

Narrowband Interference Suppression in MIMO Systems

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1. Introduction

Multiple Input Multiple Output (MIMO) communication technology has received recently significant attention triggered by the rapid development of Orthogonal Frequency Division Multiplexing (OFDM) broad-band wireless and high speed wireline communication systems. Such systems are very sensitive to Narrowband Interferences (NBI) due to their relatively low transmission power. This type of signal interference can be found in the new unlicensed frequency bands, e.g., the Industrial Scientific Medical (ISM) band, coming from systems such as Bluetooth or microwave ovens which interfere with OFDM based Wireless Local Area Networks (WLAN), like Hiperlan II. Other examples of NBI, typical for Digital Subscriber Line (DSL) communications, are strong Radio Frequency Interferences (RFI) from short-wave radio, Citizen's Band (CB) radio and amateur "ham" radio which interfere with Hybrid Fiber Coaxial (HFC) networks and high speed DSL. Ineffective shielding of a cable network may also cause the ingress from external home electrical devices, such as cordless phones, TVs and computers.

Let's consider a strong NBI signal which resides within the same frequency band as a wideband OFDM signal. In this case, severe Signal to Noise Ratio (SNR) degradation is likely to occur across all OFDM subcarriers due to spectral leakage of the NBI signal from block processing in the OFDM receiver. In Fig. 1, the magnitude-squared of the received signal samples $|X[k]|^2$ is plotted. For flat-fading channels it is straightforward to ascertain the fact that the highest peak corresponds to the subcarrier affected by NBI, as shown in Fig. 1.(a). Fig.1.(b) shows that in frequency-selective channels the OFDM signal presents a large dynamic range, and some signal peaks can have values close to the peak induced by NBI. This observation indicates that the detection of NBI becomes difficult in frequency-selective channels, especially if the Signal to Interference Ratio (SIR) is high (Giorgetti et al., 2005).

The presence of strong NBI causes nonlinear distortion in Automatic Gain Control and Analog to Digital Converter functional blocks as well as spectral leakage in the Discrete Fourier Transform (DFT) process. Many subcarriers close to the interference frequency will suffer serious Signal to Noise Ratio (SNR) degradation. Therefore, NBI suppression is of primary importance.

The issue of NBI suppression for OFDM systems has been studied extensively in recent years, and a number of general approaches are proposed. Various *Frequency Excision methods*, where the affected frequency bins of the OFDM symbol are excised or their usage

avoided, have received specific attention. Often degradation in an OFDM based receiver is beyond the reach of the frequency excision method when the SIR is less than 0dB. In such cases other approaches, related to the *Cancellation techniques* that aim the elimination or mitigation of the effect of the NBI on the received OFDM signal, are recommended. *Linear and Nonlinear filtering methods* for NBI cancellation are also proposed.

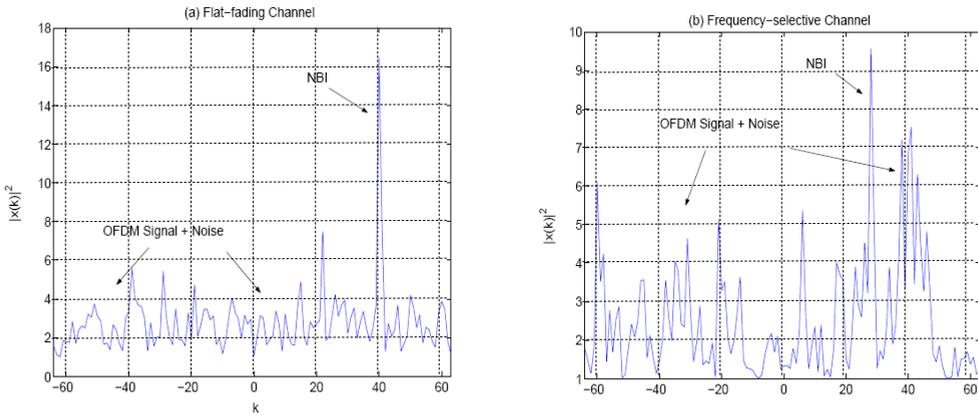


Fig. 1. The magnitude-squared of FFT bins: $|X[k]|^2$

Different specific approaches for NBI suppression are deployed in MIMO systems depending on the type of channel. For wireless channels one major group of methods is *Block Coding (BC): Space Time and Space Frequency*. It utilizes the properties of MIMO systems over fading channels. Other methods such as *adaptive beam-forming* of the MIMO antenna system and *Forward Precoding* at the transmission side are reviewed. In wire-line subscriber systems methods such as *Dynamic Spectrum Management (Level 3)*, *Optimal Precoding* and *Multi-channel Adaptive Filtering* are applied.

In this chapter the major NBI suppression methods their performance, computational complexity and application to different types of MIMO communication systems are considered. Results of simulation experiments for wireless MIMO systems and for MIMO DSL channels are analyzed. It could be seen that the methods have different computational complexity and performance depending on the parameters of the MIMO system and the communication channels.

2. Overview of NBI suppression methods

2.1 Frequency excision

This approach uses the Fast Fourier Transform (FFT) based frequency-domain excision to remove the NBI. The DFT output of block of N_{FFT} samples, $r_{m,n}$ is given by:

$$r_{m,n} = \sum_{k=1}^{N_{FFT}} r_{m,k} e^{-j2\pi kn/N_{FFT}}, \quad k=1, \dots, N_{FFT} \tag{1}$$

where m is the number of the OFDM symbol, n is the number of the subcarrier of the OFDM symbol, $r_{m,k}$ is the digital complex baseband signal sample at the demodulator input for m .

In the frequency domain, the NBI manifests itself as a peak in the spectra. Interferences can be excised by comparing and limiting the magnitude of each frequency bin to a threshold. The following method is used to determine the threshold. The mean value of the amplitude of the frequency bins and its variance are computed (Jyh-Ching et al., 2004):

$$T_{\text{mean}} = \sum_{n=1}^{N_{\text{FFT}}} \frac{10 \log_{10} |r_{m,n}|}{N_{\text{FFT}}} \quad (2)$$

$$T_{\text{var}} = \frac{1}{N_{\text{FFT}}} \left[\sum_{n=1}^{N_{\text{FFT}}} \left(10 \log_{10} |r_{m,n}| \right)^2 - \frac{1}{N_{\text{FFT}}} \left(\sum_{n=1}^{N_{\text{FFT}}} \left(10 \log_{10} |r_{m,n}| \right) \right)^2 \right] \quad (3)$$

The threshold is determined according to:

$$T_{\text{excision}} = T_{\text{mean}} - \alpha T_{\text{var}}^{1/2} \quad (4)$$

The scale factor α in the above equation is adjusted to maintain the threshold at some value of the noise floor. Each frequency bin is compared to the threshold and, if it exceeds the threshold, its value is held at the threshold. After the application of Inverse Fast Fourier Transform (IFFT), the signal is much less contaminated with narrow band interferences.

This method is characterized with relative high efficiency due to the fact that the FFT/IFFT digital signal processing could be realized in real time. In addition, it is possible to excise multiple NBIs without any initial limiting conditions. Drawbacks of this method are the impossibility to fully suppress the interference signals because of the NBI interference with the information subcarriers thus violating their orthogonality and the strong dependence of the threshold on the type and conditions of the channel.

2.2 Frequency identification and cancellation

The discrete complex baseband signal for sample k at the input of an OFDM receiver can be expressed as (Baccarelli et al., 2002):

$$r(k) = s_t(k) * h(k) + n(k) + i_n(k), \quad (5)$$

where $s_t(k)$ is the complex output signal for sample k of the transmitter, $h(k)$ is the complex impulse response for sample k of the channel, $n(k)$ is the complex Additive White Gaussian Noise (AWGN) for sample k and $i_n(k)$ is n -th complex single tone NBI for sample k . Initially the frequency position of the interference tone has to be estimated in order to approach the problem of NBI identification. After sampling the received signal $r(t)$ to obtain $r(k)$, FFT must be applied to this sequence via a Goertzel algorithm or using a butterfly lattice. It is important to note that appropriate setting of the sampling time T is a fundamental step; therefore, to increase the frequency resolution, an eight times oversampling in the frequency domain is proposed.

Assuming that the power spectrum properties of all signals constituting $r(k)$ are known, the narrow band interfering signal can be modeled as a complex sinusoidal tone:

$$i_n(k) = \alpha_n e^{j(\hat{\omega}_n k / T + \varphi_n)} = \alpha_n \cos(\hat{\omega}_n k / T + \varphi_n) + j \alpha_n \sin(\hat{\omega}_n k / T + \varphi_n). \quad (6)$$

$$i_n(k) = a_n \cos(\hat{\omega}_n k / T) + j b_n \sin(\hat{\omega}_n k / T). \quad (7)$$

Thus, it is clear that frequency domain processing is an appealing approach to estimate frequency, because the spectral properties of $r(k)$ are known.

This method is implemented in several steps. First the complex NBI frequency is estimated by finding the maximum amplitude in the oversampled signal spectrum:

$$\hat{\omega}_n = \arg \omega \in L_\omega \max(P_R(\omega)). \quad (8)$$

Then amplitude and phase estimation is done. A matrix form can be used to represent the sampled interference (Baccarelli et al., 2002):

$$\mathbf{i}_n = \mathbf{M} \mathbf{x}. \quad (9)$$

The matrix \mathbf{M} is defined as:

$$\mathbf{M} = \begin{bmatrix} \cos(\hat{\omega}_n k_1 / T) & j \sin(\hat{\omega}_n k_1 / T) \\ \cos(\hat{\omega}_n k_2 / T) & j \sin(\hat{\omega}_n k_2 / T) \\ \dots\dots & \dots\dots \\ \cos(\hat{\omega}_n k_N / T) & j \sin(\hat{\omega}_n k_N / T) \end{bmatrix}. \quad (10)$$

The vector \mathbf{x} gathers the coefficients a_n and b_n :

$$\mathbf{x} = \begin{bmatrix} a_n \\ b_n \end{bmatrix}. \quad (11)$$

And i_n is a column vector of the n -th complex NBI where N is the FFT length.

$$\mathbf{i}_n = [i(k_1) \quad i(k_2) \quad \dots \quad i(k_N)]^T. \quad (12)$$

Applying the Maximum Likelihood (ML) algorithm, the solution is given by (Iltis & Milstein, 1985):

$$\hat{\mathbf{x}} = (\mathbf{M}^T \mathbf{M})^{-1} \mathbf{M}^T \mathbf{r}. \quad (13)$$

Here \mathbf{r} is the input signal vector and $\hat{\mathbf{x}}$ is the estimation of the complex amplitude of the n -th complex NBI. The next step is to estimate the exact values of the amplitude, frequency and phase of each of the harmonic interference signals. The algorithm uses the estimation results from the first step as initial conditions of a Normalized Least Squares (NLS) optimization procedure (Baccarelli et al., 2002). The cancellation of the NBI is the last step. The identified frequency, amplitude and phase of the interference in the received signal are used for the synthesis of complex harmonic signals, which are subtracted from the received signal:

$$\bar{r}(k) = r(k) - \sum_{n=1}^M \alpha_n e^{j(\omega_n k / T + \varphi_n)}, \quad (14)$$

where $\bar{r}(k)$ is the input signal for the OFDM demodulator after the NBI cancellation.

2.3 Complex adaptive narrowband filtering

A NBI occupies a much narrower frequency band with higher power spectral density compared with a wideband signal. It could be assumed that usually a wideband signal has autocorrelation properties quite similar to that of AWGN. Therefore, filtering in the frequency domain could be realized. In OFDM systems such linear filtering is performed at the input of the demodulator. An example of such application is using an adaptive complex variable filter section with independent tuning of the central frequency and the bandwidth (Iliev et al., 2004). The transform function of such a filter section is defined as:

$$H_{RR}(z)=H_{II}(z)=\hat{\beta}\frac{1+2\hat{\beta}\cos\theta z^{-1}+(2\hat{\beta}-1)z^{-2}}{1+2(2\hat{\beta}-1)\cos\theta z^{-1}+(2\hat{\beta}-1)^2z^{-2}}, \tag{15}$$

$$H_{RI}(z)=-H_{IR}(z)=\hat{\beta}\frac{2(1-\hat{\beta})\sin\theta z^{-1}}{1+2(2\hat{\beta}-1)\cos\theta z^{-1}+(2\hat{\beta}-1)^2z^{-2}},$$

$$\hat{\beta}=\beta+2\beta\gamma(\beta-1) \tag{16}$$

where the coefficients β and γ define the filter bandwidth and parameter θ controls the central pass-band frequency ω_0 .

The proposed implementation has two very important advantages: first, an extremely low passband sensitivity increases the resistance to quantization effects; second, the central frequency and filter bandwidth can be independently controlled over a wide frequency range. Fig. 2 shows the adaptive complex notch/bandpass narrowband system based on a variable complex filter section. The band-pass variable complex filter section is tuned at the NBI frequency, thus the signal $y(n)$ represents the output of the filter which is in fact the NBI signal. Further, the NBI signal $y(n)$ is subtracted by the input complex signal $x(n)$ which is the additive sum of OFDM signal, NBI signal and AWGN. If perfect filtering is assumed, the result signal $e(n)$ is supposed to be NBI-free OFDM signal. Here $e_R(n)=x_R(n)-y_R(n)$ and $e_I(n)=x_I(n)-y_I(n)$ are the real and imaginary output of the band-stop (BS) filter. The cost function minimizes the power of the BS filter output signal $[e(n)e^*(n)]$, where $e(n)=e_R(n)+je_I(n)$.

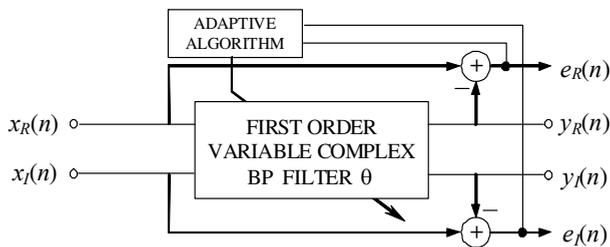


Fig. 2. Block-diagram of a BP/BS adaptive complex filter section

The central frequency ω_0 of the filter pass-band is precisely tuned by iterative update of the filter coefficients applying an LMS algorithm:

$$\theta(n+1)=\theta(n)+\mu\text{Re}[e(n)y^*(n)]. \tag{17}$$

Here μ is the step size controlling the speed of convergence, $(*)$ denotes complex-conjugate, $y'(n)$ is the derivative of $y(n) = y_R(n) + jy_I(n)$ with respect to the coefficient subject of adaptation.

2.4 Nonlinear filtering

Nowadays communication systems work in a saturated and noisy electromagnetic spectrum. Many of the interference signals could be approximated as independent stationary random processes with Gaussian distribution, but quite a lot of the radio-frequency interferences do not fit into this category. A big variety of impulse noises, to which OFDM systems are quite sensitive, could not be considered as Gaussian and/or stationary random processes. The system model has to take that into account to realize an effective NBI suppression. Under the above conditions nonlinear filtering methods, such as the two considered below, offer an improvement in NBI suppression.

a. Nonlinear ACM filter for autoregressive interference

Lets consider the received sampled signal from equation (8). In complex form the narrowband interference $\{i_k\}$ is modeled as an autoregressive Gaussian process of order p , i.e., assuming a model of the form (Hsu & Giordano, 1978), (Iltis & Milstein, 1985):

$$i_k = \sum_{i=0}^p \phi_i i_{k-i} + e_k, \tag{18}$$

where $\{e_k\}$ is a white Gaussian process, and where the autoregressive parameters $\Phi_1, \Phi_2, \dots, \Phi_p$ are known to the receiver. Under this model, the received signal has a state space representation as follows:

$$x_k = \Phi x_{k-1} + w_k, \tag{19}$$

$$z_k = Hx_k + s_k + n_k, \tag{20}$$

$$x_k = [i_k \ i_{k-1} \ \dots \ i_{k-p+1}]^T, \ H_k = [1 \ 0 \ \dots \ 0]^T, \ w_k = [e_k \ 0 \ \dots \ 0]^T, \tag{21}$$

$$\Phi = \begin{bmatrix} \phi_1 & \phi_2 & \dots & \phi_{p-1} & \phi_p \\ 1 & 0 & \dots & 0 & 0 \\ \dots & \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & 1 & 0 \end{bmatrix}. \tag{22}$$

The first component of the state vector x_k is the interference i_k . Hence, by estimating the state, an estimate of the interference which can be subtracted from the received signal to reject the interference, can be obtained.

In (Masreliez, 1975) an Approximate Conditional Mean (ACM) filter for estimating the state of a linear system with Gaussian noise and non-Gaussian measurement noise is developed. The nature of the nonlinearity is determined by the probability density of the observed noise. Under this assumption, the filtered estimate and its conditional covariance P_k and \hat{x}_k are obtained recursively through the equations for state (23,24) and time (25) estimation:

$$P_k = M_k - M_k H^T G_k(z_k) H M_k, \tag{23}$$

$$\hat{x}_k = \bar{x}_k + M_k H^T g_k(z_k), \tag{24}$$

$$M_{k+1} = \Phi P_k \Phi^T + Q_k; \quad \bar{x}_{k+1} = \Phi \hat{x}_k. \tag{25}$$

Here G_k and g_k are the nonlinear components due to the non-Gaussian noise, ε_k is the error signal and σ its variance defined by the following equations (Laster & Reed, 1997):

$$Q_k = E\{\mathbf{w}_k \mathbf{w}_k^T\}, \tag{26}$$

$$g_k(z_k) = \frac{1}{\sigma^2} \left[\varepsilon_k - \tanh\left(\frac{\varepsilon_k}{\sigma^2}\right) \right], \tag{27}$$

$$G_k(z_k) = \frac{1}{\sigma^2} \left[1 - \frac{1}{\sigma^2} \operatorname{sech}^2\left(\frac{\varepsilon_k}{\sigma^2}\right) \right], \tag{28}$$

$$\varepsilon_k = x_k - \mathbf{H} \bar{\mathbf{x}}_k, \tag{29}$$

$$\sigma^2 = \sigma_n^2 + \mathbf{H} \mathbf{M}_k \mathbf{H}^T, \tag{30}$$

The ACM filter here is seen to have a structure similar to that of Kalman - Bucy filter, as the time-update equations (23), (24) are identical. Without the nonlinear functions *tanh* and *sech* the recursive algorithm of Masreliez is reduced to the linear Kalman - Bucy algorithm (Sampei 1997). From equations (24), (27) and (29) follows, that with the ACM filter the decision feedback is realized via the function *tanh*, by correcting the measured value in the interval [-1, 1]. The behavior of the filter depends on the variance of the error signal. When the system is in a steady state, the variance is small and the nonlinear element in the feedback determines the behavior of the filter. When the variance is high, the feedback is in a linear working state and the behavior is similar to that of a linear Kalman-Bucy filter.

b. Adaptive nonlinear filter based on LMS algorithm

It has been shown in (Sampei 1997) that better interference rejection can be obtained by using one or two-sided interpolation filter. For such a filter the following Widrow Least Mean Squared (LMS) algorithm equations hold (Iltis & Milstein, 1985) (Johnson 1984):

$$X_k = [z_{k+N}, z_{k+N-1}, \dots, z_{k+1}, z_{k-1}, \dots, z_{k-N}]^T, \tag{31}$$

$$\theta_k = [a_{-N}(k), a_{-N+1}(k), \dots, a_{-1}(k), a_1(k), \dots, a_N(k)]^T, \tag{32}$$

where $2N + 1$ is the length of the data window. In order to ensure independence of the parameter μ (for control of the stability and convergence of the algorithm) from the input signal level the equations are normalized as follows (Johnson 1984):

$$\theta_k = \theta_{k-1} + \frac{\mu_0}{r_k} \xi_k X_k, \tag{33}$$

Where r_k is the estimate of the power of the input signal determined as

$$r_k = r_{k-1} + \mu_0 \left[|X_k|^2 - r_{k-1} \right]. \tag{34}$$

The output signal of the filter ε_k , which is the error signal is defined as:

$$\varepsilon_k = z_k - \hat{z}_k, \tag{35}$$

where \hat{z}_k is the predicted value of the NBI on the basis of L samples from the input signal z_k . By transforming the prediction error a nonlinear transversal filter for the prediction of z_k is obtained. The differential equation of the filter is in the form (Johnson 1984):

$$\hat{z}_k = \sum_{i=0}^L a_i(k-1) \left[\hat{z}_{k-i} + \rho_{k-1}(\xi_{k-1}) \right], \tag{36}$$

$$\rho_k(\xi_k) = \xi_k - \tanh \left(\frac{\xi_k}{\sigma_k} \right). \tag{37}$$

Here ρ_k is a nonlinear function as the one used in equation (30) and σ_k variance of a Gaussian random variable.

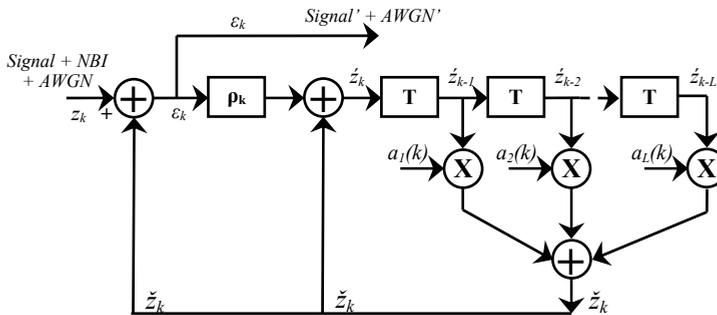


Fig. 3. One-sided Adaptive Nonlinear Filter Based on LMS Algorithm.

A block scheme of an one-sided nonlinear adaptive filter, based on LMS algorithm is shown on Fig.3. For the realization of the filter from equation (36) an estimation of σ_k and the tap weight coefficients $a_i(k)$, has to be obtained using LMS algorithm (Carlemalm et al., 2004).

3. NBI suppression in wireless MIMO OFDM systems

Following some of the specific methods for NBI suppression in MIMO communication systems are discussed, such as adaptive beamforming of the antenna system, forward precoding at the transmission side and Orthogonal Space-Time Block Coding.

3.1 Adaptive beamforming of the MIMO antenna system

One of the fastest developing methods for noise suppression in modern MIMO communication systems is employing adaptive antenna arrays in the transmit and receive

side of the radio-communication system. A block scheme of an MIMO OFDM system with adaptive beamforming is shown in Fig.4, where R is the number of transmit antennas, M – number of receive antennas, N – number of subcarriers in the OFDM symbol, $s_k(t)$ $0 \leq k < N$ is the k transmitted normalized information symbol from block 't' (Iserte et al., 2001).

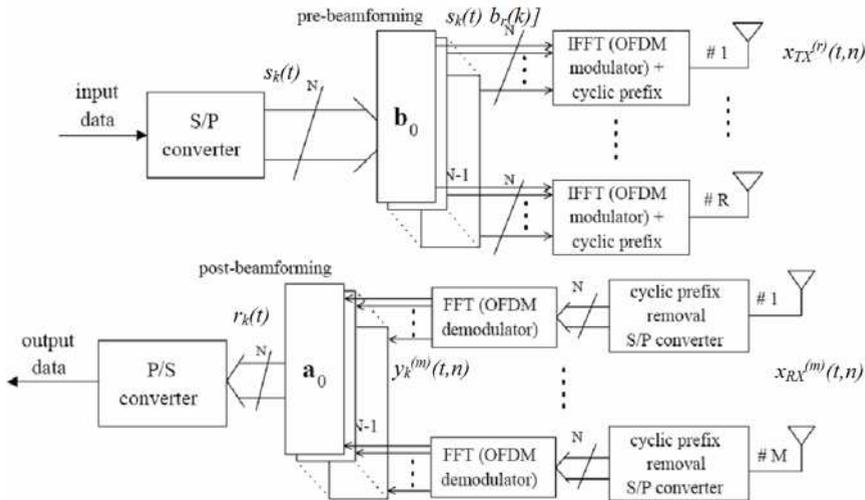


Fig. 4. Block diagram of MIMO OFDM communication system with adaptive beamforming. The control of the antenna array in the transmit side is done via a number of vectors $\mathbf{b}_k = [b_1(k) b_2(k) \dots b_R(k)]^T$, with which the corresponding information symbols are multiplied before the process of OFDM modulation. In the receive side after OFDM demodulation the FFT demodulated information symbols $y_k^{(m)}(t)$ for each subcarrier k , are multiplied with a number of vectors for control of the antenna array $\mathbf{a}_k = [a_1(k) a_2(k) \dots a_M(k)]^T$ $3a \geq N_t$ (Thung et al., 2001):

$$\mathbf{r}_k(t) = \mathbf{a}_k^H \mathbf{y}_k(t) = \mathbf{a}_k^H \mathbf{H}(k) \mathbf{b}_k s_k(t) + \mathbf{a}_k^H \mathbf{n}_k(t), \tag{38}$$

where $\mathbf{H}(k)$ is the matrix of the frequency response of the MIMO radio-channel, $\mathbf{n}_k(t)$ is the vector sum of NBI and AWGN, $r_k(t)$ is the signal at the output of the control block of the antenna array of the receiver for the k -th carrier frequency. It is assumed that all the MIMO channel state information (CSI) is available at the transmitter, including the statistical characteristics of the narrowband and wideband noises. The maximum of the signal-to-noise plus NBI is obtained when the receiver has characteristics equal to a matched filter in relation to the communication channel (Wong et al., 2001), (Iserte et al., 2001):

$$SNIR_k|_{MAX} \Leftrightarrow \mathbf{a}_k = \alpha_k \mathbf{R}_n^{-1}(k) \mathbf{H}(k) \mathbf{b}_k, \tag{39}$$

where $\mathbf{R}_n(k) = E\{\mathbf{n}_k(t) \mathbf{n}_k^H(t)\}$ is the covariance addition matrix of the NBI and AWGN.

In the real systems there are limits for the total emitted power from all of the antennas. For MIMO OFDM systems with adaptive beamforming of the transmission antenna system the emitted power from all of the antennas for the k -th subcarrier is proportional to $\| \mathbf{b}_k \|^2$. The goal of the optimization procedure is to find an optimal vector with emitted power weight coefficients - b_k for each antenna:

$$J(k)|_{MIN} = SNIR_k - \lambda(k) \left(\| \mathbf{b}_k \|^2 - |\beta(k)|^2 \right), \tag{40}$$

where $\lambda(k)$ are the eigenvalues, $|\beta(k)|^2$ is limit of the emitted power from all antennas.

3.2 NBI suppression with low-complexity precoding at the transmit side

Methods based on forward precoding of the signal at the transmission side assume that the wireless channel characteristics (narrowband and wideband noises included) are known in advance at the transmission side. One recently proposed method of low computational complexity is precoding at the transmit side with maximizing the diversity of the received signals, Fig.5 (Rico et al., 2007).

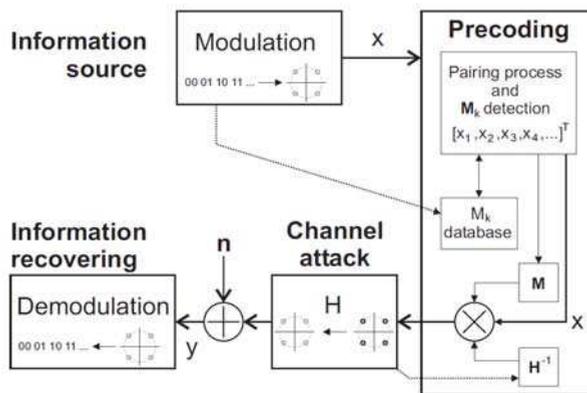


Fig. 5. Block diagram of MIMO OFDM communication system with forward precoding

This approach uses the information about the type of the transmitted symbols as criteria for the selection of optimal precoding matrix. The signal at the input of the receiver side is given as:

$$\mathbf{y} = \mathbf{H} \mathbf{T} \mathbf{x} + \mathbf{n} \tag{41}$$

where \mathbf{y} is the vector $[n_r \times 1]$ of the received signal, \mathbf{x} - vector $[n_t \times 1]$ of the transmitted signal, \mathbf{H} - matrix $[n_r \times n_t]$ of the communications channel, \mathbf{T} - precoding matrix $[n_t \times n_t]$, \mathbf{n} - vector $[n_r \times 1]$ of the complex additive noise signal at the input of the receiver. The precoding matrix of the maximum diversity \mathbf{T} is used for maximizing the energy of the received signal and to suppress the interference signals. According (Rico et al., 2007), \mathbf{T} is defined as:

$$\mathbf{T} = \frac{1}{|\mathbf{H}|} \begin{bmatrix} \sum_{i=1}^j H_{i,1} \mathbf{M}_{i,1} & \sum_{i=1}^j H_{i,1} \mathbf{M}_{i,2} & \cdots & \cdots & \sum_{i=1}^j H_{i,1} \mathbf{M}_{i,j} \\ \sum_{i=1}^j H_{i,2} \mathbf{M}_{i,1} & \sum_{i=1}^j H_{i,2} \mathbf{M}_{i,2} & \cdots & \cdots & \sum_{i=1}^j H_{i,2} \mathbf{M}_{i,j} \\ \vdots & \vdots & \ddots & & \vdots \\ \vdots & \vdots & & \ddots & \vdots \\ \sum_{i=1}^j H_{i,j} \mathbf{M}_{i,1} & \sum_{i=1}^j H_{i,j} \mathbf{M}_{i,2} & \cdots & \cdots & \sum_{i=1}^j H_{i,j} \mathbf{M}_{i,j} \end{bmatrix}, \tag{42}$$

where M_{ij} is a sub-precoding matrix of identical dimensions to \mathbf{T} , the function of which is maximizing the energy of the received signal by using apriority information of the transmitted symbols.

3.3 Space block coding

This type of block coding is used for improving the communications quality, including better interference suppression. Transmitted information is coded and transmitted via several antennas simultaneously to obtain maximum space diversity of the emitted signal. The main idea of this approach is that if the error probability of receiving a message by transmission over a wireless channel is p , with the simultaneous transmission of n orthogonal copies of the message over n independent wireless channels, the total error probability is p^n . Hence, the use of space block codes leads to relatively lower error probability or, under identical other conditions, to an increase of the channel throughput.

a. Orthogonal Space-Time Block Coding (OSTBC)

Alamouti (Alamouti, 1998) proposes an OSTBC transmit matrix for complex signals by using two transmit antennas $N_T=2$. The block diagram of an OSTBC precoder is shown on Fig.6. The proposed matrix is the only one which ensures maximum diversity equal to 2 in the transmit side with code rate $R=1$:

$$\mathbf{G}_2 = \begin{bmatrix} S_1 & -S_2^* \\ S_2 & S_1^* \end{bmatrix}, \tag{43}$$

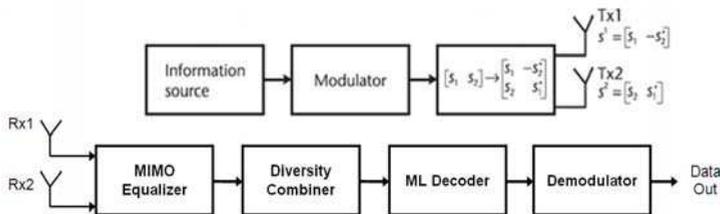


Fig. 6. Block diagram of an OSTBC MIMO OFDM system.

At the receiver side the decoding is performed using the method proposed by Tarokh (Tarokh, 1999), applying the maximum likelihood (ML) criteria. For $N_T=2$, $R=1$ and coding matrix G_2 , the decoded signal is described by the following equations:

$$\hat{S}_1 = \arg \min \left[\left| \sum_{j=1}^m (r_1^j h_{1,j} s_1^* + (r_2^j)^* h_{2,j}) \right|^2 - s_1 \right] + \left(-1 + 2 \sum_{j=1}^m \sum_{i=1}^2 |h_{i,j}|^2 \right) |s_1|^2, \quad (44)$$

$$\hat{S}_2 = \arg \min \left[\left| \sum_{j=1}^m (r_1^j h_{2,j} s_2^* - (r_2^j)^* h_{1,j}) \right|^2 - s_2 \right] + \left(-1 + 2 \sum_{j=1}^m \sum_{i=1}^2 |h_{i,j}|^2 \right) |s_2|^2, \quad (45)$$

where \hat{S}_k for $k = 1, 2$, is the estimation of the decoded signal for the k -th OFDM symbol at the input of the demodulator, h_{ij} - transmitting coefficient of the channel from the i -th TX antenna to j -th RX antenna, r_j - received signal from the j -th RX antenna for the time interval of the OFDM symbol $P = 1, 2$.

b. Space Frequency Block Code (SFBC)

There are many algorithms for the synthesis of Space-Frequency Block Codes. The algorithm described below is characterized with maximum of the diversity coefficient and maximal code rate $R = 1$ (Shao et al., 2003). Let's consider the radio-communications system shown on Fig.7, with M transmit and N receive antennas and number of subcarriers N_c , $N_c \gg M, N$. The synthesis of the space-frequency coding matrix C passes through several stages. At the first stage, the vector of the input symbols s with dimension $[N_c \times 1]$ is divided into groups of G vectors $\{s_g\}$ with dimension $[ML \times 1]$. At the second stage, each vector s_g is multiplied from the left with a coding rotational (CR) matrix Θ (Xin et al., 2001) with dimension $[ML \times ML]$. As a result of the multiplication a vector v_g with dimension $[ML \times 1]$ is obtained. At the third stage each vector v_g is divided to L sub-vectors with dimension $[M \times 1]$, after which each sub-vector is used for the synthesis of a diagonal sub-matrix $D_{S_g,k}$. At the last stage, all GL sub-matrices from all G groups are interleaved, so that the space-frequency coding matrix C show on Fig.8 is obtained (Shao et al., 2003).

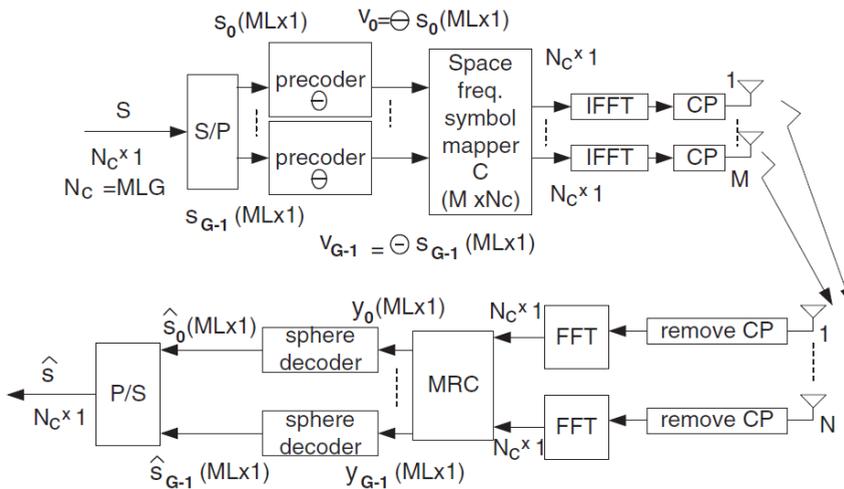


Fig. 7. Block diagram of a MIMO SFBC-OFDM system.

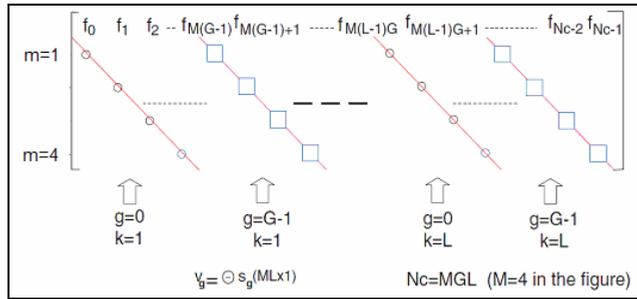


Fig. 8. Structure of the SFBC matrix C.

At the receive side the signal from each of the receive antennas is equalized, synchronized and transformed to baseband. After removing the guard interval, the OFDM symbols are demodulated via FFT and are fed into the space-frequency baseband decoder (SFBCD). After combining the information symbols from group g for all N receive antennas the result at the output of the combination scheme (MRC) is:

$$\mathbf{y}_g = \Sigma_g^{-1/2} \Theta \mathbf{s}_g + \boldsymbol{\eta}_g . \tag{46}$$

The decoding of the information symbols is performed by the method described in [459], by applying the maximum likelihood criteria:

$$\hat{\mathbf{s}}_g = \arg \min \left\| \mathbf{y}_g - \mathbf{H} \mathbf{s}_g \right\|^2 , \tag{47}$$

where \mathbf{s}_g is the transmitted information signal and \mathbf{y}_g the decoded received signal at the output of the combination scheme (Shao et al, 2003).

4. RFI suppression in MIMO DSL DMT communication systems

Some of the specific methods for RFI suppression in digital subscriber lines such as optimal dynamic spectrum management of the signal (DSM Level 3), optimal precoding and multichannel block adaptive filtering will be considered below.

4.1 Optimal dynamic signal spectrum management (DSM Level 3)

Dynamic spectrum management is a new promising alternative, based on optimal dynamic management of the spectrum of each transmitter depending on the parameters of the specific wire-line (copper cable) channel. Major practical problem of the proposed algorithms for DSM is the extremely high computational complexity exponentially proportional to the number of tones in the discrete multi-tone (DMT) symbols.

If we consider a MIMO DSL DMT communication system with independent transmission channels, for each tone of the DMT symbol the following equation is valid:

$$\mathbf{y}_k = \mathbf{H}_k \mathbf{x}_k + \mathbf{n}_k , \tag{48}$$

where \mathbf{y}_k is the vector of the received signals for tone k ; \mathbf{x}_k is the vector of the transmitted signals for tone k ; \mathbf{n}_k is the additive sum vector of the background AWGN, crosstalk noise

between the twisted pairs and RFI for tone k ; \mathbf{H}_k is the $[N \times N]$ dimensional channel matrix, the diagonal elements of which are the transmission functions of the direct channels and the rest are the transmission functions of the crosstalk; N is the number of twisted pairs in the cable. The total transmission speed for subscriber n from the MIMO channel is:

$$R_n = \sum_{k=1}^K b_k^n \quad [\text{bits}] \quad (49)$$

where b_k^n is the number of transmitted bits in the QAM symbol for subscriber n and tone k . For a channel with two subscribers with limiting conditions for the maximal emitted power and in conformity with the PSD mask for each of the DSL transmitters, the spectrum optimization problem is the following (Cendrillon et al., 2003):

$$\max_{s_1, s_2} R_2 \quad \text{for} \quad R_1 \geq R_1^{\text{arget}}, \quad (50)$$

$$\sum_{k=1}^K s_k^n \leq P_n, \quad n = 1, 2. \quad (51)$$

The direct approach to solving the optimization problem (50-51) leads to an exponential increase of the computational complexity. The computational complexity could be reduced significantly by using a Lagrange unconditional optimization instead of the conditional optimization from (50-51):

$$L = \sum_{k=1}^K L_k + \lambda_1 P_1 + \lambda_2 P_2, \quad (52)$$

$$L_k = w b_k^1 + (1-w) b_k^2 - \lambda_1 s_k^1 (b_k^1, b_k^2) - \lambda_2 s_k^2 (b_k^1, b_k^2), \quad (53)$$

$$\max_{s_1, s_2} L(w, \lambda_1, \lambda_2, s_k^1, s_k^2), \quad (54)$$

where w is the Lagrange optimization constant. The limits for the maximal emitted power are imposed indirectly through the factors λ_1 and λ_2 . The proposed method leads to the division of the global optimization problem (50-51) to K independent Lagrange optimization problems (53-54) with linear computational complexity (Cendrillon et al., 2003):

$$O(K) = K(b_{\max} + 1)^2. \quad (55)$$

4.2 Optimal precoding

Modern GDSL communication systems employ time, frequency, code and space multiplexing to achieve maximum transmission speed in a cable channel. One of the methods to achieve this goal is the design of an optimal linear precoder, that maximizes the total quantity of transmitted information under the condition of imposed limits for the Minimal Mean Square Error (MMSE).

Let us consider a complex model of a MIMO DSL channel (Perez-Cruz et al., 2008):

$$\mathbf{y} = \sqrt{snr} \mathbf{H} \mathbf{P} \mathbf{x} + \mathbf{w} , \tag{56}$$

where \mathbf{y} is a n -dimensional vector of the received discrete signals; \mathbf{x} is a m -dimensional vector of the transmitted discrete signals, which are independent random values with zero average and unit variance; \mathbf{w} is a n -dimensional additive sum vector of the received signals of the background complex AWGN and complex RFI; \mathbf{H} is the $[n \times m]$ dimensional channel matrix, the diagonal elements of which are the transmission functions of the direct channels and the rest of the elements are the transmission functions of the crosstalk; snr is a scale factor function of the total transmitted power; \mathbf{P} is a $[m \times m]$ dimensional precoding matrix. The precoding matrix \mathbf{P} is obtained as the result of a nonlinear optimization problem for maximizing the transmitted information and thus mitigating the RFI, under the following limiting conditions:

$$\max_{\mathbf{P}} I(\mathbf{x}, \mathbf{y}) , \tag{57}$$

$$Tr\{E[\mathbf{P} \mathbf{x} \mathbf{x}^H \mathbf{P}^H]\} = Tr\{\mathbf{P} \mathbf{P}^H\} \leq m . \tag{58}$$

The solution of the optimization procedure (57-58) is described through the equation:

$$\mathbf{P}^* = \lambda^{-1} \mathbf{H}^H \mathbf{H} \mathbf{P}^* \mathbf{E} . \tag{59}$$

Here the parameters λ and the matrix of the Minimal Mean Square Error (MMSE) - \mathbf{E} are determined by (Kay, 2008):

$$\lambda = \|\mathbf{H}^H \mathbf{H} \mathbf{P}^* \mathbf{E}\| / \sqrt{m} , \tag{60}$$

$$\mathbf{E} = E\left[(\mathbf{x} - E[\mathbf{x} | \mathbf{y}])(\mathbf{x} - E[\mathbf{x} | \mathbf{y}])^H\right] . \tag{61}$$

For finding \mathbf{P} , which is a global solution of the optimization problem (57-58), it is necessary to find the local solutions for the different values of the signal-to-noise ratio. Another computational problem is determining the MMSE matrix - \mathbf{E} , which is of an exponential computational complexity. When the dimension of the \mathbf{E} matrix is big, instead of direct computation for finding a representative estimation of the error matrix the *Monte Carlo* method is used. After this the precoding matrix \mathbf{P} is obtained using the iteration procedure (Perez-Cruz et al., 2008):

$$\mathbf{P}_{k+1} = \lambda^{-1} \left(\mathbf{P}_k + \mu snr \mathbf{H}^H \mathbf{H} \mathbf{P}_k \mathbf{E} \right) , \tag{62}$$

$$Tr\{\mathbf{P}_{k+1} \mathbf{P}_{k+1}^H\} = m , \tag{63}$$

where μ is a constant and λ^{-1} is chosen according the condition (60).

4.3 Multichannel adaptive filtering

The algorithms for block-based multichannel transform domain adaptive filtering solve specific problems in relation with the space-time interferences between the input signals of

the adaptive filter. Two major approaches for the suppression of the space-time interferences between the input signals are available: Frequency Domain Adaptive Filtering (FDAF) and Transform Domain Adaptive Filtering (TDAF).

a. Multichannel FDAF

This method is based on the block approach in solving the multichannel identification problem by forming each block from L consecutive samples from the error signal vector $\mathbf{e}(\mathbf{n})$. The generalized description of a MIMO system leads to the solution of a system of equations, by assigning one equation to each filter output q (Spors et al., 2009):

$$\mathbf{e}_q(n) = \mathbf{y}_q(n) - \sum_{p=1}^P \hat{\mathbf{h}}_{p,q}^T \mathbf{x}_{p,q}(n), \quad (63)$$

The resulting matrix is transformed via DFT to a diagonal matrix. The error signal block $\mathbf{e}(\mathbf{m})$ described in the time domain as a block with length L consecutive samples is:

$$\mathbf{e}(m) = [e(mL), e(mL+1), \dots, e(mL+L-1)]^T, \quad (64)$$

where m is the index of the block. The input signal of the system $\mathbf{y}(m)$ in the time domain is: described in a similar way:

$$\mathbf{y}(m) = [y(mL), y(mL+1), \dots, y(mL+L-1)]^T. \quad (65)$$

The algorithm requires DFT with dimension $2L$ which needs preliminary addition of zero samples to the error signal and the output signal of the filter. The input signals in the frequency domain are described as:

$$\mathbf{X}(m) = [\mathbf{X}_1(m), \mathbf{X}_2(m), \dots, \mathbf{X}_p(m)]. \quad (66)$$

It can be shown that the resulting normal equation for the MIMO case can be decomposed into a series of independent multiple-input single-output (MISO) normal equations for each DSL channel. Hence, the consideration of a MISO system is sufficient in the context of this work. Under the above considerations a generalized FDAF algorithm for a MISO system could be synthesized in the following four equations (Spors et al., 2009):

$$\mathbf{S}(m) = \lambda \mathbf{S}(m-1) + (1-\lambda) \mathbf{X}^H(m) \mathbf{G} \mathbf{X}(m), \quad (67)$$

$$\mathbf{K}(m) = (1-\lambda) \mathbf{S}^{-1}(m) \mathbf{X}^H(m), \quad (68)$$

$$\mathbf{e}'(m) = \mathbf{y}'(m) - \mathbf{G} \mathbf{X}(m) \hat{\mathbf{h}}'(m-1), \quad (69)$$

$$\hat{\mathbf{h}}'(m) = \hat{\mathbf{h}}'(m-1) + \mathbf{G} \mathbf{K}(m) \mathbf{e}'(m), \quad (70)$$

where $\mathbf{S}(\mathbf{m})$ is the co-variation matrix, λ the optimization constant; $\hat{\mathbf{h}}(\mathbf{m})$ the vector with the estimations of the filter coefficients; \mathbf{G} zero matrix for complementing the signal with zero samples; $\mathbf{K}(\mathbf{m})$ is the vector with Kalman amplification coefficients.

b. Block-based Multichannel TDAF

Transform-domain adaptive filtering (TDAF) is a technique that performs the filter adaptation in a transform domain. In the ideal case, the far-end signals will be decorrelated

by a suitably chosen transformation. The ideal transformation can be deduced from the covariance matrix $R_{xx}(n)$ and is data-dependent in general.

The spatio-temporal decoupling consists of two steps: (1) temporal decoupling using a discrete Fourier transform (DFT) based transformation and (2) a spatial decoupling using a unitary transform. In order to derive a block-based algorithm for multichannel TDAF both block-based FDAF and the concept of TDAF are combined in the following. The two stage approach to TDAF separates the temporal decoupling from the spatial decoupling. Hence, FDAF can be utilized for temporal decoupling combined with the concept of spatial decoupling from TDAF. For this purpose the eigenvalue decomposition of covariance matrix of TDAF is introduced into (Spors et al., 2009):

$$\underline{\mathbf{S}}(m) = \mathbf{A} \mathbf{U}(m) \mathbf{T}(m) \mathbf{U}^H(m) \mathbf{A}^T, \quad (71)$$

$$\underline{\mathbf{X}}(m) = \mathbf{X}(m) \mathbf{A} \mathbf{U}(m), \quad (72)$$

where $\mathbf{T}(m)$ is transformed covariance matrix and $\mathbf{U}(m)$ is an unitary matrix. Furthermore introducing (72) into the error signal of FDAF (69) reads:

$$\underline{\mathbf{e}}'(m) = \underline{\mathbf{y}}'(m) - \mathbf{G} \underline{\mathbf{X}}(m) \mathbf{G}_U \hat{\underline{\mathbf{h}}}(m-1). \quad (73)$$

Finally, the coefficient update is introduced by equation (74) where \mathbf{G} , \mathbf{G}_U are constant matrixes.

$$\hat{\underline{\mathbf{h}}}(m) = \mathbf{G}_U \hat{\underline{\mathbf{h}}}(m-1) + \mathbf{G} \mathbf{K}(m) \underline{\mathbf{e}}'(m). \quad (74)$$

The algorithm defined by Eq. (67-74) constitutes a combination of the concepts of FDAF and TDAF. The decoupling of the covariance matrix is performed in a two-step approach. The DFT is used for temporal decoupling and an eigenvalue decomposition for spatial decoupling. The temporal decoupling is performed in a very efficient manner by applying FDAF. The required DFTs can be realized efficiently by the fast Fourier transform (FFT). For an exact spatial decoupling, an eigenvalue decomposition has to be performed. However, the derived formulation allows also the usage of generic MIMO filtering of the far-end signals with the potential of finding efficient approximations of the exact solution. Fig. 9 illustrates a block-diagram of the algorithm exploiting these structures.

5. Comparison of NBI suppression methods

A comparison of some of the above described NBI suppression methods based on simulation experiments is given below. Methods with relatively low computational complexity were selected for practical reasons. The bit error ratio (BER) as a function of the Signal to Interference Ratio (SIR) is estimated and the simulation results for different MIMO systems are presented.

5.1 Computational complexity of NBI suppression methods

Algorithm analysis (Knuth, 1997) stands for determination of the amount of resources (i.e. time and storage) necessary to execute it. Most algorithms are designed to work with inputs of arbitrary length. Usually the efficiency or running time of an algorithm is stated as a

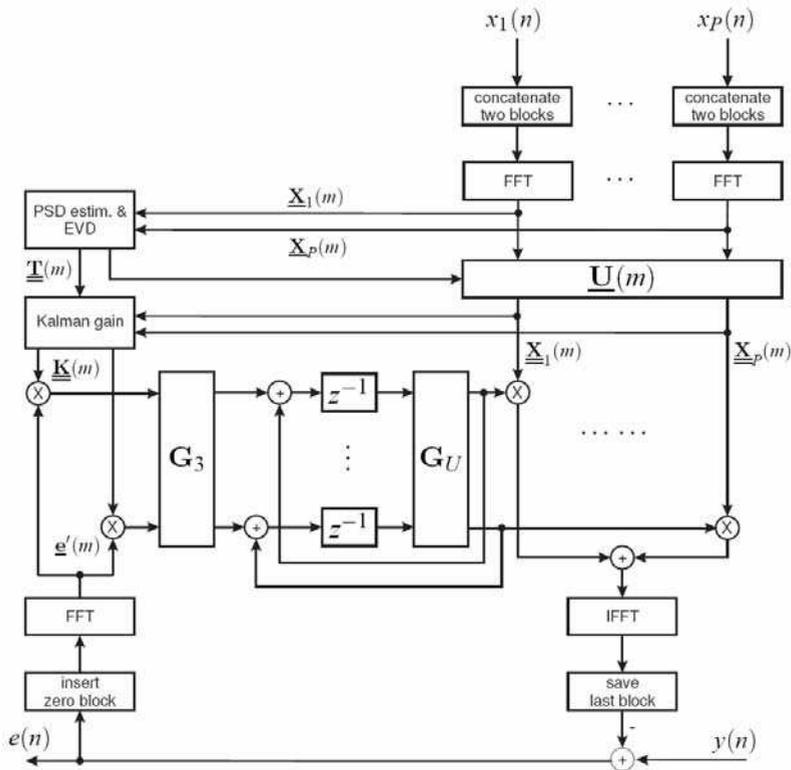


Fig. 9. Block diagram of TDAF algorithm.

function relating the input length to the number of steps (time complexity) or storage locations (space complexity). Algorithm analysis is an important part of a broader computational complexity theory, which provides theoretical estimates for the resources needed by any algorithm which solves a given computational problem. These estimates provide an insight into reasonable directions of search for efficient algorithms.

In theoretical analysis of algorithms it is common to estimate their complexity in the asymptotic sense, i.e., to estimate the complexity function for arbitrarily large input. Big O notation, omega notation and theta notation are used to this end. Usually asymptotic estimates are used because different implementations of the same algorithm may differ in efficiency. However the efficiencies of any two "reasonable" implementations of a given algorithm are related by a constant multiplicative factor called a *hidden constant*.

Time efficiency estimates depend on what we define to be a step. For the analysis to correspond usefully to the actual execution time, the time required to perform a step must be guaranteed to be upper bounded by a constant.

The computational complexity of some scalar and matrix operations is listed in Tables 1 and 2. Here $M(n)$ stands for the complexity of the chosen multiplication algorithm (Knuth,1998). Based on such estimations the computational complexity of major NBI suppression methods for wireless MIMO and MIMO GDSL systems are given in Tables 3 and 4. For the simulation experiments the methods with lowest computational complexity are chosen.

Function	Input	Algorithm	Complexity
Polynomial evaluation	One polynomial of degree n with fixed-size polynomial coefficients	Direct evaluation	$\Theta(n)$
		Horner's method	$\Theta(n)$
Polynomial GCD (over $Z[x]$ or $F[x]$)	Two polynomials of degree n with fixed-size polynomial coefficients	Euclidean algorithm	$O(n^2)$
		Fast Euclidean algorithm	$O(n (\log n)^2 \log \log n)$
DFT, IDFT, Circular Convolution	m numbers, n -digit each	Radix 2^k FFT	$O(m \log(m))$

Table 1. Complexity of some basic algebra functions.

Function	Input	Output	Algorithm	Complexity
Matrix multiplication	Two $n \times n$ -matrices	One $n \times n$ -matrix	Schoolbook matrix multiplication	$O(n^3)$
			Strassen algorithm	$O(n^{2.807})$
			Coppersmith-Winograd algorithm	$O(n^{2.376})$
Matrix multiplication	One $n \times m$ -matrix & One $m \times p$ -matrix	One $n \times p$ -matrix	Schoolbook matrix multiplication	$O(nmp)$
Matrix inversion	One $n \times n$ -matrix	One $n \times n$ -matrix	Gauss-Jordan elimination	$O(n^3)$
			Strassen algorithm	$O(n^{2.807})$
			Coppersmith-Winograd algorithm	$O(n^{2.376})$
Determinant	One $n \times n$ -matrix	One number with at most $O(n \log n)$ bits	Laplace expansion	$O(n!)$
			LU decomposition	$O(n^3)$
			Bareiss algorithm	$O(n^3)$
			Fast matrix multiplication	$O(n^{2.376})$

Table 2. Complexity of some matrix algebra functions.

NBI Suppression Methods	Number of Additions	Number of Multiplications	Computational Complexity
Frequency Excision	$6MN$	$4MN \log(N)$	$\sim O(KMN \log(N))$
Adaptive Linear Filtering	KMN	$28MN+KMN^2$	$\sim O(KMN^2)$
Identification and Compensation	$2MN^2$	$M(N+2)N^3$	$\sim O(KMN^4)$
Adaptive Antenna Beamforming	NA^*	NA^*	$\sim O(KN(MS)^3)$
Optimal Transmitter Precoding	NA^*	NA^*	$\sim O(KN(MS)!)$
OSTBC $M,S=2$ $M,S=3,4$	$N(3MS - 1)$ $N(6MS+M - 1)$	$N(3MS + 2)$ $N(7MS + 6)$	$\sim O(KMSN)$
SFBC	NA^*	NA^*	$\sim O(KNG(MS)!)$

Note: * number of additions and multiplications depends on the method used for matrix computation.

Table 3. Computational complexity of NBI suppression methods in wireless MIMO systems.

RFI Suppression Methods	Number of Additions	Number of Multiplications	Computational Complexity
Frequency Excision	$MN+K$	$KMN \log(N)$	$\sim O(K2N \log(2N))$
Adaptive Linear Filtering	KMN	$KMN+MN^2$	$\sim O(K(2N)^2)$
Identification and Compensation	$2MN^2$	$KM(N-1)N^3$	$\sim O(K(2N)^4)$
Dynamic Spectrum Management Level 3	NA^*	NA^*	$\sim O(KNM^3)$
Optimal Precoding	NA^*	NA^*	$\sim O(KNM!)$
Block-based Multichannel FDAF	NA^*	NA^*	$\sim O(KNML!)$
Block-based Multichannel TDAF	NA^*	NA^*	$\sim O(KNML^4)$

Note: * number of additions and multiplications depends on the method used for matrix computation.

Table 4. Computational complexity of RFI suppression methods in MIMO GDLS system.

5.2 Performance of NBI suppression methods for wireless systems

To evaluate the performance of NBI suppression methods in wireless systems, simulations relative to complex baseband presentation are conducted, assuming standard MIMO OFDM receiver. The information source is modeled by a generator of uniformly distributed random integers based on the modified version of Marsaglia's "Subtract with borrow algorithm" (Tezuka et al., 1993). The method can generate all the double-precision values in the closed interval $[2^{-53}, 1-2^{-53}]$. Theoretically, it can generate over 2^{1492} values before repeating itself. The channel coder is implemented as a convolutional encoder with code rate is $R_c = 1/2$ and Viterbi hard threshold convolutional decoding. A block interleaver - deinterleaver is

implemented with an algorithm that chooses a permutation table randomly, using the initial state input that is provided. The Orthogonal Space-Time Block Encoder (OSTBC) for complex signals is realized using the methods described in (Alamouti, 1998), (Berguer & Dong, 2003). The number of transmit antennas N_T and receive antennas N_R can be set from 1 to 4. For 2x2 MIMO system, the code rate is $R_c=1$ whereas for 3x3 and 4x4 MIMO systems, the code rate is $R_c=1/2$. The digital modulator block is implemented as a bank of N_T blocks each one performing 256-point IFFT. The OFDM symbol per each output channel consists of 128 data bins. Each OFDM data symbol can use different modulation formats. In the experiments Grey encoded 64-QAM modulation format is used for each transmitter. After the IFFT process, the prefix and suffix guard intervals are added. The MIMO wireless flat fading channel is realized as given in (Berguer & Dong, 2003). Channel estimation based on optimal training preamble is adopted. In the OFDM block demodulator, the guard prefix and suffix intervals are removed per each channel and 256-point FFT is applied. Finally, OSTB decoding, 64-QAM demodulation and error correction decoding are made.

The excision method is applied to the MIMO OFDM signal with a complex NBI at each input of the receiver. The signal is converted into the frequency domain by applying an FFT at each input, oversampled by 8 and the noise peaks in the spectra are limited to the determined threshold. After conversion back in the time domain the signal is fed into the corresponding OFDM demodulator. For more precise frequency excision, FFT of higher order than the one in the demodulator is applied.

For the realization of the filtering method a complex Adaptive Notch Filter Bank (ANFB) is connected at the receiver's input. The filtering process is applied independently at each receiver input. The adaptation algorithm tunes the filters at each receiver input, in such a way that the central frequency and bandwidth match to the NBI signal spectrum. In the simulations, the central frequency of the notch filters is chosen to be equal to the NBI central frequency, while their bandwidth is equal to 20% of the bandwidth between two adjacent OFDM sub-carriers.

The frequency cancellation method is implemented in several stages as discussed in section 2.2. First, the complex NBI frequency is estimated by finding the maximum in the oversampled signal spectrum per channel. Using ML approach, per each input, the NBI amplitude and phase are estimated. Then a NLS optimization algorithm is realized, where precise estimation of the NBI's complex amplitude, phase and frequency are done.

Using the above general simulation model of an OSTBC MIMO system, different experiments are performed, estimating the bit error ratio (BER) as a function of the Signal to Interference Ratio (SIR). The NBI is modeled as a single complex tone, the frequency of which is located in the middle between two adjacent OFDM sub-carriers. The MIMO channels are subject to flat fading and background AWGN. The Signal to AWGN ratio at the input of the OFDM receiver is 15dB. For comparison in Fig.10 the results for simulation of a conventional Single Input Single Output (SISO) system employing different NBI suppression methods are presented: frequency excision, frequency cancellation and adaptive filtering. The experiments show that for high NBI, where the SIR is less than 0 dB, all three suppression methods lead to a significant improvement in performance. It is evident that the frequency cancellation method gives best performance, while filtering is better than the excision method.

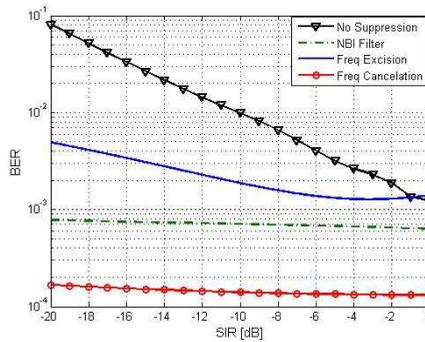


Fig. 10. BER as a function of SIR for SISO channel

In the case of 2x2 and 4x4 MIMO channels the results are presented in Fig.11 a,b. It could be seen that filtering with ANFB gives better performance for higher values of the antenna diversity in the OSTBC MIMO system. The frequency excision method manifests good performance for high SIR. It should be noted that the adaptive filtering and frequency cancellation schemes lead to a slight degradation of the overall performance when SIR>0, which is due to either an amplitude and phase distortion of the adaptive notch filters or to a wrong estimation of the NBI parameters during the identification process. The degradation could be reduced using higher-order notch filters or implementing more sophisticated identification algorithms. The degradation effect could be avoided by simply switching off the filtering when SIR~0. Such a scheme is easily realizable, as the amplitude of the NBI can be monitored at the bandpass output of the filters (Fig. 2).

The results have outlined the fact that the Frequency Identification and Cancellation method achieves the highest performance. However, the extremely high computational complexity limits its applications to the hardware resources. In this aspect, the Adaptive Notch Filter Bank offers a trade off between good performance and reasonable computational complexity. The frequency excision method shows relatively good results and his main advantage is its computational efficiency.

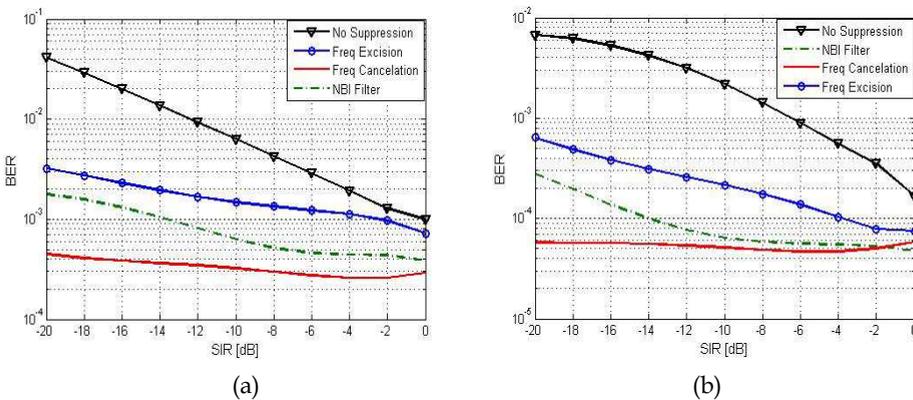
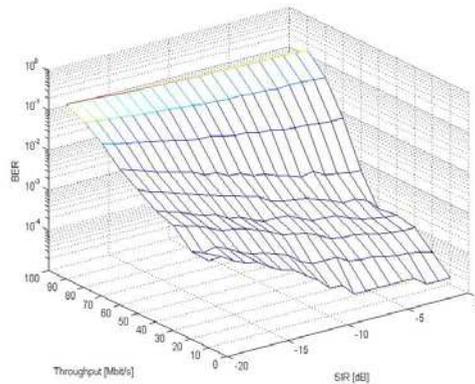
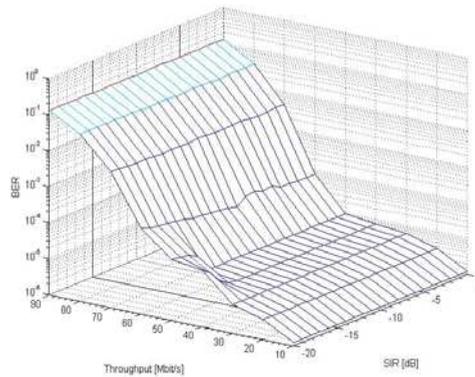


Fig. 11. BER as a function of SIR for 2x2 and 4x4 MIMO channels



(a)



(b)

Fig. 12. BER, Throughput and SIR for 4x4 MIMO OSTBC single user communication system.

The relation between BER, Throughput and SIR for 4x4 MIMO OSTBC OFDM single user communication system in flat fading environment and constant AWGN level for SNR=20dB is presented on Fig.12 where (a) is without NBI excision and (b) with NBI excision.

5.3 RFI suppression performance in wire-line systems

To evaluate the performance of RFI suppression methods, simulations are conducted assuming typical MIMO DMT receiver. The implementation of the information source, channel encoder, interleaver - deinterleaver and optimal linear precoder for complex signals is the same as the one for wireless channels. For the simulations, the number of used cable pairs is: $N=[1,2,3,4]$ and the corresponding number of MIMO inputs/outputs is: $K=2N-1$. The Digital Modulator is implemented as 8192-point Inverse Fast Fourier Transform (IFFT) process. The DMT symbol consists of up to 4096 tones. Each DMT data tone can use a different Grey encoded QAM modulation format depending on the Signal to Noise Ratio. After the IFFT process, the prefix and suffix guard intervals are added.

The MIMO wire-line channel model is realized in accordance with ITU-T Recommendations G.993.2 and G.996.1. The DSL cable test loop is modeled for common mode excitation, using the ABCD parameters block matrix. For experiments 26-gauge cable (AWG 26) is chosen. The background noise with Power Spectrum Density (PSD) at -140 dBm/Hz is modeled as Additive Complex Arbitrary White Gaussian Noise - $N_c(0, 1)$. The model includes wide-scale frequency variations with standard statistics determined from measured actual Far End Crosstalk (FEXT) and Near End Crosstalk (NEXT) transfer functions.

In the DMT Demodulator the guard prefix and suffix intervals are removed and 8192-point FFT is applied. Further, Frequency Domain Per-Tone Adaptive Channel Equalization and DMT demodulation are performed. Finally, OLP, 64-QAM demodulation and Error Correction Decoding are implemented.

For the simulation of the Excision, Frequency Identification and Cancellation and Adaptive Filtering method in the MIMO GDSL the same principles as in wireless system simulation are applied. The RFI is modeled as a complex single tone, the frequency of which is located in the middle between two adjacent DMT tones.

Using the above simulation model of MIMO Gigabit DSL system, different experiments have been performed, estimating BER as a function of the Signal to Interference Ratio (SIR). In respect to the number of used twisted pairs, four DSL systems are considered: Single Input Single Output (SISO) VDSL2 (1-pair), MIMO GDSL: 2, 3 and 4-pair. The DSL channels are subject to FEXT, NEXT and background AWGN with flat PSD at -140 dBm/Hz.

In case of 2 and 4-pair MIMO GDSL channel (Fig.13 a,b) the best results in terms of RFI filtering are obtained for the highest value of channel diversity: 4-pair Gigabit DSL MIMO system. The Frequency Excision Method manifests good performance for high SIR. It should be noted that the adaptive filtering scheme and frequency cancellation scheme lead to a slight degradation of the overall performance when $SIR > 0$, which is due to the amplitude and phase distortion caused by the adaptive notch filters or due to a wrong estimation of RFI parameters during the identification procedure. The degradation could be reduced by implementing higher-order notch filters or by applying more sophisticated identification algorithms. Its negative effect can be avoided by switching off the filtering when $SIR \sim 0$.

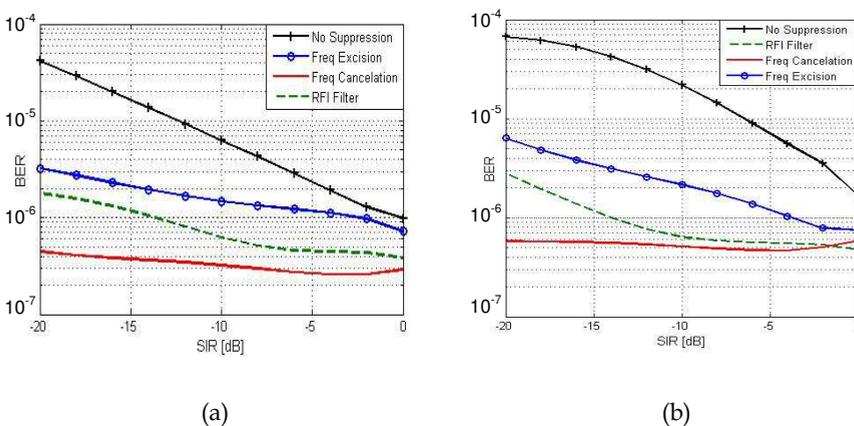
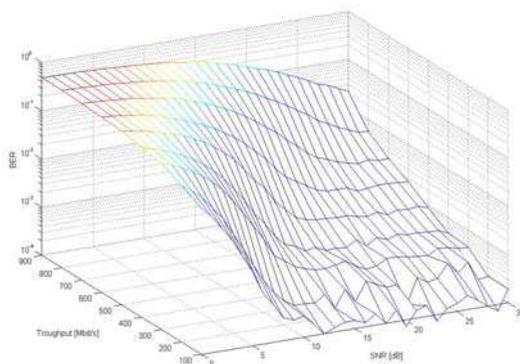
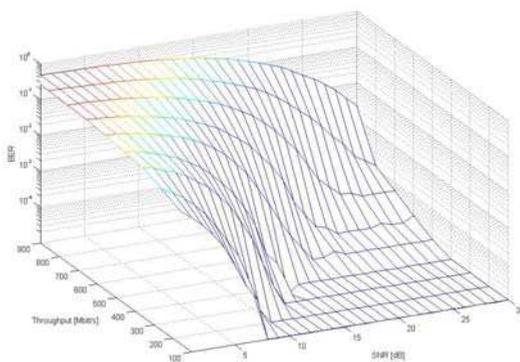


Fig. 13. BER as a function of SIR for 2-pair and 4-pair GDSL

The results have outlined the fact, that the Frequency Identification and Cancellation Method gives highest performance. However, the extremely high computational complexity limits its application up to the available hardware resources. In this aspect, the Complex Adaptive Notch Filter Bank turns to be the optimal narrowband interference suppression technique, offering the trade-off between excellent performance and low computational complexity. The Frequency Excision Method demonstrates reasonable performance as well as high computational efficiency. Figure 14 presents the relation between BER, Throughput and SNR for 4x4 MIMO GDSL DMT single user communication system for SIR=-10dB (Cable 24 AWG, L=300m.), where (a) is without RFI cancellation and (b) with RFI cancellation.



(a)



(b)

Fig. 14. Relation between BER, Throughput and SNR for 4x4 MIMO GDSL DMT single user communication system.

6. Conclusion

In this chapter some of the major NBI suppression methods were outlined. Their application in different types of wireless MIMO and MIMO DSL channels MIMO was considered. Using a simulation model the different methods were analyzed and compared in terms of computational complexity and error rate improvement. The authors consider such an approach to the comparison of narrowband interference suppression methods important for correct overall performance estimation. Each method has a different computational complexity and error rate performance depending on the type and parameters of the MIMO system and the communication channel. Choosing a NBI suppression method for practical implementation in most cases is a trade-off between good performance and lower computational complexity.

From the general methods for NBI suppression - Frequency Excision, Adaptive Filtering, Identification and Cancellation, the last gives best error rate performance. However, the extremely high computational complexity limits its application up to the available hardware resources. Complex Adaptive Filtering offers a trade-off between good error performance and lower computational complexity. The Frequency Excision Method demonstrates reasonable error performance as well as high computational efficiency.

The simulation results also show that the application of a general method for NBI suppression along with one of the specific methods that are used in wireless MIMO systems such as Orthogonal Space-Time Block Coding improves the error rate performance. Similar is the case in wire-line subscriber systems where other specific methods such as Dynamic Spectrum Management (Level 3), Optimal Precoding and Multi-channel Adaptive Filtering are used.

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In recent years, it was realized that the MIMO communication systems seems to be inevitable in accelerated evolution of high data rates applications due to their potential to dramatically increase the spectral efficiency and simultaneously sending individual information to the corresponding users in wireless systems. This book, intends to provide highlights of the current research topics in the field of MIMO system, to offer a snapshot of the recent advances and major issues faced today by the researchers in the MIMO related areas. The book is written by specialists working in universities and research centers all over the world to cover the fundamental principles and main advanced topics on high data rates wireless communications systems over MIMO channels. Moreover, the book has the advantage of providing a collection of applications that are completely independent and self-contained; thus, the interested reader can choose any chapter and skip to another without losing continuity.

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