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Electric Motor Performance Improvement Using Auxiliary Windings and Capacitance Injection

Nicolae D.V
Tshwane University of Technology
South Africa

1. Introduction
Generally, some electric machines such as induction machines and synchronous reluctance motors require reactive power for operation. While the reactive power required by a synchronous machine can be taken from the power source or supplied by the machine itself by adjustment of the field current, the power factor of an induction machine is always lagging and set by external quantities (i.e., the load and terminal voltage). Poor power factor adversely affects the distribution system and a cost penalty is frequently levied for excessive VAr consumption.

Power factor is typically improved by installation of capacitor banks parallel to the motor. If the capacitor bank is fixed (i.e. that it can compensate power factor only for a fixed load), when the load is variable, then the compensation is lost. Some authors (El-Sharkawi et al, 1984, Fuchs and Hanna, 2002) introduced the capacitors using thyristor/triac controllers; by adjusting the firing angle, the capacitance introduced in parallel with the motor becomes variable and thus compensating the power factor for any load. Other works (Suciu et al, 2000.) consider the induction motor as an RL load and power factor is improved by inserting a variable capacitor (through a bridge converter) which is adjusted for unity according with the load. For the above methods, the capacitive injection is directly into the supply. Another method conceived for slip ring induction motor was to inject capacitive reactive power direct into the rotor circuit (Reinert and Parsley, 1995; Suciu, et al. 2002).

The injection of reactive power can be done through auxiliary windings magnetically coupled with the main windings (E. Muljadi et al. 1989; Tamrakan and Malik, 1999; Medarametla et al. 1992; Umans, and H. L. Hess, 1983; Jimoh and Nicolae, 2006, 2007). This compensating method has also been applied with good results not only for induction motors but also for a synchronous reluctance motor (Ogunjuyigbe et al. 2010).

2. Method description
2.1 Physical solution
The method described in this chapter makes use of two three-phase stator windings. One set, the main winding (star or delta), is connected directly to the source. The other set of windings - auxiliary, is only magnetically coupled to the main winding. All windings have the same shape and pitch, but may have different turn numbers and wire sizes; usually smaller in order to be accommodated in the slots together with the stator. The windings are
arranged in slots such that there is no phase shift between the two windings. Figure 1 shows a possible arrangement of the windings for a four pole induction machine.

![Diagram of windings arrangement](image)

**Fig. 1. High Power factor induction machines-windings arrangement**

**2.2 Auxiliary windings connections**

As mentioned above, the main winding can have delta or star connection. Figure 2 shows the main winding connected in star and the auxiliary windings connected in generic (a), star (b) and delta (c) to the capacitor bank via a static switch.

Figure 3 shows a simpler way to inject capacitive reactive power. In this method, the auxiliary windings are in “single-phase connection” with the apparent advantage of using only one capacitor and static switch.

**2.3 Variable Capacitors**

In order to achieve a compensation for various loading of the machine, the compensating capacitor should be able to be varied. This capability is obtained through connecting a fixed capacitor via a static switch. The static switch can be achieved using thyristors or IGBTs in bidirectional configuration.
Fig. 2. Auxiliary windings: a) generic connection; b) star connection; c) delta connection

Fig. 3. Auxiliary windings: “single-phase connection”
2.3.1 Thyristor-based variable capacitor

Figure 4 shows the use of thyristor to accomplish a variable capacitor. The inductor $L_r$ is introduced to reduce – limit the surge current; it is relatively small and does not affect the overall capacitive behaviour.

![Thyristor-based variable capacitor](image)

Fig. 4. Variable capacitor using bidirectional thyristor

The equivalent capacitance depends on the delay angle. Due to the phase angle control, the device introduces harmonic currents.

2.3.2 IGBT-based variable capacitor

The above drawback can be address using IGBTs in bidirectional configuration (Figure 5) and a switching frequency higher then operational frequency (50 Hz).

![IGBT-based variable capacitor](image)

Fig. 5. IGBT in bidirectional topology

Figure 6 shows a configuration to achieve a variable capacitor using two bidirectional static switches. The main capacitor $C_1$ is introduced in the auxiliary winding circuit, via a bidirectional switch $Sw_1$, for a period of time depending on the duty cycle ($\delta$) of the switching frequency; in this time the bidirectional switch $Sw_2$ is OFF. When $Sw_1$ is OFF, the capacitor is discharged. The reactor $L_r$ limits the capacitive surge current without affecting the capacitive behaviour.

![Variable capacitor using two IGBTs in bidirectional topology](image)

Fig. 6. Variable capacitor using two IGBTs in bidirectional topology
The capacitor $C_2$, much smaller than $C_1$ is connected to mitigate the voltage spikes during switching off the main capacitor. Thus, the equivalent capacitor can be written as:

$$C_{eq} = \delta \times C_1 + C_2$$ (1)

### 2.3.3 Variable capacitor H-topology

Figure 7 shows a **single-phase H topology** to achieve a variable capacitor. This configuration using H-bridge bidirectional topology obtains a higher equivalent capacitance for the same fixed one as reference. In this configuration, the reactor $L_r$ has the same purpose of limiting the surge capacitive current, while $C_2$ also of small value mitigates the voltage spikes. The equivalent capacitance could be express as:

$$C_{eq} = C_2 + \frac{C_1}{(2\delta - 1)^2}$$ (2)

It can be notice that the equivalent capacitance could increase significant when the duty cycle approaches 50 %. In practice, the switches are not ideal and there is no “infinite increase” of the equivalent capacitance.

![Fig. 7. Variable capacitor using H-bridge bidirectional topology](image)

![Fig. 8. Variable capacitor using three-phase H-bridge topology](image)
Another solution to achieve a variable capacitance, or rather to generate a capacitive current was proposed using a **three-phase H topology** as PWM inverter (E. Muljadi, et al. 1989; Tamrakan and Malik, 1999) as presented in Figure 8. The converter injects capacitive reactive power into auxiliary windings and thus improving the power factor of the motor.

### 3. Mathematical model

The machine is treated as having two three-phase windings and the voltages equations system can be written as:

\[
[V_{abc}] = [R_1][I_{abc}] + \frac{d}{dt}[\lambda_{abc}] 
\]

\[0 = [R_2][I_{xyz}] + \frac{d}{dt}[\lambda_{xyz}] + V_{cxyz} \]  

\[0 = [R_r][I_{abcr}] + \frac{d}{dt}[\lambda_{abcr}] \]

where

\[
V_{abc} = \begin{bmatrix} V_a & V_b & V_c \end{bmatrix}^T
\]

\[
I_{abc} = \begin{bmatrix} I_a & I_b & I_c \end{bmatrix}^T; \quad \lambda_{abc} = \begin{bmatrix} \lambda_a & \lambda_b & \lambda_c \end{bmatrix}^T
\]

\[
[R_1] = \begin{bmatrix} r_a & 0 & 0 \\ 0 & r_b & 0 \\ 0 & 0 & r_c \end{bmatrix}, \quad [R_2] = \begin{bmatrix} r_x & 0 & 0 \\ 0 & r_y & 0 \\ 0 & 0 & r_z \end{bmatrix}
\]

Note that indices “1” refer to the main winding and “2” to the auxiliary winding.

\[
\begin{bmatrix} \lambda_{abcs} \\ \lambda_{xyz} \\ \lambda_{abcr} \end{bmatrix} = \begin{bmatrix} L_{abc} & L_{abcsxyz} & L_{abcr} \\ L_{xyzabc} & L_{xyz} & L_{xyzabcr} \\ L_{abcrs} & L_{abcrsyz} & L_{abcr} \end{bmatrix} \begin{bmatrix} I_{abcs} \\ I_{xyz} \\ I_{abcr} \end{bmatrix}
\]

The inductances in eq. (9) are time dependent, and this make the equation difficult and time consuming to solve. In order to obtain constant parameters, the voltage equations (3-5) are then transformed to the rotor reference frame. To achieve this, the equations are multiplied with an appropriate transformation matrix \(K(\theta)\) to obtain:

\[
[K(\theta)][V_{abcs}] = [R_1][K(\theta)][I_{abc}] + \frac{d}{dt}[K(\theta)][\lambda_{abcs}] 
\]

\[0 = [R_2][K(\theta)][I_{xyz}] + \frac{d}{dt}[K(\theta)][\lambda_{xyz}] + [K(\theta)]V_{cxyz} \]
\begin{equation}
0 = [R_r][K(\theta_r)][I_{abr}] + \frac{d}{dt}[K(\theta_r)][\lambda_{abr}]
\end{equation}

When these equations are expanded, after substantial matrix manipulations, it resolves to:

\begin{equation}
[V_{qdo1}] = [R_{s1}][I_{qdo1}] + \frac{d}{dt}[[\lambda_{qdo1}]] + [\varpi][\lambda_{qdo1}]
\end{equation}

\begin{equation}
0 = [R_r][I_{qdo2}] + \frac{d}{dt}[[\lambda_{qdo2}]] + [\varpi][\lambda_{qdo2}] + [V_{c,qdo2}]
\end{equation}

\begin{equation}
0 = [R_r][I_{qdo2}] + \frac{d}{dt}[[\lambda_{qdo2}]] + [\varpi][\lambda_{qdo1}]
\end{equation}

where

\begin{equation}
[\varpi] = \begin{bmatrix}
0 & 1 & 0 \\
-1 & 0 & 0 \\
0 & 0 & 0
\end{bmatrix} \quad \text{and} \quad [\varpi_r] = (\omega - \omega_r)
\end{equation}

and

\begin{equation}
[V_{c,qdo2}] = \frac{1}{C} \int [I_{qdo2}] dt + [\varpi][V_{c,qdo2}]
\end{equation}

Neglecting the ‘0’ sequence since we initially are assuming a balanced system, the expression for the stator and rotor flux linkages, resolves into the matrix:

\begin{equation}
\begin{bmatrix}
\lambda_{q1} \\
\lambda_{d1} \\
\lambda_{q2} \\
\lambda_{d2} \\
\lambda_{qr} \\
\lambda_{dr}
\end{bmatrix} = \begin{bmatrix}
L_{ls1} + L_m & 0 & L_{lm} + L_m & 0 & L_m & 0 \\
0 & L_{ls1} + L_m & 0 & L_{lm} + L_m & 0 & L_m \\
L_{lm} + L_m & 0 & L_{ls2} + L_m & 0 & L_m & 0 \\
0 & L_{lm} + L_m & 0 & L_{ls2} + L_m & 0 & L_m \\
L_m & 0 & L_m & 0 & L_{lsr} + L_m & 0 \\
0 & L_m & 0 & L_m & 0 & L_{lsr} + L_m
\end{bmatrix} \begin{bmatrix}
I_{q1} \\
I_{d1} \\
I_{q2} \\
I_{d2} \\
I_{qr} \\
I_{dr}
\end{bmatrix}
\end{equation}

\section{4. Equivalent model}

\subsection{4.1 Symmetrical loaded auxiliary windings}

When each phase of the auxiliary windings is loaded with equal capacitors (C), eventually star connected, the entire circuit is having a symmetrical behaviour and the equivalent circuit is very simple as shown in Figure 9.

Fig. 9. Equivalent circuit for symmetrical loading auxiliary winding
This equivalent circuit has two branches, each having separate resistance ($R_1$ – main and $R_2$ - auxiliary) and leakage reactance ($L_{l1}$ – main and $L_{l2}$ – auxiliary) together with a common mutual leakage inductance $L_m$, which occurs due to the fact that the two set of windings occupy the same slots and therefore mutually coupled by their leakage flux. The mutual inductance that occurs between main winding and rotor is represented by $L_m$.

Other parameters of the equivalent circuit are: main winding resistance $R_1$, auxiliary winding resistance $R_2$, main winding leakage reactance $L_{l1}$, auxiliary winding leakage inductance $L_{l2}$; mutual leakage inductance $L_m$, rotor leakage inductance $L_{lr}$; and the rotor resistance $R_r$ and “$s$” is the slip.

In this analysis there is no need to refer the auxiliary winding quantities to the main winding, because the two sets of windings are wound for the same number of turns with a transformation ratio of one.

The above equivalent circuit helps us to determine the input impedance seen from the supply and the condition for unity power factor.

\[
Z_{in} = R_1 + jX_{l1} + \frac{(R_3 + R_2 + X_3 + X_2)}{(R_1 + R_2 + jX_2 + X_3)} \tag{19}
\]

Where: $R_1$ and $jX_{l1}$ are the components of the main winding (per-phase impedance), $X_2$ is the equivalent reactance of the auxiliary winding including the compensating capacitor, $R_2$ is the resistance (per-phase) of the auxiliary winding, $R_3$ and $X_3$ are the equivalent resistance and reactance of the paralleling the rotor branch with magnetizing branch:

\[
X_2 = \frac{1}{\omega C} X_{l2} \tag{20}
\]

\[
X_3 = \text{Im} \left\{ jX_{lm} + \left[ \left( R_r/s \right) + jX_{lr} \right] / \left( jX_m \right) \right\} \tag{21}
\]

\[
R_s = \text{Re} \left\{ \left[ \left( R_r/s \right) + jX_{lr} \right] / \left( jX_m \right) \right\} \tag{22}
\]

The condition for unity power factor is:

\[
\text{Im} \left\{ Z_{in} \right\} = 0 \tag{23}
\]

Which, after some mathematical manipulation can be written as:

\[
\alpha X_2^2 + \beta X_2 + \gamma = 0 \tag{24}
\]

With:

\[
\alpha = X_3 + X_{l1} \tag{25}
\]

\[
\beta = -R_2 R_3 + (R_1 + R_2) R_3 + 2X_3 X_{l1} \tag{26}
\]

\[
\gamma = -X_3 \left[ R_2 R_3 - (R_2 + R_3) R_2 \right] + X_{l1} \left[ (R_2 + R_3)^2 + X_3^2 \right] \tag{27}
\]
The equation (24) together with relations (25) to (27) produces two solutions, which means for a given slip (s) there are two values for the capacitor satisfying the condition for unity power factor. The practical/recommended value is the high $X_2$ or small $C$ connected to the auxiliary winding in order to have a small current through it.

### 4.2 Asymmetrical loaded auxiliary windings.

If the auxiliary windings are connected as “single-phase configuration”, then the system has an asymmetrical behaviour. This connection is obtained by connecting in series the three auxiliary windings and thus we can write: $I_x = I_y = I_z = I_X$. Using this condition of current in the expansion that results to equations (3) – (18) it can be written: $I_{d2} = I_{q2} = 0$, thus the resulting expression from this can be represented in a d-q-0 equivalent circuit of Figure 10 shown below.

![ Equivalent Circuit Diagrams](image-url)
The particularity of connecting the auxiliary windings in a single phase winding creates an asymmetrical situation which brings about the relevance of the zero sequence. The power factor of the machine could be defined by the argument of $Z_a$, which is $V_a/I_a$. And this is expressed as:

$$Z_a = \frac{V_a}{I_a} = \frac{V_{q1} + V_{u1}}{I_{q1} + I_{u1}}$$  \hspace{1cm} (28)$$

$$V_{d1}(C) = (j\omega C + Z_{q1}) \times I_{d1} \times \frac{(Z_{q1} + Z_{im})}{Z_{im}}$$ \hspace{1cm} (29)$$

As can be observed from the equations (28) and (29), the power factor of the machine depends on $C$ and thus it can be brought to unity by means of adjusting the equivalent capacitance.

It should be also noticed that the asymmetrical behaviour of the auxiliary windings connected as “single-phase configuration” has got a significant drawback namely creating torque ripple. This disadvantage should not be overseen by the simplicity of the physical solution. Given this, further in this, we will consider only the symmetrical loading of the auxiliary winding.

5. Concept validation

For the validation of this concept of improving performances of the induction motor injecting capacitive reactive power via auxiliary windings, a standard 4 kW, 380V, 50Hz, 4 pole, 36 slots with frame size DZ113A induction motor have been used. The stator was rewound with two full-pitches, single layer windings (see Figure 1). The main windings – delta connected have same number of turns like in the original motor but the size of the wire has been reduced to accommodate the auxiliary windings. The auxiliary windings were connected in delta in order to reduce current through them. For this study, the auxiliary windings have the same number of turns as main windings. The rotor is unchanged. Table 1 shows the parameters of the modified motor under test obtained using the IEEE test procedure. The mutual leakage inductance $X_{im}$ is very small compared to the other reactances \(\) (E. Muljadi et al, 1989).

<table>
<thead>
<tr>
<th>Description of data</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Main Winding Rated Voltage</td>
<td>380 V</td>
</tr>
<tr>
<td>Auxiliary Winding Rated Voltage</td>
<td>380V</td>
</tr>
<tr>
<td>Number of poles</td>
<td>4</td>
</tr>
<tr>
<td>Magnetizing Reactance ($X_m$)</td>
<td>37.86 $\Omega$</td>
</tr>
<tr>
<td>Main winding phase resistance ($R_1$)</td>
<td>4.33 $\Omega$</td>
</tr>
<tr>
<td>Auxiliary winding phase resistance ($R_2$)</td>
<td>18.1 $\Omega$</td>
</tr>
<tr>
<td>Main winding leakage reactance ($X_{l1}$)</td>
<td>6.97 $\Omega$</td>
</tr>
<tr>
<td>Auxiliary winding leakage reactance ($X_{l2}$)</td>
<td>6.97 $\Omega$</td>
</tr>
<tr>
<td>Rotor resistance ($R_r$)</td>
<td>1.35 $\Omega$</td>
</tr>
<tr>
<td>Rotor leakage reactance ($X_{lr}$)</td>
<td>1.97 $\Omega$</td>
</tr>
<tr>
<td>Full load main winding current</td>
<td>8.6 A</td>
</tr>
</tbody>
</table>

Table 1. Specific parameters of the induction motor under test
Firstly, the motor was tested without compensation; the results are presented in Table 2.

<table>
<thead>
<tr>
<th>I_L (A)</th>
<th>T_L (Nm)</th>
<th>P (W)</th>
<th>S (VA)</th>
<th>PF</th>
<th>Slip</th>
<th>RPM</th>
</tr>
</thead>
<tbody>
<tr>
<td>5.43</td>
<td>1.83</td>
<td>678.6</td>
<td>3568.7</td>
<td>0.17</td>
<td>0.0026</td>
<td>1496</td>
</tr>
<tr>
<td>5.56</td>
<td>4.73</td>
<td>1734</td>
<td>3655.1</td>
<td>0.43</td>
<td>0.0060</td>
<td>1491</td>
</tr>
<tr>
<td>6.02</td>
<td>5.49</td>
<td>1992</td>
<td>3957.5</td>
<td>0.49</td>
<td>0.0086</td>
<td>1487</td>
</tr>
<tr>
<td>6.88</td>
<td>7.53</td>
<td>2709</td>
<td>4522.9</td>
<td>0.61</td>
<td>0.0153</td>
<td>1477</td>
</tr>
<tr>
<td>7.74</td>
<td>9.89</td>
<td>3540</td>
<td>5088.2</td>
<td>0.70</td>
<td>0.0213</td>
<td>1468</td>
</tr>
<tr>
<td>8.61</td>
<td>12.1</td>
<td>4179</td>
<td>5653.6</td>
<td>0.74</td>
<td>0.056</td>
<td>1416</td>
</tr>
</tbody>
</table>

Table 2. Experimental data for the motor under test

5.1 Simulation results

Based on Matlab platform, a simulation model has been built (Figure 11). The parameters from Table 1 have been used for Matlab model after delta-star transformation. The rotor resistor was simulated using a variable resistor depending on slip. The model was run firstly to show the capability of adjusting the power factor via the static switch.

![Basic simulation model](image)

Fig. 11. Basic simulation model

5.1.1 Thyristor-based variable capacitor

One of the first solutions to introduce a variable capacitor was to use an “ac-ideal” switch based on two thyristors anti-parallel connected. The test was done using a 100 µF and a delay angle of 45° for a slip of 0.0026 (no load). This results in a reduction of reactive power drawn by the motor from 1193 VAr to 46 VAr. The main drawback of this switching solution is the strong distorting currents introduced as could be seen in Figure 12. As could be noticed, both currents main and auxiliary are very much distorted. Obviously, the power factor compensation is accompanied with degrading of all other performances of the motor.
5.1.2 IGBT-based variable capacitor

The other solution tested to obtaining variable capacitor was that of Figure 6. The values for the two capacitors were chosen as: $C_1 = 100 \ \mu F$ and $C_2 = 1 \ \mu F$. The validation simulation was done for a slip of $s = 0.0026$; the switching frequency was 1 kHz and then the duty cycle manually adjusted. Figure 13 shows the main and auxiliary currents toward supply voltage for a duty cycle of 40 % (Fig.13. a) and 80% (Fig.13. a).

As can be noticed a duty cycle of 40 % does adjust the shift between the main current and voltage marginally increasing the power factor from 0.15 to 0.32 lagging. When the duty cycle was increased to 80%, then the main current arrived in phase with the voltage. It can also be noticed a relative high ripple especially for low duty cycle.

Figure 14 shows the same simulation conditions, but now the switching frequency was raised to 4 kHz. As can be noticed the ripple has been reduced significant.

The other methods of producing variable capacitive reactive power, meaning the H-bridge topologies require a more complex control system and are not addressed in this study.
5.1.3 Capacitance versus slip for unity power factor

Now, the model was run for each value of the slip (speed) given in Table 2. The result of these simulations is the capacitance producing unity power factor (see Table 3).

<table>
<thead>
<tr>
<th>s ( (n) )</th>
<th>( C_Y ) ( (\mu F) )</th>
<th>( I_a ) ( (A) )</th>
<th>( P_a ) ( (W) )</th>
<th>( Q_a ) ( (VAr) )</th>
<th>( S_a ) ( (VA) )</th>
<th>PF</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0026 ( (1496) )</td>
<td>0</td>
<td>5.49</td>
<td>184</td>
<td>1193</td>
<td>1207</td>
<td>0.152</td>
</tr>
<tr>
<td>&amp; 81</td>
<td>1.65</td>
<td>362</td>
<td>9</td>
<td>363</td>
<td>0.999</td>
<td></td>
</tr>
<tr>
<td>0.006 ( (1491) )</td>
<td>0</td>
<td>5.65</td>
<td>366</td>
<td>1187</td>
<td>1242</td>
<td>0.295</td>
</tr>
<tr>
<td>&amp; 81</td>
<td>2.57</td>
<td>565</td>
<td>11</td>
<td>565</td>
<td>0.999</td>
<td></td>
</tr>
<tr>
<td>0.0086 ( (1487) )</td>
<td>0</td>
<td>5.86</td>
<td>505</td>
<td>1186</td>
<td>1289</td>
<td>0.392</td>
</tr>
<tr>
<td>&amp; 81.6</td>
<td>3.27</td>
<td>718</td>
<td>15</td>
<td>719</td>
<td>0.999</td>
<td></td>
</tr>
<tr>
<td>0.0153 ( (1477) )</td>
<td>0</td>
<td>6.71</td>
<td>855</td>
<td>1200</td>
<td>1473</td>
<td>0.58</td>
</tr>
<tr>
<td>&amp; 87</td>
<td>5.21</td>
<td>1143</td>
<td>1</td>
<td>1143</td>
<td>0.999</td>
<td></td>
</tr>
<tr>
<td>0.0213 ( (1468) )</td>
<td>0</td>
<td>7.68</td>
<td>1160</td>
<td>1229</td>
<td>1689</td>
<td>0.686</td>
</tr>
<tr>
<td>&amp; 90</td>
<td>6.82</td>
<td>1499</td>
<td>17</td>
<td>1499</td>
<td>0.999</td>
<td></td>
</tr>
<tr>
<td>0.056 ( (1491) )</td>
<td>0</td>
<td>8.31</td>
<td>1330</td>
<td>1252</td>
<td>1826</td>
<td>0.728</td>
</tr>
<tr>
<td>&amp; 90.6</td>
<td>7.66</td>
<td>1684</td>
<td>27</td>
<td>1686</td>
<td>0.999</td>
<td></td>
</tr>
</tbody>
</table>

Table 3. Simulation results: capacitance versus slip for unity power factor

It is interesting to observe that the capacitance producing unity power factor does not vary so much as presented in other studies (E. Muljadi et al. 1989; Tamrakan and Malik, 1999) concerning similar method of injecting capacitive reactive power.

Moreover, it could be found a fix value of 75 \( \mu F \) which maintain a high power factor irrespective of the load/slip. Table 4 shows the simulation results for the fixed capacitor and variable load/slip.

Figure 15 shows the variation of the power factor versus slip and Figure 16 shows the variation of the supply current versus slip for compensated with a fix 75 \( \mu F \) capacitor per phase and uncompensated machine.
<table>
<thead>
<tr>
<th>s</th>
<th>$C_Y$ (µF)</th>
<th>$I_a$ (A)</th>
<th>$P_a$ (W)</th>
<th>$Q_a$ (VAr)</th>
<th>$S_a$ (VA)</th>
<th>PF</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0026</td>
<td>75</td>
<td>1.57</td>
<td>330</td>
<td>101</td>
<td>345</td>
<td>0.956</td>
</tr>
<tr>
<td>0.006</td>
<td>75</td>
<td>2.47</td>
<td>531</td>
<td>111</td>
<td>542</td>
<td>0.978</td>
</tr>
<tr>
<td>0.0086</td>
<td>75</td>
<td>3.16</td>
<td>683</td>
<td>123</td>
<td>694</td>
<td>0.984</td>
</tr>
<tr>
<td>0.0153</td>
<td>75</td>
<td>4.91</td>
<td>1066</td>
<td>170</td>
<td>1079</td>
<td>0.987</td>
</tr>
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</table>

Table 3. Simulation results: capacitance versus slip for unity power factor

Fig. 15. Power Factor versus slip

Fig. 16. Supply current versus slip

5.2 Experimental validation
After rewinding the machine under test with both sets of windings delta connected, three identical capacitors were connected to the auxiliary. Then the “compensated” motor was loaded gradually to get the same speeds as for the “uncompensated” motor.
The testing started with a capacitance of 25 µF as found during the simulation: $C_\Delta = C_Y / 3$. This did not produce the results found via the simulation. Then a value of 28 µF was found to give a relative even power factor of approximate 0.95 in the entire loading range (see Table 4).
Figure 17 shows the phase voltage ($v_{an}$) and current ($i_a$) for the uncompensated (Fig. 17.a) and compensated (Fig. 17.b) with slip of 0.0026. It can be observed, the power factor increased from 0.17 to 0.937 which represent 450% improvement for no load. For full load the improvement in power factor is 29%.

<table>
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<tr>
<th>$I_L$(A)</th>
<th>$T_L$(Nm)</th>
<th>P(W)</th>
<th>S(VA)</th>
<th>PF</th>
<th>Slip</th>
<th>RPM</th>
</tr>
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<tbody>
<tr>
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<td>2.81</td>
<td>1058</td>
<td>1129</td>
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<td>0.0026</td>
<td>1496</td>
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Table 2. Experimental data for the motor under test

Fig. 17. Voltage and current for: a) uncompensated motor; b) compensated motor

6. Comments

This study proved that direct injecting capacitance reactance through auxiliary winding does improve the power factor of the induction motor; it also increases the ratio torque over current. What is also very interesting is this method achieves a “flat” variation of power factor with respect of load variation. This is a very important improvement given the fact that majority of induction motors do not work at constant full load where the classic design produces maximum performances.

However, this method introduces extra copper losses reducing the overall efficiency and increasing the operation temperature.

This study did not intended to elucidate the full effect of the method upon the torque especially the existence of the influence produced by the current flowing through auxiliary windings. The only aspect clearly noticed was the torque ripple introduced by the “single-phase” auxiliary winding connection.

Further more, the same method was applied to a synchronous reluctance motor (Ogunjuyigbe et al, 2010). The same type of stator winded similarly as above was used with a salient milled rotor obtained from the corresponding squirrel cage induction motor. The experimental results show an improvement of the power factor from 0.41-0.69 to 0.93-0.97 for the entire loading range.
The economic benefits are related with the savings on demand especially for places where a large number of three-phase induction motors are used under variable loading.

7. References


The subject of this book is an important and diverse field of electric machines and drives. The twelve chapters of the book written by renowned authors, both academics and practitioners, cover a large part of the field of electric machines and drives. Various types of electric machines, including three-phase and single-phase induction machines or doubly fed machines, are addressed. Most of the chapters focus on modern control methods of induction-machine drives, such as vector and direct torque control. Among others, the book addresses sensorless control techniques, modulation strategies, parameter identification, artificial intelligence, operation under harsh or failure conditions, and modelling of electric or magnetic quantities in electric machines. Several chapters give an insight into the problem of minimizing losses in electric machines and increasing the overall energy efficiency of electric drives.

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