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Design and Simulation of RFID Aperture Coupled Fractal Antennas

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Abstract Different fractal antennas based on aperture coupled feeding technique are studied, analysed and compared for size reduction, low profile, and good omini-dirctional pattern suitable for RFID applications. The results are used as a guideline to propose modified fractal shapes patch antennas having lower size reduction parameters. All the designed antennas are based on zero - order square patch antenna where different fractal geometries are introduced to miniaturize the size of antenna for 5.8 GHz band. A maximum reduction in patch antenna size of 59.80 % is achieved when using modified Minkowski pre-fractal patch antenna.

Keywords Aperture Coupled, Fractal Antenna, RFID

1. Introduction

Radio frequency Identification (RFID), which was developed around World War II, is a technology that provides wireless identification and tracking capability. In recent years, RFID technology has been rapidly developed and applied to many service industries, distribution logistics, manufacturing companies, goods flow systems, and mobile dongle applications [1, 2]. Several frequency bands have been assigned to RFID applications: 125 kHz, 13.56 MHz, 869 MHz, 902–928 MHz, 2.450 (2.400–2.483) GHz and 5.800 (5.725–5.875) GHz. The advantage of operating at higher frequencies is a longer range with high data transfer rate [3].

The rapid advancements in RFID technologies are the driving force in design and development of compact and light weight antennas [4, 5]. These features can be obtained using fractal geometry-based antennas [6, 7]. Fractals naturally arise in many mathematical fields which work with recursive procedures, for example, in dynamical systems and stochastic processes [8]. Applying fractals to the antenna elements allows for smaller size, multi-band and broad-band properties [9, 10].

Fractals have self-similar shapes and can be subdivided in parts such that each part is a reduced size copy of the whole. Self-similarity of fractals causes multi-band and broad-band properties and their complicated shapes provide design of antennas with smaller size. Fractals have convoluted and jagged shapes with many corners that these discontinuities increase bandwidth and the effective radiation of antennas. Fractals can be placed long electrical length in to a small area using their ability of space filling [11].

Fractal antennas have some very special properties [9, 10] that make them attractive for the design of small antennas. These properties are

- Broad band operation the fractal antennas radiate and detect efficiently within a wide range of frequencies. The frequency range is specified by the smallest and largest size present in the antenna. The radiation pattern, and hence the detection efficiency do not vary much as a function of frequency.
- Gain the fractal antennas can display a gain that depends relatively slowly on frequency over a large frequency range.
- Spatial structure the fractal antennas can display a spatial structure which is also related to the antenna gain, as the antenna concentrate radiated power in certain positions and not in others.

Even though the theory behind fractal antennas is quite complex, their applicability to RFID is promising. In order to achieve the desired features of RFID antenna (compact size, low profile, environment insensitive, conformal and multi hand or broadband operation), a planar microstrip configuration with fractal geometry is one of the possibilities.

For microstrip patch antennas, aperture coupling [12, 13] is preferred to other feeding mechanisms as it offers greater design flexibility. Aperture coupling has considerable advantage as a feeding mechanism particularly in fractal designs where identifying a suitable feed position on such complex geometrical shapes is particularly difficult [14, 15]. In Ref. [16], a modified square fractal aperture coupled patch antenna has been used for ISM frequency band 2.4 *GHz* – 2.485 *GHz* and from 5.725 *GHz* to 5.875 *GHz* for RFID.

This paper presents design issues related to miniaturized aperture coupled fractal antennas suitable for 5.8 GHz ISM RFID band. The rest of the paper is organized as follows. Section II introduces the main concepts behind aperture coupled patch antenna. Section III presents various fractal patch antenna geometries along with design concepts. Modified fractal RFID patch antennas are given in section IV. Hybrid modified Koch fractal antennas are present in section V. Relation comparison of different types of fractal patch antennas and the main conclusions drawn from this study is presented in sections VI and VII, respectively. Simulation is presented using CST MWS 2010.

2. Aperture Coupled Feeding

The geometry of the aperture-coupled feeding is shown in Fig.1. This antenna consists of two substrates separated by

a ground plane. The top substrate (ε_{r1}) contains the radiating element, and the bottom substrate (ε_{r2}) contains the microstrip feed line. A small aperture is cut in the ground plane to allow coupling from open circuited microstrip feed line to the radiating patch. The parameters on which resonant frequency of the antenna depends upon are shape and dimensions of the radiating element, dimensions of the ground plane, shape and size of the aperture, dimensions of feed line, position of feed line and the dielectric constants of the two substrates.



Figure 1. Aperture coupled patch antenna.

3. Fractal Antenna Geometries and Design Concepts

3.1 Reference Patch

A simple microstrip patch antenna is known as the iteration zero of fractal patch antenna. For iteration zero the basic formulas for determining the length and width of a microstrip patch antenna are used. These formulas are [17]

$$W = \frac{v_o}{2f_r} \sqrt{\frac{2}{\varepsilon_r + 1}} \tag{1}$$

$$\varepsilon_{eff} = \frac{\varepsilon_r + 1}{2} + \frac{\varepsilon_r - 1}{2} \left(\frac{1}{\sqrt{1 + 12h/W}} \right) \tag{2}$$

$$\Delta L = 0.412 h \frac{\left(\varepsilon_{eff} + 0.300\right) \left[\frac{W}{h} + 0.264\right]}{\left(\varepsilon_{eff} - 0.258\right) \left[\frac{W}{h} + 0.813\right]}$$
(3)

$$L = \frac{v_o}{2f_r \sqrt{\varepsilon_{eff}}} - 2\Delta L \tag{4}$$

where *W* is the width, *L* is the length, ΔL is the length reduced from the antenna to reduce fringing effects, ε_r is the dielectric constant, v_o is the speed of wave in free space, and ε_{eff} is the effective dielectric constant. Using Eqns. 1-4, the patch antenna is designed using the following parameters

 $\varepsilon_{r1} = 4.3$, h1 = 1.6 mm, and $f_r = 5.8$ GHz

The dimensions of the patch are calculated to be

$$L = 11 mm, \qquad W = 14 mm$$

The designed patch antenna is simulated using CST MWS 2010. The simulation takes into account various structure parameters associated with the coupled aperture such as slot length L_{slot} , slot width W_{slot} , and strip line parameters: strip length Lstrip and strip width W_{strip} . Finally substrate length L_{sub} , and substrate width *W*_{sub} parameters are used.

The simulation yields a resonance frequency of 6.4 GHz which is higher than the target one 5.8 GHz. The patch structure parameters are then optimized to yield a simulated resonance frequency of 5.8 GHz under square patch condition L = W = 10 mm. These parameter values will be used later as the starting point (reference patch) to design various fractal antennas considered in this work. Table 1 shows the optimized antenna parameters for the reference patch antenna.

Parameters	Values	Parameters	Values
L = W	10	W _{strip}	2.4
L _{slot}	6.43	W _{slot}	0.5
L_{strip}	5	h_1	1.6
L _{sub}	20	h_2	0.8
W _{sub}	20	ε_{r1}	4.3
	20	ε_{r2}	2.33

Table 1. Optimized antenna parameters in (mm) to achieve $f_r = 5.8 GHz$ for reference square patch antenna.

Figure 2 shows simulation results related to the reflection return loss S_{11} of the optimised reference patch antenna.



Figure 2. Simulation return loss S_{11} of reference patch antenna. The 3D patterns as well the 2D copolar and crosspolar patterns for the reference patch are also introduced in Figure 3.



Realized Gain Copolar (Phi=0)



c. Figure 3. Patterns of the reference patch.

Theta / Degree vs. dB

It is worth to mention here that introducing fractal geometry on the reference patch antenna will reduce the resonant frequency. The dimension of the patch should be shortened as in Fig. 4 to produce $f_r = 5.8 GHz$.

Crosspolar

The figure of merit used to measure the quality of the fractal antenna in this paper is the area reduction factor ΔA defined as

$$\Delta A = \left(1 - \frac{L_f^2}{L^2}\right)\Big|_{f_r = 5.8 \ GHz} \tag{5}$$

Angular width (3 dB) = 110.4 deg.

where *L* and L_f is the length of the square patch in the absence and presence of fractal geometry, respectively.



Figure 4. Area size reduction for fractal patch antenna *a*. Reference patch *b*. Fractal patch.

3.2 .Sierpinski Carpet Fractal Patch Antenna

Sierpinski carpet fractal antenna is the most widely studied fractal geometry for antenna application [18, 19]. The fractal antenna consists of geometrical shapes that are repeated; each ones have a unique attributes. The self-similarity that distributed on this antenna expected to cause its multi-band characteristic. On the others hand its can solve a traditional antenna that operate at single frequency.

The following formulas are used to add further iterations after designing the zero iteration of Sierpinski carpet geometry

$$N^{(n)} = 8^n \tag{6}$$

$$A^{(n)} = (8/9)^n L_o^2 \tag{7}$$

Further one can show that

$$L_{perim}^{(n)} = 4 \left(1 + \sum_{i=1}^{n} 8^{i-1} / 3^{i} \right) L_{o}$$
(8)

where L_o denotes the length of the reference patch, $N^{(n)}$ is the number of squares which will be covered with a radiating material, $L_{perim}^{(n)}$ is the perimeter length at iteration n, and $A^{(n)}$ is the area of patch at iteration n.

As the iterations are added, some area of the radiating patch is removed and therefore, the physical dimensions of the radiating patch reduce. Thus the initial resonating frequency will shift from 5.8 *GHz* to some lower frequency because of increasing the current path length. As the radiating patch continues to reduce in size, the resonating frequency will continue to shift to lower frequency bands as further iterations are added. This property helps in achieving higher multiple bands, while maintaining the original size of the patch.

Sierpinski carpet fractal patch antenna designed with one, two and three iterations are analysed and simulated and the results are listed in Table 2. The results include antenna dimensions, scattering parameter S_{11} , bandwidth, and gain at 5.8 *GHz*. One can notice that when the iteration increases more reduction in patch size is obtained. With three iteration, a patch antenna size reduction of 20.79% is obtained. A new design concept is deduced from these results that more reduction is obtained when the ratio of perimeter length of patch to its enclosed area becomes higher.



Figure 5. Simulation return loss S_{11} of third iteration Sierpinski fractal patch antenna.

	Zero Iteration	First Iteration	Second Iteration	Third Iteration
Δ A (%)	-	13.51	15.36	20.79
L _{perim} (mm)	40.00	49.60	69.51	112.00
$A(mm^2)$	100.00	76.88	66.87	55.63
L_{perim}/A	0.40	0.64	1.04	2.15
$S_{11}(dB)$	-33.20	-37.19	-29.43	-23.39
BW (MHz)	356	341	340	340
Gain (dB)	4.04	3.80	3.78	3.66

Table 2. Simulated parameters of Sierpinski carpet fractal antenna.

Figure 5 shows the S_{11} simulation of the third iteration Sierpinski fractal patch antenna. The 3D patterns as well the copolar and crosspolar patterns (yz plane) at 5.8 GHz for the third iteration Sierpinski fractal patch antenna are introduced in Fig. 6.



Figure 6. Patterns of the third iteration Sierpinski fractal patch antenna.

3.3 Minkowski Fractal Antenna

The application of fractal geometry to conventional antenna structures optimizes the shape of the antennas in order to increase their electrical length, which thus reduces their overall size. Though different fractal geometries are available, a very few can be used in the design of microstrip antennas. One such geometry is Minkowski fractal antenna [20-22].

The fractal dimension D is a number which characterizes fractal structures. This parameter can be understood as a measurement of the space-filling ability by a fractal form. There are different definitions of D. One of them, which we use here, is the Hausdorff–Besicovich dimension (or self-similarity dimension) [11]. In this definition, the dimension D is the solution of the equation

$$k_1 \left(\frac{1}{h_1}\right)^D + k_2 \left(\frac{1}{h_2}\right)^D + \dots + k_m \left(\frac{1}{h_m}\right)^D = 1$$
(9)

where k_m is the number of the copies of the initiator scaled by h_m and m is the number of different scale that the fractal possesses. For the Minkowski fractal antenna there are three scales $(1 - a_1)$, a_2 , and a_1 , and $k_1 = 2$, $k_2 = 2$, $k_3 = 1$, thus Eqn. 9 becomes

$$2\left(\frac{1}{2}(1-a_1)\right)^D + 2(a_2)^D + (a_1)^D = 1$$
(10)

where a_1 is the ratio W_1/L_o and a_2 is the ratio W_2/L_o . Then according to Eqn. 9, when $a_1 \text{ or/and } a_2$ are varied, fractal structures with different dimensions may be obtained. The dimension of the traditional Minkowski island fractal, according to Eqn.10 is equal to 1.465 where in such case a_1 and a_2 both are equal to 1/3 [Fig. 7].



Figure 7. Construction of the Minkowski-like fractal structure *a*. the generator *b*. first iteration, *c*. square patch antenna.

The design of fractal Minkowski patch antenna begins from the design of the zeroth iteration which is as the same as in Sierpinski Carpet antenna. The perimeter of one side antenna at the n iteration is found as

$$L_{perim}^{(n)} = (1 + 2a_2)L_{perim}^{(n-1)}$$
(11)

where $L_{perim}^{(n)}$ is the perimeter at iteration number *n* and $L_{perim}^{(n-1)}$ is the perimeter at iteration number (n-1). The area of patch after first iteration is

$$A^{(1)} = (1 - 4a_1a_2)L_o^2 \tag{12}$$

and the area after second iteration is

$$A^{(2)} = \left(1 - 2a_1a_2(3 + 3a_1^2 - 2a_1 + 4a_2^2)\right)L_o^2 \quad (13)$$

It's found that the ratio of perimeter to area for any scales a_1 , a_2 and at any iteration gives an indication on the reduction in patch antenna size.

Two iterations of fractal Minkowski fractal antenna with different scales are simulated and the results are listed in Tables 3 and 4. From these tables a large reduction in patch size (%) is obtained when $a_1 = a_2 = 0.33$ which corresponds to a large ratio of perimeter length to enclosed area as indicated for Sierpinski carpet patch antenna. The return loss S_{11} as well bandwidth and gain are also listed in Tables 3 to 4.

The copolar and crosspolar patterns of the second iteration Minkowski fractal patch antennas when $a_1 = a_2 = 0.33$ are introduced in Fig. 8. Figure 9

show the S_{11} characteristics for the second iteration Minkowski fractal patch antenna when b = 0.33 and 0.22, respectively.

The results are displayed for three values of the scale parameter *a*: 0.11, 0.22 *and* 0.33. When the scale *a* increases for a fixed values of the scale *b*, the resonance frequency deceases, since the perimeter length of the patch increases. When b = 0.33, the resonance frequency is 6.880, 6.285, and 5.802 GHz when a = 0.11, 0.22 and 0.33 respectively. These values are to be compared with , 5.802, *and* 5.704 *GHz*, respectively, when b = 0.22

			×		
a_1, a_2	-, -	0.33, 0.22	0.33, 0.33	0.11, 0.11	0.05, 0.33
D	1.000	1.298	1.465	1.172	1.549
Δ A (%)	-	19.00	39.63	13.51	19.00
L _{perim} (mm)	40.00	52.00	51.80	45.46	44.00
$A(mm^2)$	100.00	57.00	33.54	82.21	79.00
L_{perim}/A	0.400	0.912	1.545	0.553	0.557
$S_{11}(dB)$	-33.20	-21.33	-24.06	-22.68	-27.00
BW (MHz)	356	218	171	337	272
Gain (dB)	4.04	3.43	2.56	3.80	3.58

Table 3. Simulated parameters of the first iteration fractal Minkowski patch antenna.

		*	×	**	*	**
<i>a</i> ₁ , <i>a</i> ₂	0, 0	0.22, 0.22	0.33, 0.22	0.33, 0.33	0.11, 0.33	0.22, 0.33
D	1.000	1.306	1.298	1.465	1.509	1.471
Δ A (%)	-	29.44	36.00	49.02	38.69	47.29
L _{perim} (mm)	40.00	70.10	66.76	72.34	87.00	80.67
$A(mm^2)$	100.00	50.34	36.84	15.73	46.50	28.12
L_{perim}/A	0.400	1.392	1.812	5.042	1.870	2.868
$S_{11}(dB)$	-33.20	-42.10	-51.30	-49.21	-43.15	-47.64
BW (MHz)	356	245	239	156	239	192
Gain (dB)	4.04	3.31	3.16	1.78	3.02	2.59

Table 4. Simulated parameters of the second iteration fractal Minkowski patch antenna.



Figure 8. 2D Pattern of the second iteration Minkowski fractal patch antennas when $a_1 = a_2 = 0.33$.



Figure 9. Return loss S_{11} when a = 0.11, 0.22, and 0.33 for the second iteration Minkowski fractal patch antenna (a) b = 0.33(b) b = 0.22.

3.4 Koch Fractal Patch Antenna

Koch fractal geometry exhibits well-known features that have been used to construct miniaturized monopole and loop antennas [23-25]. By applying the Koch fractal shape to the antennas, the overall electrical length of the antennas increases and the resonance frequency becomes lower than that of conventional monopole, loop, and patch-type antenna. In this paper, Koch fractal geometry is applied to microstrip patch antennas to reduce their overall size. Figure 10 shows four iterations of fractal Koch curves. In this paper, the indentation angle α is taken as a design parameter rather setting it to 60° as in conventional Koch fractal patch [26]. This gives us an additional design parameter which can be used to achieve extra size reduction (See Fig. 10).

The dimension of the modified Koch fractal patch can be calculated by applying the scales of

$$S_2 = S_3 = \frac{L_o}{3}$$
 (14a)

$$S_1 = S_4 = L_o\left(\frac{1}{2} - \frac{1}{3}\cos\theta\right)$$
 (14b)

$$k_1 = k_2 = 2, h_1 = 3, h_2 = (3 - 2\cos\theta)/6$$
 (14c)

where θ is an indentation angle. Substituting these parameters in Eqn. 9, we obtain

$$2\left(\frac{1}{3}\right)^{D} + 2\left(\frac{3-2\cos\theta}{6}\right)^{D} = 1$$
 (15)

The solution of this transcendental equation gives the value of *D* for a given θ .

The perimeter length of the wire L_{perim} is important parameter that indicates the longer of it is the lowerresonance frequency. The perimeter length of the proposed modified Koch patch geometry, at any angle and at any iteration, is found as



Figure 10. Curves corresponding to the four first iterations of Koch fractal.

$$L_{perim}^{(n)} = 4 \left[\frac{2}{3} \left(\frac{5}{3} - \cos \theta \right) \right]^n L_o$$
(16)

where $L_{perim}^{(n)}$ is the perimeter length at iteration *n* and L_o is the one side length of the square patch antenna. The effective area of modified Koch patch at any angle θ and iteration number *n* is found to be

$$A^{(n)} = \left[1 - 4\left(\sum_{i=1}^{n} \frac{4^{i-1}}{9^{i}}\right)\cos\theta\sin\theta\right]L_{o}^{2}$$
(17)

Table 5 shows the calculated length $L_{perim}^{(n)}$, area $A^{(n)}$, and dimension *D* for four iterations and different values of θ .

It is found that as the iteration number and iteration factors increase, the resonance frequencies become lower than those of the zero iteration, which represents a conventional square patch. In other words, microstrip patch antennas employing Koch fractal island geometry can operate at a much lower frequency range while maintaining identical overall antenna characteristics.



Figure 11. Relation between area of fractal Koch patch antenna with number of iterations for different values of indentation angles.

The enclosed area of the Koch fractal antenna decreases with increasing the number of iterations. The enclosed area is the same at indentation angle θ and $90^\circ - \theta$, this is clear from Fig. 11. Figure 12 indicates that the perimeter length of Koch fractal patch increases with number of iterations. Longer perimeter is obtained when large indentation angle is used. The ratio of perimeter length to enclosed area is large when more iterations and large indentation angle are used as shown in Fig. 13.



Figure 12. Relation between perimeter of fractal Koch patch antenna for different values of indentation angles and number of iterations.



Figure 13. Variation of perimeter to area ratio of fractal Koch patch antenna with indentation angles and number of iterations.



Figure14. Return loss S_{11} for different values of indentation angles (30°, 45°, 60°, and 75°) for Koch fractal patch antenna. (a) first iteration (b) second iteration (c) third iteration.

Figure 14 show the variation of the simulated reflection return loss S_{11} with indentation angle for iteration one, two, and three, respectively. The location of S_{11} minimum occurs at lower frequency when indentation angle increases, i.e. the resonance frequency decreases when the indentation angle increases.

The minimum miniaturized size is achieved when third iteration and indentation angle θ of 75° are used. This corresponds to 34.06 % reduction in enclose patch area (See Tables 6-8).

$\theta(deg.)$ D	$L_{perim}^{(n)}$ (mm)				$A^{(n)}(mm^2)$				
	n = 1	n = 2	n = 3	n = 4	n = 1	n = 2	n = 3	n = 4	
15	1.017	4.09	4.18	4.28	4.38	0.889	0.840	0.818	0.808
30	1.067	4.36	5.17	5.17	5.63	0.808	0.722	0.684	0.667
45	1.148	4.78	6.83	6.83	8.16	0.788	0.679	0.635	0.616
60	1.261	5.33	9.48	9.48	12.6	0.808	0.722	0.684	0.667
75	1.411	5.98	8.93	13.3	19.9	0.889	0.840	0.818	0.808

Table 5. Variation of *D*, $L_{perim}^{(n)}$, and $A^{(n)}$ as a function of nand θ for the modified Koch fractal patch antenna.

θ (deg.)	0	30.00	45.00	60.00	75.00
Dimension	1.000	1.067	1.148	1.261	1.411
Δ A (%)	-	20.79	25.00	29.94	31.11
L _{perim} (mm)	40.00	38.78	41.40	44.64	49.60
$A(mm^2)$	100.00	63.96	58.33	56.57	61.23
L_{perim}/A	0.40	0.60	0.71	0.79	0.81
$S_{11}(dB)$	-33.20	-33.82	-34.48	-31.25	-41.87
BW (MHz)	356	304	276	274	274
Gain (dB)	4.04	3.62	3.45	3.41	3.43

Table 6. Simulated parameters of the first iteration Koch fractal patch antenna.

θ (deg.)	0	30.00	45.00	60.00	75.00
D	1.000	1.067	1.148	1.261	1.411
Δ A (%)	-	17.55	21.50	31.11	31.77
L _{perim} (mm)	40.00	43.09	50.63	59.02	73.75
$A(mm^2)$	100.00	59.52	55.30	49.47	57.27
L_{perim}/A	0.40	0.72	0.95	1.18	1.28
$S_{11}(dB)$	-33.20	-42.18	-39.88	-37.91	-37.05
BW (MHz)	356	292	268	256	257
Gain (dB)	4.04	3.57	3.44	3.32	3.36

Table 7. Simulated parameters of the second iteration Koch fractal patch antenna.

		×	×	X	
θ(deg.)	0	30	45	60	75
Dimension	1.000	1.067	1.148	1.261	1.411
Δ A (%)	-	22.56	32.35	31.77	34.06
L _{perim} (mm)	40.00	45.50	56.18	78.31	108.33
$A(mm^2)$	100.00	52.97	42.97	46.68	53.90
L_{perim}/A	0.40	0.86	1.30	1.68	2.00
$S_{11}(dB)$	-33.20	-30.10	-27.31	-37.32	-35.41
BW (MHz)	356	289	275	242	255
Gain (dB)	4.04	3.42	3.32	3.25	3.29

Table 8. Simulated parameters of the third iteration Koch fractal patch antenna.

4. Modified Fractal Antennas

This section introduces modified Minkowski fractal antenna, Sierpinski Gasket fractal as a bowtie shape patch antenna, and hybrid fractal as modified Koch fractal ring patch with and without repeated scaled-Koch ring fractal patch antenna. The concepts of modification are identified and supported by simulation results.

4.1 Modified Minkowski Fractal Antenna

In order to achieve a reduced size of the patch antenna, a new geometry is proposed here which is derived from fractal Minkowski patch geometry. The recursive iteration of this fractal starts from the zero-order normal patch then two scales are used to generate two subpatches, one with scale se_1 , and the one other with a scales c_1 . The se_1 scaled patch at the centre and sc_1 scales the patch at the four corners of se_1 scaled centered patch. After succeed iteration new scales se_2 , and sc_2 are used, and so on, as shown in Fig. 15.

The modified Minkowski fractal antenna (MMPFA) for five patch shapes and different scales are simulated. The simulated results, return loss S_{11} , gain, and bandwidth are listed in Table 9. We notice that all shapes of the proposed antenna (MMPFA1 to MMPFA6) except MMPFA4 have more reduction in size than other fractal shapes mentioned in this paper (See Table 9).



F igure 15. Iteration o	f modified Mink	owski fractal	patch antenna.
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	MMFA1	MMFA2	MMFA3	MMFA4	MMFA5	MMFA6
sc1, sc2, sc3	0.4, 0.5, 0.48	0.4, 0.46, 0.54	0.6, 0.65, 0.5	0.4, 0.4, 0.6	0.4, 0.6, 0.6	0.45, 0.35, 0.65
se1, se2, se3	0.46, 0.5, 0.47	0.46, 0.46, 0.49	0.46, 0.46, 0.4	0.4, 0.46, 0.5	0.4,0.55,0.45	0.35, 0.45, 0.45
Δ A (%)	43.75	52.11	51.42	16.28	46.71	59.80
$S_{11}(dB)$	-29.11	-17.1	-18.82	-37.47	-39.62	-36.3
BW (MHz)	186	139	175	287	169	143
Gain (dB)	2.36	1.09	2.17	3.68	2.13	1.33

 Table 9. Simulated parameters of the proposed modified Minkowski fractal patch antenna.

	Zero Iteration	First Iteration	Second Iteration	Third Iteration	Fourth Iteration
Δ A (%)	-	48.48	49.16	50.01	52.39
$S_{11}(dB)$	-33.20	-41.29	-34.38	-44.23	-31.77
BW (MHz)	356	172	164	166	178
Gain (dB)	4.04	2.23	2.11	2.03	2.23

Table 10. Simulated parameters of bowtie Sierpinski fractal antenna.

The 2D copolar and cross polar patterns at 5.8 GHz are introduced in Fig. 16. We one can notice from Fig. 16 that these patterns are similar to the patterns of the reference patch antenna A simulation of the return loss S_{11} of MMFA6 that has the highest reduction in size area reduction (59.80%) is shown in Fig. 17.



Figure 16. 2D Pattern of modified Minkowski fractal patch (MMFA6).



Figure 17.Simulated return loss S_{11} of the MMFA6 proposed modified Minkowski fractal patch antenna.

4.2 Bowtie Sierpinski Gasket Fractal Antenna

The Sierpinski fractal patch antenna is one of widely used and studied by literature because of its behaviour and its multiband characteristics. In this paper a two Sierpinski fractal patches (as a bowtie shape) are used as the unit cell for the fractal geometry.

Four iterations of bowtie Sierpinski fractal patch antenna are simulated and the results at resonant frequency of 5.8 GHz are listed in Table 10. The return loss S_{11} , gain and bandwidth are the main results that tabulated in Table 10. Note that the four iterations give approximately the same size reduction. With a four-iteration antenna, a reduction ΔA of 52.39% is obtained

5. Hybrid Modified Koch Fractal Antenna

A new hybrid fractal patch antenna is proposed to miniaturize the size of patch antenna compared with Koch fractal antenna mentioned in section III that suitable for RFID. The fractal iteration starts from a square patch subtracted from 45° rotated half size reference square patch as a zero order then a fractal Koch is applied to the inner of the zero-order reference patch. Two iterations and four indentation angles are simulated for single ring patch, and then a second iteration for double ring with a half is simulated too.

Tables 11 to 13 show the results of the proposed hybrid fractal antenna. These tables present the return loss S_{11} , gain and bandwidth beside the reduction in patch size.

Note that more reduction in area is obtained for this patch antenna compared with previously Koch fractal patch type. A maximum of 42% reduction in *A* for θ = 75° indentation angle for double Koch second iteration fractal patch antenna (see Table 13) compared to maximum reduction in A of 34% obtained when θ = 75° for the third iteration Koch fractal patch antenna (see Table 8).

θ (deg.)	-	30	45	60	75
Δ A (%)	-	30.86	32.10	34.71	37.27
$S_{11}(dB)$	-33.20	-31.44	-36.35	-31.94	-36.54
BW (MHz)	356	264	264	258	271
Gain (dB)	4.04	3.32	3.29	3.21	3.26

Table 11. Simulated parameters of the first iteration single modified Koch fractal patch antenna.

θ(deg.)	-	30	45	60	75
Δ A (%)	-	34.06	35.35	38.38	39.16
$S_{11}(dB)$	-33.20	-46.51	-49.27	-42.27	-30.53
BW (MHz)	356	273	259	259	274
Gain (dB)	4.04	3.26	3.19	3.2	3.24

Table 12. Simulated parameters of the second iteration single modified Koch fractal patch antenna.

		Ø			
θ (deg.)	-	30	45	60	75
Δ A (%)	-	39.86	41.48	41.48	42.24
$S_{11}(dB)$	-33.20	-30.34	-36.42	-23.59	-28.16
BW (MHz)	356	274	275	247	259
Gain (dB)	4.04	3.29	3.26	3.18	3.19

Table 13. Simulated parameters of the second iteration double modified Koch fractal patch antenna.

Figure 18 show the relation between return loss S_{11} and indentation angle for iteration one, two and three of hybrid Koch fractal patch antenna. Again as stated previously in Koch fractal antenna, lower resonance frequency is achieved for large indentation angle.



Figure18. Return loss S_{11} for different values of indentation angles (30°, 45°, 60°, and 75°) for hybrid modified Koch fractal patch antenna. (a) single first iteration (b) single second iteration (c) double second iteration.

6. Relation Comparison of Different Types of Fractal Patches Antenna

Table 14 summarises the results of the above analysis. This table indicates that modified Minkowski fractal patch antenna gives the best reduction in patch area which is 59.80 %.

Antenna Type	Reduction in A (%)		
1. Modified Minkowski	59.80		
2. Bowtie Sierpinski gasket	52.39		
4. Fractal Minkowski	49.02		
5. Hybrid Koch	42.24		
5. Koch	34.06		
6. Sierpinski carpet	20.79		

Table 14. Reduction in enclosed patch area for different fractal patch antennas.

7. Conclusions

Various fractal patch antenna based on aperture coupled feeding have been designed and simulated by CST MWS 2010. New design concepts have been deduced from extensive study of these fractal shapes patch antennas. The ratio of perimeter length of patch to its enclosed area is a main factor for reduction of a given patch geometry. The large of this ratio the more reduction in the size is obtained.

A modified fractal Minkowski fractal patch antenna has been proposed that give most reduction in size among other fractal geometries. Also a hybrid Koch fractal has been introduced to miniaturize the patch antenna.

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