Growth Reinforcing Composite Materials from Liquidus Phase: Mechanical and Microstructural Parameters Relationship Essentially Evincing the Predominance of an Akin Mass Composition over the Domain of Compositions

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1. Introduction

Composite materials are heterogeneous systems consisting of two or more physically distinct and mechanically separable materials belonging to different space groups, and are in equilibrium with a single liquidus phase. The essence of composite materials lies in the concept that their properties must essentially be superior, and possibly unique in some specific respects, to those of the constituent phases, particularly if these are geometrically oriented to one another in some periodic or anisotropic manner (Sharma et al., 2008, 2009). Composite materials designed by anisotropic growth process, can offer advanced possibilities as reinforced materials for the constructions and further development of supersonic aircraft, space vehicles, high pressure tanks, for which strength properties are required that cannot be provided by the existing homogeneous materials (Ashbee & Woishnis, 1993). Besides mechanical fields, these materials are equally promising in a variety of other fields (Hull & Clyne, 2006). For example, most metallic permanent magnets are made of alnico alloys, obtained by unidirectional solid-state decomposition under cooling conditions in an applied magnetic field. The rod composite structure of quasi binary NiSb-InSb (Caram et al., 1990) obtained by unidirectional solidification from its homogeneous eutectic melt, finds a representative example in electronics. Currently, the femoral stem is constructed from Co-Cr-Mo, Co-Ni-Cr-Mo and Ti-Al-V alloys (Callister, 2006; Mallick, 1993 & Pillar, 1984) in preference to stainless steels. The advantages of composite materials appear when the specific modulus (modulus per unit weight) and specific strength (strength per unit weight) are considered. The higher specific modulus and specific strength of composite materials means that the weight of constituent phases can be reduced (Callister, 2006 & Courtney, 2000). This is a factor of greater importance in moving constituent phases in all forms of transport where reductions in weight result in greater efficiency and energy savings (Callister & Rethwisch, 2008).

The essence of anisotropic growth applied to composite materials is the ability to put strong stiff fibers in the right place, in the right orientation with right volume fraction. Implicit in the present searching approach is the concept that while in designing the composite material by variable anisotropic growth, the solidification aspect is also related to discover the final

product as an acceptable analog for manufacturing the engineering product. Because of the complex nature of the phenomena involved in an anisotropic growth process from the melt, a considerable judgment is required to assess both theoretical and experimental observations, since the composite materials that can be developed by this process exhibit a large diversity of micro-morphologies. However, a physical understanding of the mechanical properties of composite materials as a basis for the improvement of the properties by controlling the growth rates from the melt can readily be distinguished when examined in an optical or electronic microscope. In view of watching the growth process visually, binary organic eutectic systems being transparent are a most suitable option for investigation, since metals are opaque and the observations had to be made on external surfaces. A very interesting finding of the current investigation is an akin mass composition (the composition whereat masses of the constituent members would almost overlap each other) that predominates the domain of compositions, since anisotropic mechanical parameters obeying the Weibull probability distribution curve evince the predominance, particularly at moderate anisotropic growth rate. Likewise, of greater interest is the moderate anisotropic growth in the domain of solidification modes as the modal products structured by the growth process comprise microstructures which are three-to-four fold superior in mechanical strength to their isotropic growth performed in an ice bath (~273 K) and many fold to their respective individual components irrespective of the growth pattern. Vickers microhardness offers supporting evidence to the essence of an identical form of the Weibull distribution curve demonstrating the strength-growth relationship. The liquidus structure encompassing the entire composition of binary organic eutectic systems is characterized by rheological view point comprising of viscosity and surface tension measurements at different temperatures, which manifests specific interactions occurring in the eutectic compositional melt that are complimentary supported by thermodynamic analysis in terms of excess functions. The experimental data on kinetics and anisotropic crystal growth from the melt verify nucleation theory and evince the essence of dislocation mechanism. Thermal and X-ray diffraction studies of binary composite materials are accomplished in order to ascertain thermal stability, purity, composition, enthalpies of fusion and mechanical combination of homogeneous materials.

A series of binary organic eutectic systems, viz., naphthalene-o-nitrophenol; α -naphthol-naphthalene; diphenylamine- α -naphthol; benzil-diphenyl; benzoic acid-benzamide; benzoic acid-naphthalene; naphthalene-phenanthrene; α -naphthylamine-diphenylamine and binary metallic eutectic systems, namely, Sn-Cd; Cd-Bi; Pb-Sn and Pb-Bi, were selected for the investigation. The choice of homogeneous materials in aforementioned systems is restricted to the methodical considerations: low temperatures of melting, purity and the possibility of precisely controlling and measuring temperatures.

2. Experimental details

2.1 Materials and methodology

A great precautionary care was taken to the selection of utmost pure homogeneous materials, since organic materials are less pure and even small portion of soluble impurities can essentially influence the crystal growth. Consequently, preference was given to analytical reagent, especially of The British Drug House Limited and Merck for 99.9% pure organic materials (naphthalene, o-nitrophenol, α -naphthol, diphenylamine, benzil, diphenyl, benzoic acid, benzamide, phenanthrene and α -naphthylamine) and Alfa Aesar for 99.999%

pure metals (Pb, Sn, Bi and Cd). The melting temperatures and enthalpies of fusion of the experimental homogeneous materials were determined by thaw-melt technique and thermal analysis (DSC Linseis STA PT-1000) and found consistent with the literal values (Lide, 2009).

2.2 Diagrams of state

Mixtures of the constituent materials were prepared covering the whole of the mole fraction composition range (binary organic systems) and weight percent composition converted into mole fraction composition range (binary metallic systems). The homogeneity in mixtures was ascertained by heat-chill method. The solidus-liquidus equilibrium curves of binary organic systems were studied by thaw-melt method, while those of binary metallic systems by thermal analysis.

2.3 Heterogeneous nucleation

Nucleation studies of binary organic systems being transparent in nature were performed following the procedure referred earlier (Sharma et al., 2004a). A nearly constant amount (4.0 g) of each composition of the systems was carefully taken into different pyrex tubes of uniform internal diameters. The sample tubes were sealed and successively undertaken for spontaneous nucleation observations in a paraffin bath manipulated at the temperature $\sim 30\text{K}$ higher than the melting temperature of each specimen. The bath temperature attained by the tube was ensured by thermometric technique before cooling process for spontaneous crystallization. The melt-nucleation process for each sample tube was recycled for several observations (minimum six runs) necessary in comparative estimate of undercooling. Maximum care was taken to perform undercooling experiments for different compositional melts under almost identical conditions by keeping the volume of the melt and the rate of cooling nearly the same in all the cases.

2.4 Anisotropic growth velocity

The experimental technique for determining the anisotropic growth velocity from different compositional melts of binary organic systems was similar to that adopted earlier (Sharma, 2003). The velocity of anisotropic growth from a definite compositional melt was measured in a transverse direction along the length $10 \times 10^{-2} \text{ m}$ and internal diameter of $6 \times 10^{-2} \text{ m}$ of the pyrex tube with terminal right-angled bends. The experimental tube was placed in a paraffin thermostat kept constant to $\pm 0.01 \text{ K}$ for experimental observations at several degrees of undercooling. The rate of advance of the crystal boundary was recorded by stop watch. Several observations (minimum six runs) of anisotropic growth velocity were recorded for each compositional melt at the selected experimental supercooling. The results are found less accurate from the eutectic melts of each system, since within the observation time the growing crystal front moved only a very small distance which could not be ascertained very accurately.

2.5 Rheological measurements

Viscosities of different compositional melts representing the complete mole fraction composition range of each binary organic system, were measured relative to the literal viscosity values of reference liquid p-xylene (Lide, 2009) in a paraffin bath with an accuracy of $\pm 0.05 \text{ K}$ in the temperature range 391-408 K. The viscometer employed for the purpose was modified as shown in Fig.A. Likewise, an attempt was made for the first time to

measure surface tension of binary α -naphthylamine-diphenylamine eutectic melt system related to the reference liquid p-xylene (Lide, 2009 & Edward, 1930) in the aforementioned bath in the temperature range 323-373 K using modified stalagmometer (Fig.B) compatible with the suitability of the experiment. The viscometer and stalagmometer are essentially modified by the side tube 'S' connecting the bulb 'B' right below the capillary of the viscometer to its upper mark 'X', and the bulb 'B' of the stalagmometer to the upper mark 'X' in the light of the following:

- i. the excess pressure of the melt increasing the kinetic energy of the flow is made to escape through the side tube 'S' leaving the experimental volume of the melt to flow freely down the capillary under its own gravity. This minimizes kinetic energy correction.
- ii. the bulb 'B' is an important component of the viscometer in connection with the elimination of upward thrust due to surface tension which could resist the free flow of the melt. The bulb 'B₁' of the stalagmometer would also overcome in nipping the resistance.
- iii. the advantage of the modified stalagmometer over other stalagmometer lies in the concept that the relative surface tension measurements of low temperature solid materials in general and binary or ternary solid mixtures in particular can easily be undertaken at different temperatures in an air oven or a suitable bath to assess the specific interactions in their respective melts' surface.

2.6 Growth technique

2.6.1 Anisotropic crystal form

Pyrex tubes of nearly the same dimensions were selected as dies to achieve anisotropic rod form of crystals from different compositional melts in the following experimental setup. An experimental pyrex tube containing half-full melt of freshly prepared eutectic or non-eutectic phase, was vertically clamped to the centre of an empty graduated beaker (volume capacity 1dm³) arranged in an oven set at a temperature ~ 30 K higher than the melting temperature of the experimental specimen. The molten mass was nucleated by circulating water in case of organic melt, and silicone oil in case of metallic melt from their respective reservoirs manipulated to perforate at ~ 300 K. The melt in the tube started nucleating when the rising level of water or silicone oil as the case may be, just touched the bottom of the tube creating sharp temperature gradient at the solidus-liquidus interface that resulted in the occurrence of melt-growth process anisotropically towards longitudinal direction along the length of the tube. In this manner, each compositional melt in a separate pyrex tube was grown to crystal form at 18 different intervals in the experimental time range 5-45 min. The crystal sample grown anisotropically was removed from an experimental pyrex tube by warming its section in both longitudinal and transverse directions just to glide the solidus mass to its easier exit.

2.6.2 Isotropic crystal form

Nuclei of critical size almost grew out instantaneously in all directions when a pyrex tube containing the melt at ~ 30 K higher than its freezing temperature was dropped vertically into an ice bath maintained at ~ 273 K. This particular mode of solidification is presumed to be time independent and thereby zero order reference growth. The solidified crystal from the tube was removed following the aforementioned procedure. A good many crystal samples of eutectic and akin mass eutectic compositions, and the constituent materials were

grown isotropically and anisotropically from their respective melts at different but nearly constant growth rates determined by circulating approximately the same volume of water or silicone oil for each experimental interval. An interesting feature of time variable growth is the yield of moderate anisotropic growth velocity ($\sim 2.90 \times 10^{-7} \text{ m}^3\text{s}^{-1}$) determined by setting the flow-interval of reservoir liquid at $\sim 5 \times 10^{-4} \text{ m}^3$ for 30 min. At this moderate solidification rate, the growth from an akin mass compositional melt of each experimental binary organic system is found to be more efficient in promoting its mechanical properties which are superior, as revealed by the experimental evidences in the present work, to those of the eutectic composite and constituent materials grown under the same environmental conditions.

2.7 Mechanical test

2.7.1 Macrorupture test

The experimental samples after dimensions' ascertainment were subsequently subjected to tensile, modulus of rupture (flexural) and compressive tests in a VEB Thuringer Industrie Werk Rauenstein tensometer where a steadily increasing load would determine the rupture force of a crystal specimen until it shows least resistance. These tests were performed visually watching the fracture process. Though the tests are of conventional nature, yet can be related also to the macro scale, particularly relevant to engineering products.

2.7.2 Microdeformation test

Metallic systems are suitable materials for micro hardness testing because of atomically rough surfaces. Indentations were induced on selected points chosen diagonally on an anisotropically or isotropically grown specimen at room temperature (~ 300 K) using Vickers microhardness tester attached to an incident-light metallurgical research microscope (Neophot-2) in the applied load range 10×10^{-2} - 100×10^{-2} N. For each test, a very small diamond indenter having pyramidal geometry was forced into the surface of the specimen at room temperature and the size of the indent was found growing with rising applied load.

2.8 Microscopic studies

2.8.1 Optical microscopic examination

The micro-slides of binary organic eutectic and akin mass composite phases grown anisotropically and isotropically were examined in a polarizing microscope to view the growth habits of crystallites which were later photographed.

2.8.2 Electron microscope examination

The metallic specimens grown isotropically and anisotropically were polished at room temperature by following the procedure referred in connection with the analogous problem (Caram et al., 1991). A thin layer of a specimen etched in ferric chloride was mounted on stub with gold coated holder and examined in a scanning electron microscope (Jeol T-330) for microgrowth observations. Several grown samples of eutectic and akin mass eutectic composites were viewed in this manner and the growth habits acquired by the growing eutectic phases during solidification process at different growth rates were photographed.

2.9 X-ray diffraction (XRD) studies

X-ray diffraction patterns of eutectics and non-eutectics were scanned in a Rigaku X-ray diffractometer with Cu K_{α} radiation of wave length $1.540 \text{ \AA}$ at room temperature to reveal their nature of combination.

3. Observations

The experimental evidences offer convincing similarity among binary organic systems in physical behavior and characterization. Metallic systems Sn-Cd and Pb-Sn also exhibit alike behavior with distinct morphology (regular) from that (complex regular) of Cd-Bi and Pb-Bi systems. In view of physical habits' resemblance of the systems, two representative examples, namely, naphthalene-o-nitrophenol from organic systems and Sn-Cd from metallic systems shall be the main components revealing the objectivity of the work. The melting temperatures of their constituent materials are recorded in Table1, also containing

their entropies of fusion and α -values (where $\alpha = \xi \Delta S_f / R$, is called dimensionless entropy, since R is the molar gas constant) as well computed thereby.

material	melting temperature(K)	enthalpy of fusion (kJmol ⁻¹)	entropy of fusion (Jmol ⁻¹ K ⁻¹)	α -value
naphthalene	353.00	19.00	53.81	6.47
o-nitrophenol	318.70	17.50	54.91	6.60
Sn	509.00	7.00	13.70	1.65
Cd	597.00	6.10	10.22	1.23

Table 1. Melting temperatures, enthalpies and entropies of fusion, and α -values

Diagrams of state representing the experimentally determined liquidus temperatures and theoretically computed ideal temperatures of naphthalene-o-nitrophenol and Sn-Cd systems are represented in Fig.1 (a and b). The undercooling curve resulting in by experimentally determined temperatures of spontaneous crystallization for naphthalene-o-nitrophenol system is also included in its phase diagram (Fig.1a). Thermodynamic analysis of the systems reveals specific molecular interactions in their molten states and hence their non-ideal nature. The non-ideal character of the system is authenticated by excess functions (E), namely, Gibbs free energy (G^E), entropy (S^E) and enthalpy (H^E), computed by the following standard relations (Sharma et al.,2004b):

$$G^E = RT[x_1^l \ln \gamma_1^l + x_2^l \ln \gamma_2^l] \quad (1)$$

$$S^E = -R[x_1^l \ln \gamma_1^l + x_2^l \ln \gamma_2^l + Tx_1^l (\partial \ln \gamma_1^l / \partial T)_P + Tx_2^l (\partial \ln \gamma_2^l / \partial T)_P] \quad (2)$$

$$H^E = -RT^2[x_1^l \ln \gamma_1^l + x_2^l \ln \gamma_2^l] \quad (3)$$

where x_i^l and γ_i^l respectively, denote the mole fraction and activity coefficient of the eutectic phase i ($i = 1, 2$) in binary mixture of liquidus temperature T , with the enthalpy of fusion $\Delta_f H_i^\circ$, obtained by thermal analysis, at its melting point T_i° . The superscript l refers to the condensed phase of the systems. The differential quantities $(\partial \ln \gamma_1^l / \partial T)_P$ and $(\partial \ln \gamma_2^l / \partial T)_P$ are the slopes of the liquidus lines obtained by plotting activity coefficients of the eutectic phases in eutectic mixtures versus their liquidus temperatures.

The quantitative magnitudes of G^E , S^E and H^E , obtained by Eqs. (1, 2 and 3) at different mole fraction compositions with their respective liquidus temperatures, are plotted in Fig.2. The minimal and maximal inflections respectively of G^E , and S^E and H^E at the eutectic compositions evidentially evince their obedience to the spontaneity criteria and Planck probability distribution ($S = k \ln w$, k and w respectively being the Boltzmann constant and the configurational weight of the phase molecules). Microstructural parameters structuring the modal microstructures of the systems drive movement strength from excess functions (Sharma et al., 2008,2009) to overcome their faults called lamellar faults (Hunt & Jackson, 1966). The following symmetry relations obtained from the limit of undercooling (Table 2) are found consistent over the whole of the compositional range expressing their obedience to the criteria of nucleation theory:

$$\xi = \frac{T_c}{T_m} \quad (4)$$

$$\frac{\Delta T}{T_m} = \frac{T_m - T_c}{T_m} \quad (5)$$

at which ΔT , T_m and T_c respectively, are the undercooling, liquidus and spontaneous crystallization temperatures. ξ is a crystallographic factor which is less than and almost one, and represents fraction of total number of neighbors situated in the newly formed crystal layer.

Fig. 1. Diagrams of State

Fig. 2. Excess functions G^E , H^E and S^E , a) Naphthalene- o-nitrophenol system, b) Sn-Cd system

mole fraction of naphthalene	liquidus temperature T_m (K)	temperature of spontaneous crystallization T_c (K)	maximum undercooling $\Delta T=(T_m- T_c)$ (K)	$\xi = \frac{T_c}{T_m}$	$\frac{\Delta T}{T_m} \times 10^{-2}$
0.0	318.70	307.20	11.50	0.96	3.61
0.1	315.20	303.10	12.10	0.97	3.84
0.2	311.70	299.00	12.65	0.96	4.06
0.3	304.70	294.70	10.00	0.97	3.28
0.33(e*):	303.70	293.20	10.50	0.97	3.46
0.4	313.70	304.70	9.00	0.97	2.87
0.5	321.20	312.40	8.80	0.97	2.74
0.6	329.70	319.80	9.90	0.97	3.00
0.7	339.90	327.70	12.20	0.97	3.59
0.8	343.20	333.70	9.50	0.97	2.77
0.9	348.70	339.10	9.60	0.97	2.75
1.0	353.50	343.70	9.80	0.97	2.77

Table 2. Heterogeneous nucleation data for the naphthalene-o-nitrophenol eutectic system. (e*: eutectic)

The kinetics of anisotropic crystallization velocity, V , from the molten states of the eutectic and non-eutectic phases follows the parabolic law:

$$\log V = \log k + n \log \Delta T \quad (6)$$

since k and n respectively, being the intercept and the slope are determined from the straight lines obtained by plotting $\log V$ versus $\log \Delta T$ (Fig.3) wherein n equals or almost equals 2 for the system. The observed anisotropic velocity of crystallization estimated from the eutectic melt is relatively low in comparison to its values from the non-eutectic melts ($\Delta T = 10$ K).

Fig. 3. Anisotropic velocity of crystallization at various degrees of undercooling for naphthalene- o-nitrophenol system: (I) pure naphthalene; (II) pure o-nitrophenol; (III)-(V) 0.2, 0.4 and 0.3250 (eutectic) mole fractions of naphthalene.

The viscosities for different compositional melts of the naphthalene-o-nitrophenol system measured in the temperature range 337–402 K are represented in Fig.4, which evidentially predicts the anomalous viscous behavior by the eutectic compositional melt, particularly in the vicinal temperatures to its liquidus temperature and this unusual behavior starts declining with rising temperature and completely evanesces at 402 K.

Fig. 4. Viscosity-composition plot for naphthalene-o-nitrophenol system at different temperatures (e^* eutectic)

The viscosity data of the system in the experimental temperature range follow the Arrhenius equation:

$$\log \eta = \log \eta_0 + \frac{E_{\text{vis}}}{2.303RT} \quad (7)$$

the parameters η and E_{vis} respectively, being the viscosity and activation energy for viscous flow of any compositional melt of the system at different rising temperatures T . The $\log \eta$ values are plotted against $1/T$ for any compositional melt at different temperatures and the slope of the best straight line obtained thereby, determines the activation energy and the intercept of the line yields the constant η_0 for that composition. The activation energy data (Table 3) for experimental compositional melts of the system obtained likewise reveal the predominance of activation energy for the eutectic melt over its values for the pre- and post-eutectic melts, which finally, consociates with a normal value of the system at 402 K (Fig.5).

I o-nitrophenol

XI naphthalene

II-X mixtures with 0.1, 0.26, 0.32 (eutectic), 0.38, 0.46, 0.52, 0.7, 0.8 and 0.9 mole fractions of naphthalene respectively

Fig. 5. A plot of $\log \eta$ vs T for naphthalene-o-nitrophenol system

mole fraction of naphthalene	activation energy E_{vis} ($\times 10^{-2} \text{ kJmol}^{-1}$)	mole fraction of naphthalene	activation energy E_{vis} ($\times 10^{-2} \text{ kJmol}^{-1}$)
0.00	3.96	0.50	3.92
0.10	3.72	0.57	3.86
0.26	3.62	0.80	3.78
0.33 (e*)	3.88	0.90	3.64
0.38	3.64	1.00	3.56
0.46	3.82		

Table 3. Activation energy data in the temperature range 337-402 K for naphthalene- o-nitrophenol system in the paraffin thermostat with an accuracy of $\pm 0.05 \text{ K}$

Alike, the surface tension, γ , measurements for different compositional melts of the system α -naphthylamine-diphenylamine in the temperature range 323-373 K (Fig.6) offers supporting evidence to the abnormal tendency of the phase molecules in the eutectic compositional melt.

The surface tension data of the system in the experimental temperature range obey Eotvos empirical equation:

$$\gamma = k(T_c - T) [d/M]^{3/2} \quad (8)$$

where k is the constant with numerical value $2.1 \times 10^{-7} \text{ JK}^{-1}\text{mol}^{-2/3}$ valid for almost all materials and the parameters T_c , T , d and M respectively, are the critical temperature at which internal pressure equals 1 atmospheric pressure, experimental temperature, density and molar mass. The situation at which T_c equals T , the surface tension approaches zero. Figure 7 is a plot showing the variation of surface tension over its entire compositional

Fig. 6. Surface tension-composition plot for α -naphthalene-diphenylamine system at different temperatures, e^* eutectic

I diphenylamine

XIII α -naphthalene

II-XII mixtures with 0.1, 0.2, 0.3, 0.4, 0.46, 0.5, 0.55, (eutectic) 0.6, 0.7, 0.8, 0.9 molfractions α -naphthalene respectively

Fig. 7. A plot of γ vs temperature for naphthalene-diphenylamine system range with increasing temperature. The temperature greatly effects the surface tension reducing it to its limiting value at $T = T_c$, an experimental observation possible only when there is no meniscus or barrier between the melt and the vapors (1 atm pressure). This implies that experimental observations of both viscosity and surface tension strongly support the excess functions predicting prominent molecular interactions and consequently, the structural changes in the eutectic melt evincing the endothermic nature of the systems.

The germinating crystallites from organic eutectic phases melt in an ice bath environment (~ 273 K) are of short size, aggressive, non-attaching and crossing each other showing no crystallite-matrix relationship resulting in overall morphology amply rich in small spherulites (Fig. 8a). The spherulitic density (spherulites per unit area) decreases with

Fig. 8. Morphological diversity of naphthalene-o-nitrophenol eutectic composite materials by different modes of solidification (100 x). Microstructure of eutectic composite material in (a) ice bath (~ 273 K), isotropic growth, (b) at room temperature (~ 300 K), random growth, (c) at 315 K, (d) at moderate anisotropic growth from bottom to top ($\sim 2.90 \times 10^{-7} \text{ m}^3\text{s}^{-1}$), (e) akin mass eutectic composite material at moderate anisotropic growth from bottom to top ($\sim 2.90 \times 10^{-7} \text{ m}^3\text{s}^{-1}$), (f) eutectic composite material at anisotropic growth from bottom to top ($\sim 2.14 \times 10^{-7} \text{ m}^3\text{s}^{-1}$)

decreasing undercooling (Fig. 8b) and spherulitic size increases (~ 300 K) showing its centre as the seat of nucleation which finally evanesces (Fig.8c) with further undercooling decrease (~ 315 K). Nevertheless, the crystallites' growth habits of eutectic and akin mass eutectic compositions can be transformed from spheric or irregular morphology to unique fibrous and lamellar structures consisting of crystallites which are non-aggressive, attaching and embedded parallel to each other reinforcing the matrix by anisotropic growth modes of

solidification. In the domain of solidification rates, microstructures represented by Figs. 8d and 8e are respectively discovered for eutectic and akin mass eutectic composites of naphthalene-o-nitrophenol system at moderate anisotropic growth rate ($\sim 2.90 \times 10^{-7} \text{ m}^3\text{s}^{-1}$). Both the microstructures indispensably exhibit long and continuous crystallites with damaged free surfaces embedded parallel to each other along the growth direction. The akin mass eutectic composite structure is annexed superior to that of eutectic composite, vis-à-vis strength point of view. Figure 8f is a microstructure of the eutectic phases developed at anisotropic growth velocity $\sim 2.14 \times 10^{-7} \text{ m}^3\text{s}^{-1}$ showing crystallites of short size and disconnected with aligning tendency to the longitudinal growth direction. On the contrary, pure eutectic components grew out from their respective melts as lamellar cells that crystallized either from the bulk of the melt or through secondary nucleation during the entire anisotropic solidification process. In view of anisotropic growth ability to organize the growing eutectic phases from the molten state, microstructures represented by Fig.9 (a, b and c) comprising of aligning lamellae, respectively are the specimens of Sn-Cd eutectic phases grown at moderate ($\sim 2.90 \times 10^{-7} \text{ m}^3\text{s}^{-1}$), post-moderate ($\sim 3.50 \times 10^{-7} \text{ m}^3\text{s}^{-1}$) and pre-moderate ($\sim 2.30 \times 10^{-7} \text{ m}^3\text{s}^{-1}$) anisotropic growth rates. The basic distinction in morphologies of non-metallic and metallic eutectic systems lies in the thermodynamic concept (Ovsienko et al., 1980) that coupled growth occurs when both phases have low entropies of fusion ($\alpha < 2$); i.e.; the lamellae or crystallites of the phases grow in contact resulting in regular structure with their round growth fronts and the overall growth is termed non-faceted-non-faceted (nf-nf). A coupled growth doesn't occur when both the eutectic phases have high entropies of fusion ($\alpha > 2$) and consequently a regular structure result in consisting of crystallites or lamellae of the phases that grow side by side near each other with sharp growth fronts and the type of the growth is differentiated faceted-faceted (f-f). A complex regular structure comprising of either nf-f lamellae or nf-f crystallites is produced when the entropy of fusion is low ($\alpha < 2$) in one phase but high ($\alpha > 2$) in the other and the growth being the intermediate case, is distinguished non-faceted-faceted (nf-f). In the naphthalene-o-nitrophenol system, both the phases have high entropy of fusion ($\alpha > 2$) furnishing an irregular structure, whereas in Sn-Cd system, both the phases have low entropy of fusion producing regular morphology. Regular morphology implies that the spacing among lamellae or crystallites must appear constant throughout the structure; otherwise irregular in nature. For this very reason, rod-type growth has a perfect ordered structure merely because of periodic constant inter-rod spacing, whereas lamellar structure proves to be less regular sheerly because of the movement of lamellae or crystallites termed lamellar or fiber faults that would become the cause of slight uncertainty in their spacing consistency. Macro-rupture of naphthalene-o-nitrophenol system is virtually a collection of the following stress-strain fractures (Boyer, 1999; Callister, 2006 & Kollmann, 1975):

$$(i) \quad \text{Modulus of rupture, } Y_{rup} = \frac{PL}{\pi r^3} \text{ (circular cross section)} \quad (9)$$

$$(ii) \quad \text{Tensile strength, } T_{rup} = \frac{P}{\pi r^2} \quad (10)$$

$$(iii) \quad \text{Compressive strength, } \sigma_{rup} = \frac{P}{\pi r^2} \quad (11)$$

where the parameters P , L and r respectively, are the applied load in Newton force (N), span, and radius of an experimental specimen in metres, herewith P and r being dependent on the dimensions of the specimen and nature of the fracture, have variable magnitudes. In each fracture, the specimens yielding strength deviations by $>15\%$ from the averaged result were not included in the computed mechanical property data presented for eutectic and akin mass eutectic composite phases grown at both moderate anisotropic ($2.90 \times 10^{-7} \text{ m}^3\text{s}^{-1}$) and isotropic ($\sim 273 \text{ K}$) solidification rates, in Table 4.

Fig. 9. Lamellar growth of Sn-Cd eutectic alloy in the moderate growth region (1500x): (a) lamellar Sn-Cd eutectic at moderate anisotropic growth from bottom to top ($\sim 2.90 \times 10^{-7} \text{ m}^3\text{s}^{-1}$), (b) disconnected lamellar Sn-Cd eutectic at anisotropic growth from bottom to top ($\sim 3.50 \times 10^{-7} \text{ m}^3\text{s}^{-1}$), (c) disconnected and short lamellae structure of Sn-Cd eutectic at anisotropic growth from bottom to top ($\sim 2.30 \times 10^{-7} \text{ m}^3\text{s}^{-1}$).

The mechanical observations data, obtained by Eqs. (8, 9 and 10) for the entire composition range of the naphthalene-*o*-nitrophenol system at constant moderate anisotropic growth ($\sim 2.90 \times 10^{-7} \text{ m}^3\text{s}^{-1}$), are plotted in Fig.10, implicitly indicating the predominance of the akin mass eutectic composition. In search of authenticity onto this experimental evidence, both eutectic and akin mass eutectic composite materials grown at constant but different anisotropic growth rates, were subsequently subjected to tensile, flexural (modulus of rupture), and compressive tests and the computed tensile strength data are represented in Fig.11, while data for modulus of rupture and compressive modes are recorded in Table 5, supporting the predominance of the akin mass eutectic composite over eutectic composite, both expressing obedience to the Weibull distribution. Evidently, this aspect generates the strength-growth relationship which follows an identical form of the Weibull probability distribution curve inculcating the obedience of the microstructural parameters, namely, crystallite diameter, crystallite length, crystallite length distribution, volume fraction of crystallites, and the alignment and packing arrangements of crystallites, to the distribution.

Fig. 10. Variation of mechanical properties of naphthalene-o-nitrophenol system at moderate growth ($\sim 2.90 \times 10^{-7} \text{m}^3 \text{s}^{-1}$) (i) modulus of rupture (ii) tensile strength (iii) compressive strength a^* akin mass composition, e^* eutectic

Fig. 11. Plots of tensile strength at variable growth (i) akin mass composition and (ii) eutectic composition of the naphthalene-o-nitrophenol system

mechanical property	akin mass composition		eutectic composition		Noneutectic materials			
	moderate anisotropic growth	isotropic growth	moderate anisotropic growth	isotropic growth	naphthalene		o-nitrophenol	
					moderate anisotropic growth	isotropic growth	moderate anisotropic growth	isotropic growth
(i) Modulus of rupture Y_{rup} (Mpa)	7.90	2.96	5.10	2.50	1.30	0.60	1.00	0.50
(ii) Tensile Strength T_{rup} (Mpa)	8.60	3.40	6.00	2.90	1.80	1.0	1.80	1.00
(iii) Compressive Strength σ_{rup} (Mpa)	9.20	3.70	6.70	3.30	2.30	1.10	2.40	1.30

Table 4. Mechanical properties of akin mass and eutectic compositions of naphthalene-o-nitrophenol system at moderate anisotropic ($\sim 2.90 \times 10^{-7} \text{m}^3 \text{s}^{-1}$) and isotropic ($\sim 273 \text{K}$) growth rates.

growth velocity ($V \times 10^{-7} \text{m}^3\text{s}^{-1}$)	akin mass composition		eutectic composition	
	modulus of rupture Y_{rup} (MPa)	compressive strength σ_{rup} (MPa)	modulus of rupture Y_{rup} (MPa)	compressive strength σ_{rup} (MPa)
0.8	1.10	2.80	0.70	1.50
1.0	1.80	3.50	1.00	1.90
1.2	2.80	4.40	1.30	2.40
1.4	4.20	5.10	1.70	2.70
1.6	5.40	6.00	2.30	3.70
1.8	6.20	6.80	2.80	4.30
2.0	6.80	7.60	3.30	5.00
2.2	7.10	8.20	3.80	5.70
2.5	7.70	8.90	4.20	6.30
2.7	7.80	9.10	4.40	6.50
2.8	7.90	9.20	4.50	6.60
3.0	7.80	9.10	4.40	6.50
3.2	7.60	9.00	4.30	6.40
3.5	7.10	8.80	3.80	6.00
4.0	6.10	7.80	2.70	5.20
4.5	4.80	6.20	2.00	3.80
5.0	3.70	4.70	1.50	2.90
5.5	2.60	3.80	1.10	2.30
6.0	2.10	3.00	0.80	1.80
6.2	1.70	2.70	0.60	1.60
7.0	1.20	1.80	0.30	1.50
7.5	0.80	1.30	0.20	0.80

Table 5. Variation of modulus of rupture and compressive strength with growth velocity of naphthalene- o-nitrophenol binary system.

Micro deformation test virtually represents the Vickers microhardness, H_v , which is a measure of a materials resistance to localized plastic deformation (e.g., a small dent or a scratch) by the stress-strain relation (Beigh et al., 1995 & Hayden, 1965):

$$H_v = 1.8544 P/d^2 \quad (12)$$

herewith, P signifies the same as mentioned above, whereas the parameter d denotes the average diagonal length of the indentation mark in meter and varies with the size of the cracks.

The variation of Vickers microhardness for specimens of the eutectic alloy Sn-Cd grown by different modes of experimental anisotropic solidification rates at constant applied load of $50 \times 10^{-2} \text{ N}$ for a specified interval of 20s, offers supporting evidence to the essence of an identical form of the Weibull distribution curve (Fig.12) exhorting the strength-growth relationship. The specimens of the eutectic alloy Sn-Cd obtained by moderate anisotropic ($\sim 2.90 \times 10^{-7} \text{ m}^3\text{s}^{-1}$) growth process inflicted with indentation impressions by a constant load ($60 \times 10^{-2} \text{ N}$) at different indentation times (Fig.13 a, b and c), measurement of crack length and growing indents' dimensions by a variable load are illustrated in terms of photomicrographs in Fig.13 (d, e and f). A maximum care was exercised to consider only

well defined cracks developed during indentation process. The average crack length of all such cracks was estimated for a particular indentation impression. The crack length was measured from the centre of the indentation mark to the tip of the crack (Fig.13d). The size growth with a variable load is represented in Fig.13 (e and f).

Fig. 12. Variation of micro hardness with growth velocity for the eutectic alloy Sn-Cd at constant applied load of $50 \times 10^{-2} \text{ N}$ for a specified interval of 20 s

Fig. 13. Photomicrographs showing indentation impressions inflicted on the anisotropic specimens of the eutectic alloy Sn-Cd (625x): (a) size of indentation with a load of $60 \times 10^{-2} \text{ N}$ at 50s; (b) size of indentation with a load of $60 \times 10^{-2} \text{ N}$ at 100s; (c) size of indentation with a load of $60 \times 10^{-2} \text{ N}$ at 150s; (d) measurement of crack length; (e) size of indentation with a load of $20 \times 10^{-2} \text{ N}$; (f) size of indentation with a load of $40 \times 10^{-2} \text{ N}$.

Figures 14 and 15 respectively predict the variation of microhardness with increasing indentation time and applied load. The analysis of microhardness is summarized in Figs. 16-19.

Fig. 14. A plot showing invariability of micro-hardness with variable indetation time for eutectic alloy Sn-Cd for constant applied load. P (30×10^{-2} N)

Fig. 15. Dependence of micro-hardness on applied load for eutectic alloy Sn-Cd for constant indetation time, t (20 s)

Fig. 16. Relationship between $\log P$ and $\log d$ for the eutectic alloy Sn-Cd

Fig. 17. Variation of d^n and d^2 for the eutectic alloy Sn-Cd

Fig. 18. Relationship between $\log (P-W)$ and $\log d$ for eutectic Sn-Cd

Fig. 19. A plot showing variation of cracklength (l) with applied load (P) for eutectic alloy Sn-Cd

The parameters extracted from the analysis are recorded in Tables 6-7.

eutectic alloy	n	10^6Nm^{-2} k_1	10^6Nm^{-2} k_2	k_2/k_1	W (10^{-3}N)	W/k_1 (10^{-8}m^2)
Sn-Cd	1.5672	1.3824	7.4155	5.3642	8.7868	6.3562

Table 6. Hardness analysis constants for the eutectic alloy Sn-Cd

applied load $P \times 10^{-2}\text{N}$	crack length ($l \times 10^{-2}\text{m}$)	fracture toughness K_c ($\text{Nm}^{-3/2}$)	brittleness B_i ($10^6\text{m}^{-1/2}$)	hardness H_v (MPa)	yield strength σ_y (MPa)
10	0.3	89.29	1.79	160	53.33
20	0.7	84.03	1.37	115	38.33
30	0.9	50.19	1.79	90	30.00
40	1.2	43.62	1.60	70	23.33
50	1.6	35.36	1.69	60	20.00
60	1.9	32.72	1.68	55	18.33
70	2.1	32.89	1.73	57	19.00
80	2.7	25.74	2.29	59	19.67
90	3.2	22.48	2.67	60	20.00
100	3.4	22.78	2.68	61	20.33

Table 7. Hardness parameters for the eutectic alloy Sn-Cd

The XRD data summarized in Table 8 and X-ray patterns represented by Fig. 20 for the eutectic alloy Pb-Bi, selected as representative example in the current work, specify that the number of peaks and intensities exhibited by the eutectic alloy are complementary to its constituent phases.

Fig. 20. X-ray diffraction patterns of the eutectic alloy Pb-Bi

	Pb		Bi		Pb-Bi eutectic		Corresponding Planes (hkl)
S. No	Pos [2°TH]	d-spacing [Å]	Pos [2°TH]	d-spacing [Å]	Pos [2°TH]	d-spacing [Å]	
1	6.487	13.6113	6.224	14.189	22.469	3.95389	Bi (003)
2	28.918	3.0850	22.220	3.997	27.297	3.26449	Bi (012)
3	31.448	2.8423	22.805	3.8962	29.443	3.03125	Pb (110)
4	36.440	2.4636	24.091	3.6911	30.873	2.89399	Pb (111)
5	43.381	2.0842	26.821	3.3213	33.344	2.68499	Pb (111)
6	49.973	1.8236	27.427	3.2492	38.107	2.35960	Bi (104)
7	52.407	1.7444	31.502	2.8376	39.841	2.26084	Bi (110)
8	56.271	1.6335	37.740	2.3817	43.192	2.09287	Pb (200)
9	62.314	1.4888	38.211	2.3524	46.117	1.96670	Bi (113)
10	65.414	1.4255	39.872	2.2589	48.953	1.85921	Bi (202)
11	77.135	1.2353	44.826	2.0202	52.218	1.75035	Pb(220)
12	77.397	1.2321	45.684	1.9843	56.477	1.62804	Bi (024)
13	85.579	1.1339	46.199	1.9634	61.084	1.51583	Bi (200)
14	85.852	1.1310	48.511	1.8751	61.895	1.49790	Pb (311)
15	88.363	1.1052	48.954	1.8591	63.376	1.46641	Bi (211)
16	88.646	1.1024	49.561	1.8378	64.299	1.44758	Bi (122)
17	89.714	1.0921	56.286	1.6331	64.856	1.43648	Pb (222)
18			59.566	1.5507	69.979	1.34333	Bi (214)
19			61.325	1.5140	71.207	1.32314	Bi (009)
20			62.434	1.4862	72.258	1.30647	Bi (300)
21			64.761	1.4383	80.478	1.19245	Bi (208)
22			67.682	1.3832	84.428	1.14645	Bi (119)
23			71.013	1.3262	86.472	1.12452	Bi (101)
24			72.110	1.3087	86.763	1.12149	Bi (217)
25			73.917	1.2812	87.328	1.11568	Bi (217)
26			75.542	1.2576	87.590	1.11302	Pb (420)

Table 8. X-ray analysis for the eutectic alloy Pb-Bi

4. Analysis and discussion

The deviations of the systems from ideal regions covered by their respective diagrams of state (Fig.1) consisting of solidus-liquidus equilibrium curves, predict specific interactions between unlike phase molecules or unlike atoms in the miscibility phenomenon. The thermodynamic analysis of the systems confirms the deviations (Fig.2) and comprehensively yields quantitative idea of the interactions, inasmuch the excess functions are being computed from experimentally determined parameters, are reliable and discovered expedient for predicting the phase equilibrium curves of binary systems (Sharma et al.,2004).

The heterogeneous nucleation data obtained from the limit of undercooling (Table 2) provide a lucid consistency in the symmetry relations, $\xi = T_c/T_m$ and $\Delta T/T_m$, which certainly authenticates the nucleation theory for the system entirety. This essential constancy in symmetry relations implicitly explores a definite relationship existing between the nucleating solidus form obtained from the limit of undercooling and the liquid structure conceived by the entropy of fusion.

The critical analysis of the plot (Fig. 3) shows that the anisotropic velocity of crystallization from binary compositional melts essentially decreases significantly with the gradual addition of one eutectic phase to the other. Consequently, the inferential interference of the eutectic phases decreases the crystallization velocity from the eutectic melt ($10 \times 10^{-4} \text{ms}^{-1}$) which is much lower than its value from the non eutectic melts; naphthalene ($158 \times 10^{-4} \text{ms}^{-1}$) and o-nitrophenol ($92 \times 10^{-4} \text{ms}^{-1}$) for fixed undercooling $\Delta T = 10\text{K}$. The kinetics of the anisotropic crystal growth being dependent on parabolic form, follow the dislocation mechanism wherein eutectic phases would diffuse and grow at the sites at which surface with the stages is formed owing to lattice imperfections and screw dislocations. These imperfections do intersect the surfaces and produce steps of one or more molecular diameters in height. These steps are the center of lattice disturbance and wind themselves in spirals during crystal growth. The logical growth concept extracted from the theoretical interpretation of the experimental observations is consistent with the diffusion growth of the eutectic phases from their binary melt that the growing phases mutually sustain the diffusion process through melt layer becoming rich in their concentration at different times of successive nucleation.

The anomalous behavior of viscosity (Fig.4) and surface tension (Fig.6) for the eutectic melt furnishes supporting evidence to the essence of molecular interactions conceiving magnitudes already delivered by the excess functions. The most probable structural change (configurational weight) in phase molecules occurs in the eutectic compositional melt owing to three phases' coexistence, resulting in significant molecular clusters' formation rich in one of the eutectic phases. The degree of molecular clustering tendency decreases as the temperature is gradually raised that would finally become the cause of limiting values of rheological parameters. The explanation for the higher value of the activation energy for the eutectic melt may be attributed to the following contributions: (i) the activation energy for viscous flow; (ii) the energy essentially required overcoming the molecular clusters' tendency. The molecular clustered array of atoms would inevitably result in an increase both in viscosity and surface tension, and a reduction in surface area. Consequent thereupon, the thermal energy expended to break the clusters would certainly exceed activation energy. An increasing temperature vitiates clustering phenomenon and the

particular temperature whereat it completely evanesces only the first contribution will be the activation energy. In the current work, the cluster-free flow is evidentially illustrated for viscosity at 402K in Fig.4 and for surface tension at 373 K (Fig.6). Likewise, the activation energy for eutectic compositional melts also consociates with normal value of the systems as indicated by dotted lines in Fig.5 for viscous flow of naphthalene-o-nitrophenol system at 402K, and in Fig 7 for loose surface flow of α -naphthylamine-diphenylamine system at 373K.

An irregular morphology (Fig 8 a -c) by f-f growth of eutectic phases from molten state results in because of their high entropies of fusion, since the formation of packs of their crystallites from the eutectic melt would arise under the influence of large thermal and mechanical stresses during the growth process. These stresses seem to be the cause of splitting the main single crystallite into separate single crystallites or groups of single crystallites in the absence of orientation relationship among faceted crystallites, eventually accomplishing an irregular morphology. The crystallite spherulitic form occurs at a large undercooling (~ 273 K) merely because the rich eutectic phase first nucleates and grows depleting the vicinal melt to be rich in other phase that also nucleates at a certain supersaturation. Alike, both the phases grow side by side. The large thermal and mechanical stresses influence the splitting of crystallites to occur along the direction and successive splitting lead to the formation of spherulites. As mentioned in the observation section, the moderate anisotropic growth is predominant finding in the domain of anisotropic solidification rates because of its aesthetics ability to produce in-situ oriented composite materials consisting of crystallites (Fig.8 d - e) and lamellae (Fig.9a) which are attaching, nonaggressive and embedded parallel to each other exhibiting nearly consistent periodic orientation relationship. Microstructure (Fig.9b) consisting of long and continuous parallel lamellae indicates lamellar faults (Hunt & Jackson, 1966). Microstructures (Figs.8f and 9c) consisting of crystallites or lamellae of short size, exhibit their disconnected but non aggressive alignment along the growth direction. The supercrescent crystallites or lamellae growth virtually produces the complete lamellar or rod-type microstructures. The eutectic phases with $\alpha > 2$ grow side by side near each other from binary melt resulting in lamellar structures of long and continuous non aggressive crystallites lamina (Fig.8d - e), whereas eutectic phases with $\alpha < 2$ grow supercrescently (edge-wise) from the melt to produce lamellar or rod-type lamina consisting of long and continuous nonaggressive lamellae which are embedded parallel to each other showing orientation relationship almost consistent throughout the structure (Fig. 9a).

An insight analysis of Table 4 reveals approximately one and a half to two fold enhancement in each mode of mechanical property of the akin mass eutectic composite material at the moderate anisotropic growth velocity ($\sim 2.90 \times 10^{-7} \text{ m}^3\text{s}^{-1}$) in comparison to the eutectic composite material and many fold superiority over its isotropic growth (~ 273 K) and constituent materials whether grown anisotropically or isotropically. The plot of Fig.10 drawn between different modes of macrohardness and the entire range of composition of the naphthalene-o-nitrophenol system at nearly constant moderate anisotropic growth velocity ($\sim 2.90 \times 10^{-7} \text{ m}^3\text{s}^{-1}$) strengthens the quantitative analysis by showing the predominance of the akin mass eutectic composition. Consequently, the curve (Fig.11) divides the experimental range of anisotropic growth velocity into three regions, namely, (i) slow growth region; (ii) moderate growth region and (iii) fast growth region. Among which, the moderate growth region, as is evident from the plot (Fig.11), would seem to be the most probable for producing lamellar or rod-type structures of both eutectic (Fig.8d) and akin

mass eutectic (Fig.8e) composite materials, since microstructural parameters appear to be nearly obeying the Gauss distribution. Consequentially, the microstructural crystallites of the akin mass composite material nearly follow the rod- type growth habits (Fig.8e) reinforcing the matrix where there is a perfect crystallite- matrix bond. On the contrary, the crystallites of the eutectic microstructure (Fig.8d) emerge with lamellar growth habits reinforcing the matrix but the crystallite- matrix bond exist with less perfection .The mechanical parameters of both the composite materials in the slow and fast growth regions are found comparable (Table 5 and Fig.11) because microstructural parameters express their obedience to the Weibull distribution in these regions showing no crystallite matrix relationship (Fig.8 a- c).The analysis necessarily involves a physical understanding of the relationship between the microstructures of materials and their mechanical properties .Evidentially, the curve (Fig.11) has two cut-off points corresponding to a lower strength limit in the slow and fast growth regions, and an upper strength limit in the moderate growth region. The later is equivalent to the theoretical strength of the matrix reinforced crystallites with damaged free surfaces, practically having no density of dislocations; i.e.; internal defects or surface flaws responsible for reduced strength. Likewise, the microhardness of the eutectic alloy Sn-Cd (Fig. 12) can be explained essentially involving its microstructures presented in Fig.9 on the similar dependence pattern with variable anisotropic growth velocity as tensile strength for the eutectic and akin mass eutectic composite materials of the naphthalene-o-nitrophenol system, follows in Fig.11. Implicit in the plots (Figs.11 and 12) is the concept that the variation of an anisotropic mechanical property over the entire range of growth velocity furnishes an evidence of its dependence as linear, optimum, and linear respectively in slow, moderate, and fast growth regions of solidification. An interesting finding to be noted from Tables 4 -5 is that, both eutectic and akin mass eutectic composite materials with isotropic growth (~ 273 K) are respectively found nearly twice and thrice stronger than that of their constituent materials merely because of their high specific modulus and high specific strength due to alignment of the crystallites although having dislocations. Likewise, moderate anisotropic growth of pure constituent materials is superior to their isotropic growth. Besides, the quantitative perusal of mechanical parameters presented in Tables 4 and 5,explores that the compressive mode slightly exceeds the tensile mode, which in turn shows an edge on modulus of rupture ($\sigma_{rup} > T_{rup} > Y_{rup}$).The inequality existing between mechanical modes essentially involves crystallite's length, which in the current work, accomplishes with the attachment of alike crystallites at different times and their efficiency in gripping and the reinforcing the matrix decreases with the reduction of crystallite's length. Crystallite-ends play important role in the fracture of short crystallite composite materials (Fig.8f and Fig.9c) and also in continuous crystallite composite materials (Fig.8d and Fig.9b), since the long crystallites may break down into discrete lengths.

Figure 13a-c reveals that the indentation size by a constant load (60×10^{-2} N) is independent of variable indentation times inferring the microhardness (H_v) to be so. The observation is strongly supported by Fig.14 indicating practically no change in the microhardness with the variable indentation time for a constant applied load of (30×10^{-2} N) at room temperature, which is consistent with the plastic deformation of the eutectic alloy that remains unaffected with variable indentation times. The nonlinear variation of microhardness (Fig.15) with variable applied load in the range $10 \times 10^{-2} - 100 \times 10^{-2}$ N at constant indentation time, t (20s) shows that H_v decreases with increasing load until about 60×10^{-2} N and thereafter , H_v tends to saturation which is full at 70×10^{-2} N.The qualitative explanation of the variation follows

that the indenter penetrates only surface layers at small loads, consequently, the effect is more pronounced at these loads. However, the increasing load increases the penetration depth that damages the inner layers more effectively to shattering the ability of hardness and ultimately, H_v appears to be independent of further applied load. The variation is in good agreement with the microhardness increase during early stages of plastic deformation (Brookes, 1986) but is contrary to Kick's law that H_v remains constant irrespective of the magnitude of applied load, P (Ascheron et al., 1989), qualitatively:

$$P = k_1 d^n \quad (13)$$

the Meyer's index, $n = 2$, accounts for constant H_v , and k_1 is a constant. A linear plot between $\log P$ and $\log d$ (Fig. 16) of Eq. (13) yields slope, n and intercept, k_1 at the particular applied load P that exists at $d = 10^{-3}$ m for any set of discrete data. The literature (Beigh et al., 1995) speaks that for any material with rising applied load H_v decreases when $n < 2$ and increases when $n > 2$. Both n and k_1 computed for the eutectic alloy Sn- Cd are recorded in Table 6. In fact, hardness is a measure of the resistance to localized plastic deformation, defined as the ratio W/A where W , the load in N and A , the area of indentation in m^2 . This implies that a load applied to a specimen is partially affected, since a portion of it being utilized to overcome the Newtonian resultant pressure, W of the specimen itself. Consequently, the H_v data of the specimen necessarily bound to be analyzed in terms of the actual load ($P - W$) acting on the specimen. The inference from this concept to be drawn is that a load less than W will not result in plastic deformation. In view of the resultant pressure, Hays and Kendall (Hays & Kendall, 1973) modified Eq. (13) in a manner:

$$(P - W) = k_2 d^2 \quad (14)$$

where k_2 is a constant and $n=2$, in the Eq. (14) called the logarithmic index, since W allows the limiting case to prevail where hardness is not markedly dependent on the load and the index can be evaluated by subtracting Eq. (13) from Eq. (14), which results:

$$d^n = (k_2 / k_1) d^2 + W / k_1 \quad (15)$$

again, the plot of Eq. (15) for d^n versus d^2 (Fig. 17) yields the slope k_2 / k_1 and the intercept W/k_1 . From the known value of k_1 , obtained by the plot (Fig. 16), k_2 and W computed thereby are recorded in Table 6 accomplishing the key data on microhardness. Furthermore, the plot (Fig. 18) of $\log (P - W)$ versus $\log d$ of Eq. (14) yields the value of the logarithmic index, $n < 2$, virtually evincing the validity of the Newtonian resistant pressure concept of the eutectic alloy Sn- Cd.

The fracture toughness, K_c is a measure of resistance to brittle fracture when a crack is developed on the alloy specimen and follows the relation:

$$K_c = P / \beta l^{3/2} \quad (16)$$

where l is the crack length measured from the center of the indentation mark to the crack tip. β is a numerical constant that depends on indenter's geometry, $\beta = 7$ for Vickers indenter. The satisfactory values of K_c can be obtained from Eq. (16) only if $l/a \geq 3$ or $l/a < 3$ respectively for median or radial crack system (Fig. 13 d) where $a = d / 2$. Table 7 records the parameter K_c and factor l/a at variable applied load P . The plot in (Fig. 19) shows the linear dependence of the crack length l with increasing applied load P . The

brittleness is usually expressed as the brittleness index B_i and can be estimated from K_c values by the relationship (Lawn & Fuller, 1975):

$$B_i = H_v / K_c \quad (17)$$

B_i values calculated by Eq.(17) for the eutectic alloy Sn- Cd are presented in Table 7. The yields strength of a material can be estimated from the microhardness values using the relation (Beigh et al., 1995) valid for $n < 2$:

$$\sigma_v = H_v / 3 \quad (18)$$

the yields strength of the eutectic alloy in the load range $10 \times 10^{-2} - 100 \times 10^{-2}$ N for constant indentation interval for 20 s is recorded in Table 7. All these parameters authenticate the plastic deformation of the eutectic alloy Sn- Cd and comprehensively accomplish the key data on hardness.

Figure 20 shows the XRD patterns for the eutectic alloy Pb-Bi containing a number of peaks and intensities of pure Pb and Bi atoms and expressing their immiscibility in the solidus eutectic, since the eutectic alloy does not indicate any peak of its own. The analysis implicitly, confirms the eutectic alloy to be a mechanical mixture of its constituent phases simulating weak interactions at their atomic levels. This implies that the eutectic composite is a terminal solidus solution.

5. Conclusions

Thermodynamic analysis of binary solidus-liquidus equilibrium data besides predicting the non-ideal nature of the systems, also offers an alternative thermal device for studying the phase equilibrium curve of binary systems, particularly capable of forming eutectic mixtures, in terms of excess functions G^E , S^E and H^E by variation in a mole fraction composition. The heterogeneous nucleation data verify the nucleation theory revealing the consistency in symmetry relations which predict that there is a definite relationship between the nucleation determined from the limit of undercooling and the liquidus structure of eutectic and non-eutectic melts associated with the entropy of fusion. The analysis of anisotropic growth kinetics emphasizes that the nucleation of eutectic phases from a binary melt follows the diffusion growth process. The rheological properties evince the essence of prominent molecular interactions in the binary eutectic melt and their emulation as a function of temperature. The excess functions and rheological properties are found complementary in predicting the non-ideal nature of binary eutectic systems and hence their liquidus structures. Microscopic studies confirm the f-f growth of the eutectic phases with $\alpha > 2$ and nf-nf growth of the eutectic phases with $\alpha < 2$, and also reveal their dependence on both temperature and modes of solidifications. The strength-growth relationship follows an identical form of the Weibull probability distribution curve that acquires two cut-off points corresponding to a lower strength limit in the slow and fast growth regions, and an upper strength limit in the moderate growth region. The moderate growth is an experimental evidence for being the most probable one in the domain of solidification modes in structuring the modal microstructure consisting of crystallites or lamellae reinforcing the matrix where there is a perfect crystallite-matrix bond. Of greater interest is the akin mass composition that predominates the domain of compositions in strength view point because

of its superior microstructure. The chapter also discusses the microhardness of binary metallic eutectic system Sn-Cd and the experimental evidences confirm the plastic deformation of the system. The chapter work authenticates with experimentally investigated strength data that the physical properties, and in particular, the mechanical behavior of a material depend on the growth habits to produce the modal microstructure of the material. X-ray studies affirm the mechanical combination of the eutectic phases resulting in terminal solidus solution and hence the eutectic solidus structure.

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