

Secular Evolution of Satellites by Tidal Effect

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1. Introduction

Both the Earth's Moon and Pluto's moon, Charon, have an important fraction of the mass of their systems, and therefore they could be classified as double-planets rather than as satellites. The proto-planetary disk is unlikely to produce such systems, and their origin seems to be due to a catastrophic impact of the initial planet with a body of comparable dimensions (e.g. Canup, 2005; Canup & Asphaug, 2001). On the other hand, Neptune's moon, Triton, and the Martian moon, Phobos, are spiraling down into the planet, clearly indicating that the present orbits are not primordial, and may have undergone a long evolving process from a previous capture (e.g. Goldreich et al., 1989; Mignard, 1981).

The present orbits of all these satellites are almost circular, and their spins appear to be synchronous with the orbital mean motion, as well as being locked in Cassini states (e.g. Colombo, 1966; Peale, 1969). This also applies to the Galilean satellites of Jupiter, which are likely to have originated from Jupiter's accretion disk and additionally show orbital mean motion resonances (e.g. Yoder, 1979). All these features seem to be due to tidal evolution, which arises from differential and inelastic deformation of the planet by a perturbing body.

Previous long-term studies on the orbital evolution of satellites have assumed that their rotation is synchronously locked, and therefore limits the tidal evolution to the orbits (e.g. McCord, 1966). However, these two kinds of evolution cannot be dissociated because the total angular momentum must be conserved. Additionally, it has been assumed that the spin axis is locked in a Cassini state with very low obliquity. Although these assumptions are correct for the presently known situations, they were not necessarily true throughout the evolution.

In this article we model the orbital evolution of a satellite from its origin or capture until the preset day, including spin evolution for both planet and satellite, and we also regard its future evolution. We provide a simple averaged model adapted for fast computational simulations, as required for long-term studies, following Correia (2009). However, we present an improvement with respect to previous work, here we do not average the equations of motion over the argument of the periastron, as in Correia et al. (2011). Therefore, this model is more complete, and allows the eccentricity of the satellite to show secular variations due to the gravitational perturbations of the star on its orbit around the planet. We then apply this model to the Triton-Neptune system. The results do not differ much from those in Correia (2009) for the final stages of the orbital evolution, but can show some significant differences during the initial stages. In the last section we discuss the results obtained.

2. The model

We consider a hierarchical system composed of a star, a planet and a satellite, with masses $M \gg m_0 \gg m_1$, respectively. Both planet and satellite are considered oblate ellipsoids with gravity field coefficients given by J_{2_0} and J_{2_1} , rotating about the axis of maximal inertia along the directions $\hat{\mathbf{s}}_0$ and $\hat{\mathbf{s}}_1$, with rotation rates ω_0 and ω_1 , respectively. The potential energy U of the system is then given by (e.g. Smart, 1953):

$$\begin{aligned}
 U = & -G \frac{Mm_0}{r_0} \left(1 - \sum_{i=0,1} J_{2_i} \frac{m_i}{m_0} \left(\frac{R_i}{r_0} \right)^2 P_2(\hat{\mathbf{r}}_0 \cdot \hat{\mathbf{s}}_i) \right) \\
 & -G \frac{m_0 m_1}{r_1} \left(1 - \sum_{i=0,1} J_{2_i} \left(\frac{R_i}{r_1} \right)^2 P_2(\hat{\mathbf{r}}_1 \cdot \hat{\mathbf{s}}_i) \right) \\
 & -G \frac{Mm_1}{r_0} \left(\frac{r_1}{r_0} \right)^2 P_2(\hat{\mathbf{r}}_0 \cdot \hat{\mathbf{r}}_1), \quad (1)
 \end{aligned}$$

where terms in $(R_i/r_j)^3$ have been neglected ($i, j = 0, 1$). G is the gravitational constant, R_i the radius of the planet or the satellite, r_i the distance between the planet and the star or the satellite, and $P_2(x) = (3x^2 - 1)/2$ the Legendre polynomial of degree two.

Neglecting tidal interactions with the star, the tidal potential is written (e.g. Kaula, 1964):

$$U_T = -\frac{G}{r_1^3} \sum_{i=0,1} k_{2_i} m_{(1-i)}^2 \frac{R_i^5}{r_i^3} P_2(\hat{\mathbf{r}}_1 \cdot \hat{\mathbf{r}}'_i), \quad (2)$$

where k_{2_i} is the potential Love number for the planet or the satellite, and \mathbf{r}'_i the position of the interacting body at a time delayed of Δt_i . For simplicity, we will adopt a model with constant Δt_i , which can be made linear (e.g. Mignard, 1979; Néron de Surgy & Laskar, 1997):

$$\mathbf{r}'_i \simeq \mathbf{r}_1 + \Delta t_i (\omega_i \mathbf{s}_i \times \mathbf{r}_1 - \dot{\mathbf{r}}_1). \quad (3)$$

The complete evolution of the system can be tracked by the evolution of the rotational angular momentums, $\mathbf{H}_i \simeq C_i \omega_i \hat{\mathbf{s}}_i$, the orbital angular momentums, $\mathbf{L}_i \simeq m_i n_i a_i^2 (1 - e_i^2)^{1/2} \hat{\mathbf{k}}_i$, and the Laplace-Runge-Lenz vector, which points along the major axis in the direction of periapsis with magnitude e_1 :

$$\mathbf{e}_1 = \frac{\dot{\mathbf{r}}_1 \times \mathbf{L}_1}{GMm_1} - \frac{\mathbf{r}_1}{r_1}. \quad (4)$$

n_i is the mean motion, a_i the semi-major axis, e_i the eccentricity, and C_i the principal moment of inertia. The contributions to the orbits are easily computed from the above potentials as

$$\dot{\mathbf{L}}_0 = -\mathbf{r}_0 \times \mathbf{F}_0, \quad \dot{\mathbf{L}}_1 = -\mathbf{r}_1 \times \mathbf{F}_1, \quad (5)$$

$$\dot{\mathbf{e}}_1 = \frac{1}{GMm_1} \left(\mathbf{F}_1 \times \frac{\mathbf{L}_1}{m_1} + \dot{\mathbf{r}}_1 \times \dot{\mathbf{L}}_1 \right), \quad (6)$$

where $\mathbf{F}_i = -\nabla_{\mathbf{r}_i} U'$, with $U' = U + U_T + GMm_0/r_0 + Gm_0m_1/r_1$.

Since the total angular momentum is conserved, the contributions to the spin of the planet and satellite can easily be computed from the orbital contributions:

$$\dot{\mathbf{H}}_0 + \dot{\mathbf{H}}_1 + \dot{\mathbf{L}}_0 + \dot{\mathbf{L}}_1 = 0. \tag{7}$$

Because we are only interested in the secular evolution of the system, we further average the equations of motion over the mean anomalies of both orbits. The resulting equations for the conservative motion are (Boué & Laskar, 2006; Farago & Laskar, 2010):

$$\dot{\mathbf{L}}_0 = -\gamma(1 - e_1^2) \cos I \hat{\mathbf{k}}_1 \times \hat{\mathbf{k}}_0 + 5\gamma(\mathbf{e}_1 \cdot \hat{\mathbf{k}}_0) \mathbf{e}_1 \times \hat{\mathbf{k}}_0 - \sum_i \alpha_i \cos \varepsilon_i \hat{\mathbf{s}}_i \times \hat{\mathbf{k}}_0, \tag{8}$$

$$\dot{\mathbf{L}}_1 = -\gamma(1 - e_1^2) \cos I \hat{\mathbf{k}}_0 \times \hat{\mathbf{k}}_1 + 5\gamma(\mathbf{e}_1 \cdot \hat{\mathbf{k}}_0) \hat{\mathbf{k}}_0 \times \mathbf{e}_1 - \sum_i \beta_i \cos \theta_i \hat{\mathbf{s}}_i \times \hat{\mathbf{k}}_1, \tag{9}$$

$$\begin{aligned} \dot{\mathbf{e}}_1 = & -\frac{\gamma(1 - e_1^2)}{\|\mathbf{L}_1\|} \left[\cos I \hat{\mathbf{k}}_0 \times \mathbf{e}_1 - 2\hat{\mathbf{k}}_1 \times \mathbf{e}_1 - 5(\mathbf{e}_1 \cdot \hat{\mathbf{k}}_0) \hat{\mathbf{k}}_0 \times \hat{\mathbf{k}}_1 \right] \\ & - \sum_i \frac{\beta_i}{\|\mathbf{L}_1\|} \left[\cos \theta_i \hat{\mathbf{s}}_i \times \mathbf{e}_1 + \frac{1}{2}(1 - 5 \cos^2 \theta_i) \hat{\mathbf{k}}_1 \times \mathbf{e}_1 \right], \end{aligned} \tag{10}$$

and

$$\dot{\mathbf{H}}_i = -\alpha_i \cos \varepsilon_i \hat{\mathbf{k}}_0 \times \hat{\mathbf{s}}_i - \beta_i \cos \theta_i \hat{\mathbf{k}}_1 \times \hat{\mathbf{s}}_i, \tag{11}$$

where

$$\alpha_i = \frac{3GMm_i J_2 R_i^2}{2a_0^3(1 - e_0^2)^{3/2}}, \tag{12}$$

$$\beta_i = \frac{3Gm_0 m_1 J_2 R_i^2}{2a_1^3(1 - e_1^2)^{3/2}}, \tag{13}$$

$$\gamma = \frac{3GMm_1 a_1^2}{4a_0^3(1 - e_0^2)^{3/2}}, \tag{14}$$

and

$$\cos \varepsilon_i = \hat{\mathbf{s}}_i \cdot \hat{\mathbf{k}}_0, \quad \cos \theta_i = \hat{\mathbf{s}}_i \cdot \hat{\mathbf{k}}_1, \quad \cos I = \hat{\mathbf{k}}_0 \cdot \hat{\mathbf{k}}_1, \tag{15}$$

are the direction cosines of the spins and orbits: ε_i is the obliquity to the orbital plane of the planet, θ_i the obliquity to the orbital plane of the satellite, and I the inclination between orbital planes.

For the dissipative tidal effects, we obtain (Correia et al., 2011):

$$\dot{\mathbf{L}}_0 = 0, \quad \dot{\mathbf{L}}_1 = -\dot{\mathbf{H}}_0 - \dot{\mathbf{H}}_1, \tag{16}$$

$$\begin{aligned} \dot{\mathbf{e}}_1 = & \sum_i \frac{15}{2} k_2 n_1 \left(\frac{m_j}{m_i} \right) \left(\frac{R_i}{a_1} \right)^5 f_4(e_1) \hat{\mathbf{k}}_1 \times \mathbf{e}_1 \\ & - \sum_i \frac{K_i}{\beta_1 a_1^2} \left[f_4(e_1) \frac{\omega_i}{2n_1} (\mathbf{e}_1 \cdot \hat{\mathbf{s}}_i) \hat{\mathbf{k}}_1 - \left(\frac{11}{2} f_4(e_1) \cos \theta_i \frac{\omega_i}{n_1} - 9f_5(e_1) \right) \mathbf{e}_1 \right], \end{aligned} \tag{17}$$

and

$$\begin{aligned} \dot{\mathbf{H}}_i = K_i n_1 \left[f_4(e_1) \sqrt{1 - e_1^2} \frac{\omega_i}{2n_1} (\hat{\mathbf{s}}_i - \cos \theta_i \hat{\mathbf{k}}_1) \right. \\ \left. - f_1(e_1) \frac{\omega_i}{n_1} \hat{\mathbf{s}}_i + f_2(e_1) \hat{\mathbf{k}}_1 + \frac{(\mathbf{e}_1 \cdot \hat{\mathbf{s}}_i)(6 + e_1^2)}{4(1 - e_1^2)^{9/2}} \frac{\omega_i}{n_1} \mathbf{e}_1 \right], \end{aligned} \quad (18)$$

where,

$$K_i = \Delta t_i \frac{3k_2 G m_{(1-i)}^2 R_i^5}{a_1^6}, \quad (19)$$

and

$$f_1(e) = \frac{1 + 3e^2 + \frac{3}{8}e^4}{(1 - e^2)^{9/2}}, \quad (20)$$

$$f_2(e) = \frac{1 + \frac{15}{2}e^2 + \frac{45}{8}e^4 + \frac{5}{16}e^6}{(1 - e^2)^6}, \quad (21)$$

$$f_3(e) = \frac{1 + \frac{31}{2}e^2 + \frac{255}{8}e^4 + \frac{185}{16}e^6 + \frac{25}{64}e^8}{(1 - e^2)^{15/2}}, \quad (22)$$

$$f_4(e) = \frac{1 + \frac{3}{2}e^2 + \frac{1}{8}e^4}{(1 - e^2)^5}, \quad (23)$$

$$f_5(e) = \frac{1 + \frac{15}{4}e^2 + \frac{15}{8}e^4 + \frac{5}{64}e^6}{(1 - e^2)^{13/2}}. \quad (24)$$

The first term in expression (17) corresponds to a permanent tidal deformation, while the second term corresponds to the dissipative contribution. The precession rate of \mathbf{e}_1 about $\hat{\mathbf{k}}_1$ is usually much faster than the evolution time-scale for the dissipative tidal effects. As a consequence, when the eccentricity is constant over a precession cycle, we can average expression (18) over the argument of the periapsis and get (Correia, 2009):

$$\dot{\mathbf{H}}_i = -K_i n_1 \left(f_1(e_1) \frac{\hat{\mathbf{s}}_i + \cos \theta_i \hat{\mathbf{k}}_1}{2} \frac{\omega_i}{n_1} - f_2(e_1) \hat{\mathbf{k}}_1 \right). \quad (25)$$

3. Secular evolution

In the previous section we presented the equations that rule the tidal evolution of a satellite in terms of angular momenta and orbital energy. However, the spin and orbital quantities are better represented by the rotation angles and elliptical elements. The direction cosines (Eq.15) are obtained from the angular momenta vectors, since $\hat{\mathbf{s}}_i = \mathbf{H}_i / \|\mathbf{H}_i\|$ and $\hat{\mathbf{k}}_i = \mathbf{L}_i / \|\mathbf{L}_i\|$, as well as the rotation rate $\omega_i = \mathbf{H}_i \cdot \hat{\mathbf{s}}_i / C_i$. The eccentricity and the semi-major axis can be obtained from $e_1 = \|\mathbf{e}_1\|$, and $a_1 = \|\mathbf{L}_1\|^2 / (GMm_1^2(1 - e_1^2))$, respectively.

3.1 Spin evolution

The variation in the satellite’s rotation rate can be obtained from $\dot{\omega}_i = \dot{\mathbf{H}}_i \cdot \hat{\mathbf{s}}_i / C_i$ (Eq. 25), giving (Correia & Laskar, 2009):

$$\dot{\omega}_1 = -\frac{K_1 n_1}{C_1} \left(f_1(e_1) \frac{1 + \cos^2 \theta_1}{2} \frac{\omega_1}{n_1} - f_2(e_1) \cos \theta_1 \right). \tag{26}$$

For a given obliquity and eccentricity, the equilibrium rotation rate, obtained when $\dot{\omega}_1 = 0$, is attained for:

$$\frac{\omega_1}{n_1} = \frac{f_2(e_1)}{f_1(e_1)} \frac{2 \cos \theta_1}{1 + \cos^2 \theta_1}, \tag{27}$$

The obliquity variations can be obtained from equation (15):

$$\frac{d \cos \theta_i}{dt} = \frac{\dot{\mathbf{H}}_i \cdot (\hat{\mathbf{k}}_1 - \cos \theta_i \hat{\mathbf{s}}_i)}{\|\mathbf{H}_i\|} + \frac{\dot{\mathbf{L}}_1 \cdot (\hat{\mathbf{s}}_i - \cos \theta_i \hat{\mathbf{k}}_1)}{\|\mathbf{L}_1\|}. \tag{28}$$

For the conservative motion (Eqs. 9, 11), stable configurations for the spin can be found whenever the vectors $(\hat{\mathbf{s}}_1, \hat{\mathbf{k}}_1, \hat{\mathbf{k}}_0)$ or $(\hat{\mathbf{s}}_1, \hat{\mathbf{k}}_1, \hat{\mathbf{s}}_0)$ are coplanar and precess at the same rate g (e.g. Colombo, 1966; Correia et al., 2011; Peale, 1969). The first situation occurs if $\gamma \gg \beta_0$ (outer satellite) and the second situation when $\gamma \ll \beta_0$ (inner satellite). The equilibrium obliquities can be found from a single relationship (e.g. Ward & Hamilton, 2004):

$$\lambda_1 \cos \theta_1 \sin \theta_1 + \sin(\theta_1 - I_0) = 0, \tag{29}$$

where $\lambda_1 = \beta_1 / (C_1 \omega_1 g)$ is a dimensionless parameter and I_0 is the inclination of the orbit of the satellite with respect to the Laplacian plane ($I_0 \simeq I$ and $g \simeq \gamma \cos I / \|\mathbf{L}_1\|$ for an outer satellite, and $I_0 \simeq \theta_0$ and $g \simeq \beta_0 \cos \theta_0 / \|\mathbf{L}_1\|$ for an inner satellite) (e.g. Laplace, 1799; Mignard, 1981; Tremaine et al., 2009). The above equation has two or four real roots for θ_1 , which are known by *Cassini states*. In general, for satellites we have $I_0 \sim 0$, and these solutions are approximately given by:

$$\tan^{-1} \left(\frac{\sin I_0}{\cos I_0 \pm \lambda_1} \right), \quad \pm \cos^{-1} \left(-\frac{\cos I_0}{\lambda_1} \right). \tag{30}$$

For a generic value of I_0 , when $\lambda_1 \ll 1$, which is often the case of an outer satellite, the first expression gives the only two real roots of equation (29), one for $\theta_1 \simeq I_0$ and another for $\theta_1 \simeq \pi - I_0$. On the other hand, when $\lambda_1 \gg 1$, which is the case of inner satellites, we will have four real roots approximately given by expressions (30).

In turn, the dissipative obliquity variations are computed by substituting equation (25) in (28) with $\|\mathbf{H}_1\| \ll \|\mathbf{L}_1\|$, giving:

$$\dot{\theta}_1 \simeq \frac{K_1 n_1}{C_1 \omega_1} \sin \theta_1 \left(f_1(e_1) \cos \theta_1 \frac{\omega_1}{2 n_1} - f_2(e_1) \right). \tag{31}$$

Because of the factor n_1 / ω_1 in the magnitude of the obliquity variations, for an initial fast rotating satellite, the time-scale for the obliquity evolution will be longer than the time-scale for the rotation rate evolution (Eq.26). As a consequence, it is to be expected that the rotation

rate reaches its equilibrium value (Eq.27) earlier than the obliquity. Thus, replacing equation (27) in (31), we have:

$$\dot{\theta}_1 \simeq -\frac{K_1 n_1}{C_1 \omega_1} f_2(e_1) \frac{\sin \theta_1}{1 + \cos^2 \theta_1}. \quad (32)$$

We then conclude that the obliquity can only decrease by tidal effect, since $\dot{\theta}_1 \leq 0$, and the final obliquity tends to be captured in low obliquity Cassini states.

3.2 Orbital evolution

The variations in the eccentricity are easily obtained from the Laplace-Runge-Lenz vector (Eq.17):

$$\dot{e}_1 = \frac{\dot{\mathbf{e}}_1 \cdot \mathbf{e}_1}{e_1} = \sum_i \frac{9K_i}{m_1 a_1^2} \left(\frac{11}{18} f_4(e_1) \cos \theta_i \frac{\omega_i}{n_1} - f_5(e_1) \right) e_1, \quad (33)$$

while the semi-major axis variations are obtained from the eccentricity and the norm of the orbital angular momentum:

$$\frac{\dot{a}_1}{a_1} = \frac{2\dot{e}_1 e_1}{(1 - e_1^2)} + \frac{2\dot{\mathbf{L}}_1 \cdot \mathbf{L}_1}{\|\mathbf{L}_1\|^2} = \sum_i \frac{2K_i}{m_1 a_1^2} \left(f_2(e_1) \cos \theta_i \frac{\omega_i}{n_1} - f_3(e_1) \right). \quad (34)$$

For gaseous planets and rocky satellites we usually have $k_{20} \Delta t_0 \ll k_2 \Delta t_1$, and we can retain only terms in K_1 .

The ratio between orbital and spin evolution time-scales is roughly given by $C_1 / (m_1 a_1^2) \ll 1$, meaning that the spin achieves an equilibrium position ($\dot{\mathbf{H}}_1 = 0$) much faster than the orbit. Replacing the equilibrium rotation rate (Eq. 27) with $\theta_1 = 0$ (for simplicity) in equations (33) and (34), gives:

$$\dot{a}_1 = -\frac{7K_1}{m_1 a_1} f_6(e_1) e_1^2, \quad (35)$$

$$\dot{e}_1 = -\frac{7K_1}{2m_1 a_1^2} f_6(e_1) (1 - e_1^2) e_1, \quad (36)$$

where

$$f_6(e) = \frac{1 + \frac{45}{14}e^2 + 8e^4 + \frac{685}{224}e^6 + \frac{255}{448}e^8 + \frac{25}{1792}e^{10}}{(1 + 3e^2 + \frac{3}{8}e^4)(1 - e^2)^{15/2}}. \quad (37)$$

Thus, we always have $\dot{a}_1 \leq 0$ and $\dot{e}_1 \leq 0$, and the final eccentricity is zero. However, from this point onwards, the tidal effects on the planet cannot be neglected (Eq.34), and they govern the future evolution of the satellite's orbit. For $a_f < a_s$ or $\theta_0 \geq \pi/2$, where $a_s^3 = Gm_0 / (\omega_0 \cos \theta_0)^2$, the semi-major axis continues to decrease until the satellite crashes into the planet, while in the remaining situations it will increase.

4. Application to Triton-Neptune

Neptune's main satellite, Triton, presents unique features in the Solar System. It is the only moon-sized body in a retrograde inclined orbit and the images taken by the Voyager 2 spacecraft in 1989 revealed an extremely young surface with few impact craters (e.g. Cruikshank, 1995). This satellite should have remained molten until about 1 Gyr ago and

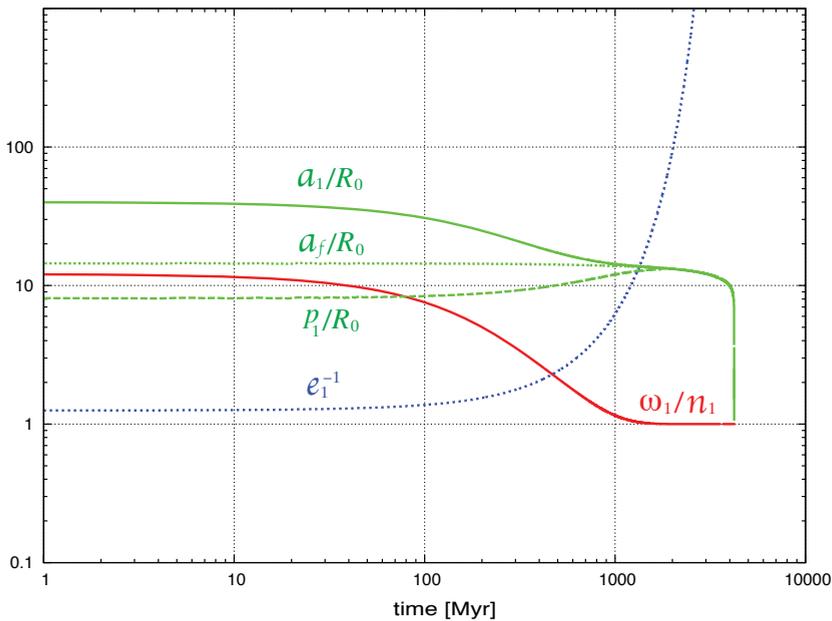


Fig. 1. Secular tidal evolution of the Triton-Neptune system. We plot the semi-major axis ratios a_1/R_0 and a_f/R_0 , the periastron distance p_1/R_0 , the inverse of the eccentricity e_1^{-1} and Triton’s rotation rate ratio ω_1/n_1 .

its interior is still warm and geologically active considering its distance from the Sun (Schenk & Zahnle, 2007). Its composition also presents some similarities with Pluto (Tsurutani et al., 1990).

These bizarre characteristics lead one to believe that Triton originally orbited the Sun, belonging to the family of Kuiper-belt objects. Most likely during the outward migration of Neptune, the orbits of the two bodies intercepted and capture occurred. This possibility is strongly supported by the fact that Triton’s present orbit lies between a group of small inner prograde satellites and a number of exterior irregular satellites both prograde and retrograde. Nereid, with an orbital eccentricity around 0.75, is also believed to have been scattered from a regular satellite orbit (McKinnon, 1984).

How exactly the capture occurred is still unknown, but some mechanisms have been proposed: gas drag (McKinnon & Leith, 1995; Pollack et al., 1979), a collision with a pre-existing regular satellite of Neptune (Goldreich et al., 1989), or three-body interactions (Agnor & Hamilton, 2006; Vokrouhlický et al., 2008). All these scenarios require a very close passage to Neptune, and leave the planet in eccentric orbits that must be damped by tides to the present one. Tides are thus the only consensual mechanism acting on Triton’s orbit. The tidal distortion of Triton after a few close passages around Neptune, and the consequent dissipation of tidal energy, can account for a substantial reduction in the semi-major axis of its orbit, quickly bringing the planet from an orbit outside Neptune’s Hill sphere ($\sim 4700 R_0$)

to a bounded orbit. Therefore, it cannot be ruled out that Triton was simply captured by tidal interactions with Neptune after a close encounter in an almost parabolic orbit (McCord, 1966).

Here, we simulate the tidal evolution of the Triton-Neptune system using the complete model described in Sect.2. Triton is started in a very elliptical orbit with $e_1 = 0.99$ and a semi-major axis of $a_1 = 40 R_0$, corresponding to a final equilibrium $a_f \simeq 14.4 R_0$, close to the present position of $14.33 R_0$. These specific values give a closest approach at a periape of $8 R_0$.

For the radius of the bodies we use $R_0 = 24\,764$ km and $R_1 = 1\,353$ km (Thomas, 2000), while for the masses, the J_2 of Neptune and the remaining orbital and spin parameters we take the present values as determined by Jacobson (2009). For Triton we adopt $J_2 = 4.38 \times 10^{-4}$, the value measured for Europa (Anderson et al., 1998), and $C_{22} = 0$, since our model does not take into account spin-orbit resonances. This choice is justified because Triton's observed topography never varies beyond a kilometer (Thomas, 2000). In addition, Triton should have undergone frequent collisions either with other satellites of Neptune, or with external Kuiper-belt objects, and any capture in a spin-orbit resonance different from the synchronous one, may not last for a long time (Stern & McKinnon, 2000). For tidal dissipation we adopt the same parameters as previous studies, that is, $k_{2_0} = 0.407$ and $Q_0 = 9000$ (Zhang & Hamilton, 2008), and $k_{2_1} = 0.1$ and $Q_1 = 100$ (Chyba et al., 1989; Goldreich et al., 1989), where $Q_i^{-1} = \omega_i \Delta t_i$.

As for the orbit, the initial spin of Triton is unknown. We tested several possibilities, but tides acting on the spin always drive it in the same way: the rotation rate quickly evolves into the equilibrium value given by equation (27), while the obliquity is trapped in a Cassini state. In our standard simulation (Fig.1) we start Triton with a rotation period of 24 h. The semi-major axis and the eccentricity always decrease, as predicted by equations (35) and (36), and the quantity $a_f = a_1(1 - e_1^2)$ is preserved during the first stages of the evolution, with the reduction observed being caused by tides on Neptune. The eccentricity is very high during the first evolutionary stages, but it decreases rapidly as the satellite approaches its present orbit. Finally, the rotation of the satellite decreases as the satellite orbit shrinks into Neptune and ultimately stabilizes in the synchronous resonance, the presently observed configuration.

5. Conclusion

The numerical results presented here are very similar to those shown in Correia (2009) for $a_1 \leq 40 R_0$. For these values of the semi-major axis, Triton can still be considered as an "inner satellite", that is, the inclination with respect to the equatorial plane of Neptune, θ_0 , is approximately constant. However, for higher values of the semi-major axis, we observe exchanges between the inclination and the eccentricity of Triton. Since the eccentricity is no longer constant, it is not possible to average over the argument of the periastron as in Correia (2009). Therefore, the results with the non-averaged model presented here will show some differences. In particular, the perturbation on Triton's orbit will cause the eccentricity to vary around the mean value, allowing the periape to attain lower values. As a consequence, tidal effects will be stronger for close encounters with Neptune, and the migration of Triton may occur in much faster time-scales. In a future study we will analyze in detail the evolution of Triton's orbit for $a_1 > 40 R_0$.

Our study should also apply to the Moon, Charon and the satellites of Mars, although in this case we need to take into account the quadropole moment of inertia $C_{22} \neq 0$ (Correia, 2006).

6. References

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