For a 60% confidence level, the characteristic life can be redefined as

$$\eta^\beta \equiv \frac{1}{r+1} \cdot n \cdot h^\beta \quad (5)$$

In order to introduce the B_x life in the Weibull distribution, the characteristic life can be modified as

$$L_B^\beta \equiv x \cdot \eta^\beta = \frac{x}{r+1} \cdot n \cdot h^\beta \quad (6)$$

where $L_B = B_x$ life and $x = 0.01X$, on the condition that $x \leq 0.2$.

B_x is the time by which X % of the drawer and handle system installed in a particular population of refrigerators will have failed. In order to assess the B_x life with about a 60% confidence level, the number of test samples is derived in Eq. (7). That is,

$$n \equiv \frac{1}{x} \cdot (r+1) \cdot \left(\frac{1}{h^*} \right)^\beta \quad (7)$$

with the condition that the durability target is defined as follows,

$$h^* = (AF \cdot h) / L_B \geq 1 \quad (8)$$

Based on the customer usage conditions, the normal range of operating conditions and cycles of the product (or parts) are determined. Under the worst case, the objective number

of cycles and the number of required test cycles can be obtained from Eq. (7). ALT equipment can then be conducted on the basis of load analysis. Using ALT we can find the missing or improper parameters in the design phase.

1.4. Refrigerator unit L_{Bx} life and failure rate, λ , with the improved designs

The parameter design criterion of the newly designed samples can be more than the target life of $B_x = 10$ years. From the field data and from a sample under ALT with a corrective action plans, we can obtain the missing or improper parameters of parts and their levels in the design phase.

With the improved design parameters, we can derive the expected L_{Bx} life of the final design samples using Equation (6).

$$L_B^\beta \equiv x \cdot \frac{n \cdot (h \cdot AF)^\beta}{r + 1} \quad (9)$$

Let $x = \lambda \cdot L_B$ in Equation (9). The failure rate of the final design samples is derived in Equation (10)

$$\lambda \equiv \frac{1}{L_B} \cdot (r + 1) \cdot \frac{L_B^\beta}{n \cdot (h \cdot AF)^\beta} \quad (10)$$

2. Case study: Reliability design of a refrigerator drawer and handle system

Figure 2 shows a refrigerator with the newly designed drawer and handle system and its parts. In the field, the refrigerator drawer and handle system had been failing, causing consumers to replace their refrigerators (Figure 3). The specific causes of failures of the refrigerator drawers during operation were repetitive stress and/or the consumer improper usage. Field data indicated that the damaged products had structural design flaws, including sharp corner angles and weak ribs that resulted in stress risers in high stress areas.

A consumer stores food in a refrigerator to have convenient access to fresh food. Putting food in the refrigerator drawer involves opening the drawer to store or takeout food, closing the drawer by force. Depending on the consumer usage conditions, the drawer and handle parts receive repetitive mechanical loads when the consumer opens and closes the drawer.

Figure 4 shows the functional design concept of the drawer and handle system. The stress due to the weight load of the food is concentrated on the handle and support slide rail of the drawer. Thus, the drawer must be designed to endure these repetitive stresses.

The force balance around the drawer and handle system cans be expressed as:

$$F_{draw} = \mu W_{load} \quad (11)$$

Figure 2. Refrigerator and drawer assembly. (a) French refrigerator (b) Mechanical parts of the drawer: handle ①, drawer ②, slide rail ③, and pocket box ④

Figure 3. A damaged product after use

(a) Parameter diagram of drawer and handle system

(b) Design concept of mechanical drawer and handle system

Figure 4. Functional design concept of the drawer and handle system

Because the stress of the drawer and handle system depends on the food weight, the life-stress model (LS model) can be modified as follows:

$$T_f = A(S)^{-n} = A(F_{draw})^{-n} = A(\mu W_{load})^{-n} \quad (12)$$

where A is constant. Thus, the acceleration factor (AF) can be derived as

$$AF = \left(\frac{S_1}{S_0} \right)^n = \left(\frac{F_1}{F_0} \right)^2 = \left(\frac{\mu W_1}{\mu W_0} \right)^2 = \left(\frac{W_1}{W_0} \right)^2 \quad (13)$$

3. Laboratory experiments

The normal ranges of the operating conditions for the drawer system and handle were 0 to 50°C ambient temperature, 0 to 85% relative humidity and 0.2 to 0.24G vibration. The normal

number of operating cycles for one day was approximately 5; the worst case was 9. Under the worst case, the objective drawer open/close cycles for ten years would be 32,850 cycles (Table 3).

Item	Number of operations (times)			
	1 day		10 years	
	Normal	Worst	Normal	Worst
Drawer	5	9	18,250	32,850

Table 3. Operating number of a drawer

For the worst case, the food weight force on the handle of the drawer was 0.34 *kN*. The applied food weight force for the ALT was 0.68 *kN*. With a quotient, *n*, of 2, the total *AF* was approximately 4.0 using equation (13).

The parameter design criterion of the newly designed drawer can be more than the target life of $B_1 = 10$ years. Assuming the shape parameter β was 2.0 and x was 0.01, the test cycles and test sample numbers calculated in Equation (7) were 67,000 cycles and 3 units, respectively. The ALT was designed to ensure a B_1 life of 10 years with about a 60% level of confidence that it would fail less than once during 67,000 cycles.

(a) ALT equipment and controller

(b) Duty cycles of repetitive food weight force on the drawer

Figure 5. ALT equipment and duty cycles.

Figure 5 shows ALT equipment and duty cycles for the repetitive food weight force, F_{draw} . For the ALT experiments, the control panel on top of the testing equipment started and stopped the drawer during the mission cycles. The food load, F , was controlled by the accelerated weight load in the drawer storage. When a button on the control panel was pushed, mechanical arms and hands pushed and pulled the drawer.

4. Parametric ALTs with corrective action plans

Figures 6(a) and 6(b) show the failed product from the field and the 1st accelerated life testing, respectively. The failure sites in the field and the first ALT occurred at the drawer handle as a result of high concentrated stress. Figure 7 shows a graphical analysis of the ALT results and field data on a Weibull plot. For the shape parameter, the estimated value on the chart was 2.0. For the final design, the shape parameter was determined to be 3.1. These methodologies were valid for pinpointing the weak design responsible for failures in the field and 1st ALT.

(a) Failed product in field

(b) Failed sample in first accelerated life testing

Figure 6. Failed products in field and first ALT

Figure 7. Field data and results of 1st ALT on Weibull chart.

Figure 8. Failed slide rails in second ALT

The fracture of the drawer in the first and second ALTs occurred in the handle and slide rails (Figure 6(b) and Figure 8). The missing or improper parameters of the handle and slide rails in the design phase are listed in Table 4. These design flaws can result in a fracture when the repetitive food load is applied.

CTQ	Parameters			Unit
Fracture	KNP	N1	Consumer food loading	kN
		C1	Reinforced handle width	–
		C2	Handle hooker width	–
	KCP	C3	Fastening screw number	–
		C4	Slide rail chamber	mm
		C5	Slide rail boss thickness	mm
		C6	New added rib	–

Table 4. Vital parameters based on ALTs

To prevent the fracture problem and release the repetitive stresses, the handle and slide rails were redesigned. The corrective action plan for the design parameters included: (1) increasing the width of the reinforced handle, C1, from 90mm to 122mm; (2) increasing the handle hooker size, C2, from 8mm to 19mm; (3) increasing the rail fastening screw number, C3, from 1 to 2; (4) adding an inner chamber and plastic material, C4, from HIPS to ABS; (5) thickening the boss, C5, from 2.0mm to 3.0mm; (6) adding a new support rib, C6 (Table 5).

The parameter design criterion of the newly designed samples was more than the target life, B_1 , of ten years. The confirmed value, β , on the Weibull chart was 3.1. For the second ALT, the recalculated test cycles and sample size in Equation (7) were 32,000 and 3 units, respectively. In the third ALT, no problems were found with the drawer after 32,000 cycles and 65,000 cycles. We therefore concluded that the modified design parameters were effective.

Table 6 provides a summary of the ALT results. Figure 9 shows the results of the 1st ALT and 3rd ALT plotted in a Weibull chart. With the improved design parameters, the B_1 life of the samples in the third ALT was lengthened to more than 10.0 years.

Handle	Right/left slide rail
Increase Screw 1 → 2 EA
	Chamfer Rib Enforcement HIPS → ABS
	Thickness Enforcement 2.0 → 3.0mm
	Liner Support Enforcement Rib
C1: Width L90mm → L122mm (1 st ALT) C2: Width L8mm → L19mm (1 st ALT)	C3: Rail fastening screw number 1→2 (2 nd ALT) C4: Chamfer: Corner chamfer Plastic material HIPS → ABS (2 nd ALT) C5: Boss thickness 2.0 → 3.0 mm (2 nd ALT) C6: New support rib (2 nd ALT)	

Table 5. Redesigned handle and right/left slide rail

Figure 9. Results of 1st ALT and 3rd ALT plotted in Weibull chart

	First ALT	Second ALT	Third ALT
	Initial design	First design iteration	Final design
In 32,000 cycles, Fracturing is less than 1	7,500 cycles: 2/3 Fail 12,000 cycles: 1/3 OK $\lambda = 26.6 \text{ \%/year}$ $B_1 = 3.4 \text{ year}$	16,000 cycles: 2/3 Fail $\lambda = 2.46 \text{ \%/year}$ $B_1 = 7.3 \text{ year}$	32,000 cycles: 3/3 OK 65,000 cycles: 3/3 OK $\lambda = 0.1 \text{ \%/year}$ $B_1 = 10 \text{ year}$
Drawer structure
Material & Spec.	Width1: L90 → L122 Width2: L8 → L19.0	Rib1: new support rib boss: 2.0 → 3.0 mm Chamfer1: Corner Material: HIPS → ABS	

Table 6. Results of ALTs

6. Conclusions

We developed a new reliability design method based on a study of a defective refrigerator drawer and handle system that was failing under field use conditions. The failure modes and mechanisms for the drawer in the field and in the ALTs were identified. Important design parameters were studied and improvements were evaluated using ALTs.

Based on the products returned from the field and the results of the first ALT, we found that the handles were fracturing because of design flaws. The handle design was corrected by increasing the handle width. During the second ALT, the slide rails fractured because they did not have enough strength to endure the repetitive food storage loads. The slide rails were corrected by providing additional reinforced ribs, reinforced boss, and an inner chamber. As a result these modified design parameters, there were no problems in the third ALT. We therefore concluded that the values for the design parameters were effective to meet the life cycle requirements. The yearly failure rate and B_1 life of the redesigned drawer and handle system, based on the results of ALT, were under 0.1% and more than 10 years, respectively. The study of the missing or improper design parameters in the design phase, through the inspection of failed products in the field, load analysis, and ALTs was very effective in redesigning more reliable parts with significantly longer life.

The case study focused on a mechanical structure consisting of several parts subjected to repetitive stresses under consumer usage conditions. The same principles developed for the new reliability design methodology could be applied to other mechanical systems, including construction equipment, automobile gear trains and engines, forklifts, washing machines, vacuum cleaners, and motor fan systems. We recommend that the missing or improper controllable design parameters on these systems also be studied for reliability design. These parameter studies would also include failure analysis, load analysis, and a tailored series of accelerated life tests. These methodologies could then predict part life quantitatively through accelerated factors and exact sample size.

7. Nomenclature

AF	acceleration factor
B_x	durability index
$C1$	width of reinforced handle, mm
$C2$	width of handle hooker, mm
$C3$	back rib of slide rail
$C4$	screw boss height of slide rail, mm
$C5$	inner chamber of slide rail
$C6$	material of slide rail
$C7$	screw number of slide number
e	effort
e_0	effort under normal stress conditions
e_1	effort under accelerated stress conditions
E_a	activation energy
f	flow
$F(t)$	unreliability
F_{draw}	open/close force of the freezer drawer system, kN
F_1	weight force under accelerated stress conditions, kN
F_0	weight force under normal conditions, kN
h	testing time (or cycles)
h^*	non-dimensional testing cycles, $h^* = h/L_B \geq 1$
i	current, A
k	Boltzmann's constant, $8.62 \times 10^{-5} \text{ eV/deg}$
KCP	Key Control Parameter
KNP	Key Noise Parameter
L_B	the target B_x life and $x = 0.01X$, on the condition that $x \leq 0.2$
n	the number of test samples
$N1$	consumer freezer door drawer open/close force, kN
ΔP	pressure difference, MPa
r	failed numbers

R	reliability function
S	stress
S_0	mechanical stress under normal stress conditions
S_1	mechanical stress under accelerated stress conditions
t_i	test time for each sample
T	absolute temperature, K
T_1	absolute temperature under accelerated stress conditions, K
T_0	absolute temperature under normal stress conditions, K
T_f	time to failure
V	velocity, m/s
V	voltage, <i>volt</i>
W_1	food weight force under accelerated stress conditions, kN
W_0	food weight force under normal stress conditions, kN
W_{load}	total food weight force in the freezer door drawer, kN
X	accumulated failure rate, %
x	$x = 0.01 \cdot X$, on condition that $x \leq 0.2$.

Greek symbols

η	characteristic life
λ	failure rate
μ	friction coefficient

Superscripts

β	shape parameter in a Weibull distribution
n	stress dependence, $n = - \left[\frac{\partial \ln(T_f)}{\partial \ln(S)} \right]_T$

Subscripts

0	normal stress conditions
1	accelerated stress conditions

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