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Abstract

In the past decades, multiple-point geostatistical methods (MPS) are increasing in popularity in various fields. Compared with the traditional techniques, MPS techniques have the ability to characterize geological reality that commonly has complex structures such as curvilinear and long-range channels by using high-order statistics for pattern reconstruction. As a result, the computational burden is heavy, and sometimes, the current algorithms are unable to be applied to large-scale simulations. With the continuous development of hardware architectures, the parallelism implementation of MPS methods is an alternative to improve the performance. In this chapter, we overview the basic elements for MPS methods and provide several parallel strategies on many-core architectures. The GPU-based parallel implementation of two efficient MPS methods known as SNESIM and Direct Sampling is detailed as examples.

Keywords: geostatistics, multiple point, stochastic simulation, training image, many-core architecture

1. Introduction

Geostatistical stochastic simulation is important for the research of geological phenomenon. In the past several decades, a large number of geostatistical methods have been developed based on the spatial covariance properties of the geological data. The traditional tool to quantify the spatial covariance is known as variogram, which measures the covariance among any two points separated by a certain distance [1]. Although variogram-based methods are successfully applied to multi-Gaussian system, they have limitations for the characterization of complex systems such as the curvilinear or long-range continuous facies [2–4]. An alternative known as multiple-
point geostatistical (MPS) simulation was proposed to produce geologically realistic structure by using high-order spatial statistics based on conceptual training images [5, 6]. The concept of training image is introduced from explicit to represent geological structures with a numeral image generated from outcrops, expert sketching, or conditional simulations of variogram-based methods. Since the training images can incorporate additional information such as the expert guesses, prior database, and physical models, besides the spatial features, the simulation using TIs is straightforward and smart [7].

Due to the ability of reconstructing geological realistic, MPS methods are gaining popularity, and various algorithms have been proposed including pixel-based algorithms [5, 8, 9], pattern-based algorithms [10–13], and optimal algorithms [14–16]. These algorithms have been applied to broad fields such as oil and gas industry [17–19], fluid prediction [20, 21], climate modeling [22]. However, some application suffers from the computational burden routinely. Since MPS methods need to scan the training image, abstract patterns, and reconstruct the patterns in the simulation grid, physical memory and running time are challenging or even unusable for large-scale or pattern-rich simulation models.

Many effects have been made to decrease the central processing units (CPU) and RAM expense. Approaches such as multiple grid technique [23], optimization of data storage with a list structure [24], hierarchical decomposing [25], Fourier space transform [26] have been introduced, while the computational burden remains heavy for very large grids and complex spatial models.

With the development of hardware, utilization of multiple-core central processing units (CPU), or graphic processing units (GPU), for parallel applications are increasing in popularity in various fields including geostatistical simulation. In 2010, Mariethoz investigated the possibility to parallelize the MPS simulation process on realization level, path-level, or node-level and proposed a general conflict management strategy [27]. This strategy has been implemented on a patch-based SIMPAT method [28]. Parallel implements for other geostatistical algorithms, such as the parallel two-point geostatistical simulation [29], parallel pixel-based algorithms [30], and parallel optimal algorithms [31] have been proposed constantly.

In this article, we will present the parallel several schemes of MPS simulation on many-core and GPU architectures. The Compute Unified Device Architecture (CUDA) that provides access between CUPs and GPUs is used to illustrate the parallel strategies [32, 33]. Examples of the two general MPS algorithms known as SENSIM and DS are implemented and compared [34, 35] with the original algorithms to present the ability of pattern reproduction and the improvement of computational performance.

2. Methodology

Currently, geostatistical simulations are processed with a large number of MPS algorithms using various techniques. Besides the difference in process definition and algorithmic implementation, these algorithms share similarities of the fundamental elements [36].
2.1. General framework

Generally, the overall framework of these algorithms is constructed as follows:

1. Migrate conditioning points to the corresponding grid nodes.
2. Define data template to abstract or clustering patterns from the training image.
3. Define a simulation path for the nodes to be simulated.
4. Using the conditioning data and previous simulated nodes as priori data to sample from the training image.
5. Place the sample to the simulation grid.
6. Repeat three–five until meeting the stopping criterion.

For each algorithm, one or some of the basic steps may have some identity. In this section, we will focus on the two algorithms following different theory, single normal equation simulation (SNESIM) and DS, to illustrate the application of parallel strategies on MPS simulations.

2.2. SNESIM review

The methodology of single normal equation simulation (SNESIM) is a sequential paradigm developed from the random concepts theory with the property of generating conditional distribution with local conditioning instead of global conditioning. The local conditional distribution is aggregated with the local data event. Considering a category property S with K possible states \( s(k), k = 1, \ldots, K \), a data template \( \tau_n \) is comprised of a geometry of \( n \) vectors \( \{h_\alpha, \alpha = 1, \ldots, n\} \). The data event \( d_n \) centered at \( u \) is defined with the template and the corresponding \( n \) values \( \{s(u + h_\alpha), \alpha = 1, \ldots, n\} \). Consequently, the conditional probability of the occurrence of state \( s_k \) denoted as \( \text{Prob} \{S(u) = s_k | S(u_\alpha), \alpha = 1 \ldots n\} \) or \( \text{Prob} \{S(u) = s_k | d_n\} \) is defined following Bayes’ theorem:

\[
\text{Prob} \{S(u)=s_k | d_n\} = \frac{\text{Prob} \{S(u)=s_k \text{ and } d_n\}}{\text{Prob} \{d_n\}} \tag{1}
\]

Where \( \text{Prob} \{d_n\} \) and \( \text{Prob} \{S(u) = s_k \text{ and } d_n\} \) are the probability of the occurrence of \( d_n \) and the associated to a central value \( S(u) = s_k \) respectively. In practice, this probability can be obtained by counting the number of replicates of the training image, which is calculated by:

\[
\text{Prob} \{S(u)=s_k | d_n\} = \frac{c_k(d_n)}{c(d_n)} \tag{2}
\]

\( c(d_n) \) is the number of replicates of the conditioning data \( d_n \) and \( c_k(d_n) \) is the number of replicates inferred from \( c(d_n) \) of which the central node \( S(u) \) has a value of \( s(k) \).
To reduce the computational burden of scanning the training image, SNESIM analyzes the training image and constructs a search tree to store all the patterns before sequential simulation. Then the same data template is used to aggregate the local distribution of the simulation grid for sampling values from the database to the simulation grid.

The implementation of SNESIM algorithm is shown in Figure 1.

![Figure 1. Flowchart for SNESIM process.](image)

As described, the memory consumption is largely related to the size of data template and the pattern richness of the training image. At the same time, the pattern retrieving time also increases for the complex cases. To address this problem, a GPU-based parallel method is proposed in the following section.

2.3. Direct Sampling review

Direct Sampling is a novel MPS technique that borrows ideas from a sampling method introduced by Shannon totally abandoning the conditional probability approach. Instead of the conditional distribution, a measurement distance is used to calculate the similarity between
the local conditioning and the data event got from the training image along a random path. The distance method enables the application to both categorical and continuous variables. During the sequential simulation, for each node to be simulated in the simulation grid, the training image is scanned along a circular unilateral path [37] and the distance is calculated. As long as the distance is smaller than the defined threshold, the current data event in the training image is sampled, and the central value is assigned to the node to be simulated in the simulation grid directly. The flowchart of Direct Sampling is shown in Figure 2.

Figure 2. Flowchart for Direct Sampling process.
Since this method does not need to store patterns, it releases the memory intensity; on the other hand, parameter is the key factor for Direct Sampling.

There are three main input parameters:

1. Maximum number of closest neighbors $n$, namely, the size of data template of SNESIM.
2. The distance threshold $t$. A value of $t = 0$ means a trend of verbatim copy of the training and the increasing value introduce more variabilities between realizations in pattern reproduction.
3. The fraction of scanned TI $f$. The fraction is defined to stop the process of scanning the training image while no distances are under the threshold. If the percentage of nodes in the training image reach $f$, the scanning stops and the pattern with lowest distance is sampled.

Sensitivity analysis of parameters [38] shows trade-offs between the quality of realizations and the CPU times.

3. Many-core architectures

3.1. Overview

A computing component that featured with two or more processing units to execute program instructions independently is known as a multicore processor. With the ability of running multiple instructions at the same time, multicore processors increase overall speed for many general-purpose computing. Currently, adding support for more execution threads is the norm avenue to improve the performance of high-end processors. The many-core architectures are formed by manufacturing massive multicores on a single component. For general-purpose parallel computing, many-core architectures on both the central processing unit (CPU) and the graphics processing unit (GPU) are available for different tasks.

Compared with a many-core CPU architecture known as a supercomputer, the general GPU has many more cores, which are constructively cheap and suitable for intensive computing.

3.2. GPU and CUDA

Originally, a GPU is a graphic card attached with a cluster of streaming processors aimed at graphic-oriented details that needs the ability of extremely fast processing of large-volume data sets. To apply the special-purpose GPU to general-purpose application, NVIDIA provides a user-friendly development environment that is Compute Unified Device Architecture (CUDA). The CUDA platform enables the generation of parallel codes on GPUs by driving the process from the CPU to GPU. A CUDA program is a unified code that consists of executions on both the host (CPU) and the device (GPU) by CUDA kernel functions that are called out from the host to the device for asynchronously execution. The massive parallelism is carried out in each kernel on CUDA threads that are the basic executing units on the GPU. The CUDA
provides an interface named Peripheral Component Interconnect Express (PCI-e) for the intercommunication between host and device and shared memory for synchronization among the parallel threads. The general architecture of CUDA and CUDA memory is illustrated in Figures 3 and 4. More details could be referred from the Guides of NVIDIA.

Figure 3. The general architecture of CUDA.

Figure 4. CUDA device memory organization.
4. Parallel strategies

Generally, there are three strategies to implement the parallelism of MPS algorithms, that is, realization-level, path-level, and the node-level parallelization. The bottleneck for large-scale application focuses on the millions’ of nodes in the training image and simulation grids. So we present two parallel implementations on node-level for SNESIM and on both node-level and path-level for Direct Sampling in this section.

4.1. GPU-based SNESIM implementation

In 2013, a node-level parallelization was applied to SNESIM algorithm and achieved significant performance improvement [34]. The overall parallel scheme is illustrated in Figure 5.

By transferring the training image and simulation grid from the CPU to GPU, each node is assigned to a CUDA thread. For each unsimulated node along the random simulation path, Kernel 1 compares each value of the given data template $d_n$ with every central nodes in the training image simultaneously and returns the number of replicates $c_k(d_n)$ for each stage $k$. With these outputs, Kernel 2 calculates the conditional cumulative distribution function (CCDF) and uses Monte Carlo sampling to draw a value to this node. Repeat the kernels along a random path until all the nodes in the simulation grid are simulated. Transfer the results from GPU to CPU.
Since the most time-consuming part, that is getting data event for each node, is parallelized in Kernel 1, this GPU-based implementation gains significant speedup. Moreover, in contrast with the increasing physical memory demanding along the template sizes of original implementation, the proposed GPU implementation fixes the amount of memory.

### 4.2. GPU-based Direct Sampling implementation

Similar parallelization could also be applied to the Direct Sampling algorithm. Besides the parallelism of the data template, the searching fraction could also be parallelized. The two-stage parallel scheme was implemented in 2013 [35]. The procedure of the GPU-based implementation is illustrated in **Figure 6**.

![Figure 6. Procedure of GPU-based Direct Sampling implementation.](http://dx.doi.org/10.5772/64276)
As described, there are three important parameters controlling the simulation of Direct Sampling, that is \( t, n, \) and \( f \). This scheme implements the parallelism on two of the three parameters that is \( n \) and \( f \).

4.2.1. Parallelism of \( n \)

The number of neighbor is the \( n \) closest previously simulated nodes to define a data template. Different from the data template used in SNESIM that is controlled by the predefined geometry, the data templates consisted of the \( n \) closest simulation nodes and have the flexibility of adaption shape and searching range. Due to these flexibilities, this approach can directly catch large-scale structures and easily condition to hard data. On the other hand, the searching for the \( n \) neighbors is also the most time-consuming part in the serial implementation.

The parallelism of \( n \) is achieved in Kernel 2 and Kernel 3. In Kernel 2, each previously simulated node is allocated to a CUDA thread and calculates the Euclidean distance to the node to be simulated simultaneously. These distances are transferred to Kernel 3 and sorted using a parallel sorting algorithm.

4.2.2. Parallelism of \( f \)

In the serial program if the similarity-distance between data events of the simulation grid and the one sampled from the current training image node is higher than the threshold, a new central node will be sampled from the training image along a random path. Most nodes of the training image that may be visited is defined as \( f \times N^{TI} \), as a result, large amount of data event will be sampled in large-scale 3-days simulations.

The parallelization of \( f \) is implemented in Kernel 4 that allocates \( f \times N^{TI} \) threads to \( f \times N^{TI} \) central nodes in the training image using a unique random path denoting each node. Thus these similarity distances are calculated simultaneously. There are two possibilities for the similarity distance and the data sampling strategy is shown as follows:

1. There are values lower than the threshold \( t \), choose the one that has the smallest path index from the data events with a lower distance.
2. There are no values lower than the threshold \( t \), choose the one that has the smallest path index from the data events with the lowest distance.

Finally, the central value of the chosen data event is assigned to the simulation grid by Kernel 6. Repeat all these kernels until all the nodes in the simulation grid are simulated.

5. Experiments

In this section, the performance of the GPU-based implementations is compared with that obtained using SGeMS software [39]. A computer with 4 GB main memory, Intel Core i3540 3.07 GHz CPU, and NVIDIA GeForce GTX 680 GPU that contains eight streaming multiprocessors with 192 CUDA Cores/MP and 2 GB device memory is used for the simulation. The
programming platform is the NVIDIA driver version 301.42 with CUDA version 4.2 implemented on VS2010 using C++.

To test the performance of the GPU-based SNESIM algorithm, a 2D porous slice image obtained by CT scanning is used as the training image. The $200 \times 200$ pixels training image and the corresponding histogram for background and the pore are shown in Figure 7.

![Figure 7. Training image of porous slice and the Histogram.](image)

Realizations of the same size as the training image using data template of 50, 120, 200, and 350 nodes are generated for each simulation. The realizations generated with CPU and GPU are shown in Figure 8. The average variograms for each simulation are shown in Figure 9a, and
the performance is shown in Figure 9b. The results show that the proposed GPU-based algorithm can generate similar realizations as the original algorithm, whereas significantly increases the performance. The speedup ranges from six to 24 times depending on the template size than a larger template size resulting in a larger speedup.

![Figure 9](image.png)

Figure 9. Results and performance comparison between the CPU and GPU implementation. (a) Variogram of the training image and the average variogram of the realizations of Figure 8 and (b) speedup obtained by using the GPU-based parallel scheme.

The performance of the GPU-based Direct Sampling algorithm is also compared with the original algorithm on a 100 × 130 by 20 fluvial reservoir training image as shown in Figure 10.

![Figure 10](image.png)

Figure 10. A 100 × 130 by 20 fluvial reservoir training image.

Parameter sensitivities are analyzed on $n = 30, 50, 100, 200, f = 0.005, 0.01, 0.02, 0.05$, and $t = 0.01, 0.02, 0.05, 0.1$, respectively, with which reasonable realizations are generated. The performance times are shown in Figure 11.
The results show that GPU-based implementation significantly improves the performance for all the tests. Moreover, the sensitivity of parameters to performance is alleviated with the parallel scheme. The time difference is around 200 s for $n$ and $f$ and almost none for $t$ for the GPU-based implementation, whereas it can be as large as several magnitudes for the CPU-based implementation.

In summary, both the presented GPU-based parallel schemes for SNESIM and Direct Sampling achieve significant speedups, especially for large-scale simulations with their node-level parallelism strategy. Moreover, the parallel implementations are insensitive to parameters that are the key points not only for performance but also for simulation results implying for better results in application. These strategies could be further improved with other parallel optimization methods as well. In fact, besides the node-level parallel schemes for SNESIM and Direct Sampling, various parallelisms have been proposed and new optimizations are keeping introduced aimed at further improvements. Up to now, almost all kinds of MPS algorithms could be implemented on a parallel scheme. Many-core architectures are the current main-streams to improve the performance of extremely massive computing tasks. The developing of computer hardware and parallel interface techniques promise the wider and wider utilization of high-performance parallelization. These parallel schemes of training images-based stochastic simulations approve the application to high-resolution and large-scale simulations.
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References


