1. Introduction

Microstrip antennas are one of the most widely used types of antennas in the microwave frequency range, and they are often used in the millimeter-wave frequency range. Actually as the demand for high data rates grows and microwave frequency bands become congested, the millimeter-wave spectrum is becoming increasingly attractive for emerging wireless applications. The abundance of bandwidth and large propagation losses at millimeter-wave frequencies makes these bands best-suited for short-range or localized systems that provide broad bandwidth. Automotive radar systems including cruise control, collision avoidance and radiolocation with operation up to 10 GHz have a large market potential in the near future of millimetre wave applications.

One advantage of the microstrip antenna is easy matching, fabrication simplicity and low profile, in the sense that the substrate is fairly thin. If the substrate is thin enough, the antenna actually becomes conformal, meaning that the substrate can be bent to conform to a curved surface. Disadvantages of the microstrip antenna include the fact that it is usually narrowband, with bandwidths of a few percent being typical. Also, the radiation efficiency of the microstrip antenna tends to be lower than some other types of antennas, with efficiencies between 70% and 90% being typical. A microstrip antenna operating in a travelling wave configuration could provide the bandwidth and the efficiencies needed.

Travelling-wave antennas are a class of antennas that use a travelling wave on a guiding structure as the main radiating mechanism. It is well known that antennas with open-ended wires where the current must go to zero (dipoles, monopoles, etc.) can be characterized as standing wave antennas or resonant antennas. The current on these antennas can be written as a sum of waves traveling in opposite directions (waves which travel toward the end of the wire and are reflected in the opposite direction). For example, the current on a dipole of length $l$ is given by:

$$I(z) = I_0 \sin \left[ k \left( \frac{l}{2} - z' \right) \right] - \frac{I_0}{2j} \left[ e^{jk \left( \frac{l}{2} - z' \right)} - e^{-jk \left( \frac{l}{2} - z' \right)} \right]$$

(1)
Traveling wave antennas are characterized by matched terminations (not open circuits) so that the current is defined in terms of waves traveling in only one direction (a complex exponential as opposed to a sine or cosine). A traveling wave antenna can be formed by a single wire transmission line (single wire over ground) which is terminated with a matched load (no reflection). Typically, the length of the transmission line is several wavelengths.

The antenna shown in Fig. 1 above is commonly called a Beverage or wave antenna. This antenna can be analyzed as a rectangular loop, according to image theory. However, the effects of an imperfect ground may be significant and can be included using the reflection coefficient approach. The contribution to the far fields due to the vertical conductors is typically neglected since it is small if $l >> h$. Note that the antenna does not radiate efficiently if the height $h$ is small relative to wavelength. In an alternative technique of analyzing this antenna, the far field produced by a long isolated wire of length $l$ can be determined and the overall far field found using the 2 element array factor. Traveling wave antennas are commonly formed using wire segments with different geometries. Therefore, the antenna far field can be obtained by superposition using the far fields of the individual segments. Thus, the radiation characteristics of a long straight segment of wire carrying a traveling wave type of current are necessary to analyze the typical traveling wave antenna. Traveling-wave antennas are distinguished from other antennas by the presence of a traveling wave along the structure and by the propagation of power in a single direction. Linear wire antennas are the dominant type of traveling-wave antennas.

There are in general two types of traveling-wave antennas [1-2]. The first one is the surface-wave antenna, which is a slow-wave structure, where the phase velocity of the wave is smaller than the velocity of light in free space and the radiation occurs from discontinuities in the structure (typically the feed and the termination regions). The propagation wavenumber of the traveling wave is therefore a real number (ignoring conductors or other losses). Because the wave radiates only at the discontinuities, the radiation pattern physically arises from two equivalent sources, one at the beginning and one at the end of the
structure. This makes it difficult to obtain highly-directive singlebeam radiation patterns. However, moderately directly patterns having a main beam near endfire can be achieved, although with a significant sidelobe level. For these antennas there is an optimum length depending on the desired location of the main beam. Examples include wires in free space or over a ground plane, helixes, dielectric slabs or rods, corrugated conductors, “beverage” antenna, or the V antenna. An independent control of the beam angle and the beam width is not possible.

The second type of the travelling wave antennas are a fast-wave structure as leaky-wave antenna (LWA) where the phase velocity of the wave is greater than the velocity of light in free space. The structure radiates all its power with the fields decaying in the direction of wave travel.

A popular and practical traveling-wave antenna is the Yagi–Uda antenna It uses an arrangement of parasitic elements around the feed element to act as reflectors and directors to produce an endfire beam. The elements are linear dipoles with a folded dipole used as the feed. The mutual coupling between the standing-wave current elements in the antenna is used to produce a traveling-wave unidirectional pattern. Recently has been developed a new simple analytical and technical design of meanderline antenna, taped leaky wave antenna (LWA) and taped composite right/left-handed transmission-line (CRLHTL) LWA. The meanderline antenna is a traveling-wave structure, which enables reduction of the antenna length. It has a periodical array structure of alternative square patterns. With this pattern, the extended wire can be made much longer than the initial antenna (dipole) length, so that the selfresonance can be attained. The resonance frequency is then lower and radiation resistance is higher than that of a dipole of the same length. This in turn implies that the antenna is effectively made small.

2. Leaky wave antennas

In detail this type of wave radiates continuously along its length, and hence the propagation wavenumber $k_z$ is complex, consisting of both a phase and an attenuation constant. Highly-directive beams at an arbitrary specified angle can be achieved with this type of antenna, with a low sidelobe level. The phase constant $\beta$ of the wave controls the beam angle (and this can be varied changing the frequency), while the attenuation constant $\alpha$ controls the beamwidth. The aperture distribution can also be easily tapered to control the sidelobe level or beam shape.

All kinds of open planar transmission lines are predisposed to excite leaky waves. There are two kinds of leaky waves. Surface leaky waves radiate power into the substrate. These waves are in most cases undesirable as they increase losses, cause distortion of the transmitted signal and cross-talk to other parts of the circuit. Space leaky waves radiate power into a space and mostly also into the substrate. These waves can be utilized in leaky wave antennas. Leaky-wave antennas can be divided into two important categories, uniform and periodic, depending on the type of guiding structure. A uniform structure has a cross section that is uniform (constant) along the length of the structure, usually in the form of a waveguide that has been partially opened to allow radiation to occur. The guided wave on the uniform structure is a fast wave, and thus radiates as it propagates.
As said previously leaky-wave antennas form part of the general class of travelling-wave antennas which are a class of antennas that use a travelling wave on a guiding structure as the main radiating mechanism [3], as defined by standard IEEE 145-1993: “An antenna that couples power in small increments per unit length, either continuously or discretely, from a travelling wave structure to free space”.

Leaky-wave antennas are a fast-wave travelling-wave antennas in which the guided wave is a fast wave, meaning a wave that propagates with a phase velocity that is more than the speed of light in free space.

The slow wave travelling antenna does not fundamentally radiate by its nature, and radiation occurs only at discontinuities (typically the feed and the termination regions). The propagation wavenumber of the travelling wave is therefore a real number (ignoring conductors or other losses). Because the wave radiates only at the discontinuities, the radiation pattern physically arises from two equivalent sources, one at the beginning and one at the end of the structure. This makes it difficult to obtain highly-directive singlebeam radiation patterns. However, moderately directly patterns having a main beam near endfire can be achieved, although with a significant sidelobe level. For these antennas there is an optimum length depending on the desired location of the main beam. An independent control of the beam angle and the beam width is not possible. By contrast, the wave on a leaky-wave antenna (LWA) may be a fast wave, with a phase velocity greater than the speed of light. Leakage is caused by asymmetry, introduced in radiating structure transversal section (e.g.: aperture offset, waveguide shape, etc…), feeding modes or a combination of them. In this type of antennas, the power flux leaking from waveguide to free space ($P_{out}$ in Fig. 2 and Fig. 3), introduces a loss inside structure, determining a complex propagation wavenumber $k_z$ [4-5]:

$$k_z = \beta - j\alpha$$  \hspace{1cm} (2)

Where $\alpha$ is the leakage constant and $\beta$ is the propagation constant. The phase constant $\beta$ of the wave controls the beam angle (and this can be varied changing the frequency), while the attenuation constant $\alpha$ controls the beamwidth. Highly-directive beams at an arbitrary specified angle can be achieved with this type of antenna, with a low sidelobe level.
Moreover the aperture distribution can also be easily tapered to control the sidelobe level or beam shape. Leaky-wave antennas can be divided into two important categories, uniform and periodic, depending on the type of guiding structure.

Fig. 3. Example of periodic leaky wave antenna, using a dielectric substrate upon which are placed rods of other material, even metal, in a periodic layout.

A uniform structure has a cross section that is uniform (constant) along the length of the structure, usually in the form of a waveguide that has been partially opened to allow radiation to occur [6]. The guided wave on the uniform structure is a fast wave, and thus radiates as it propagates. A periodic leaky-wave antenna structure is one that consists of a uniform structure that supports a slow (non radiating) wave that has been periodically modulated in some fashion. Since a slow wave radiates at discontinuities, the periodic modulations (discontinuities) cause the wave to radiate continuously along the length of the structure. From a more sophisticated point of view, the periodic modulation creates a guided wave that consists of an infinite number of space harmonics (Floquet modes) [7]. Although the main ($n = 0$) space harmonic is a slow wave, one of the space harmonics (usually the $n = -1$) is designed to be a fast wave, and hence a radiating wave.

3. LWA in waveguide

A typical example of a uniform leaky-wave antenna is a rectangular waveguide with a longitudinal slot. This simple structure illustrates the basic properties common to all uniform leaky-wave antennas. The fundamental $TE_{10}$ waveguide mode is a fast wave, with

$$\beta = \sqrt{k_0^2 + \left(\frac{\pi}{a}\right)^2}$$

lower than $k_0$. As mentioned, the radiation causes the wavenumber $k_z$ of the propagating mode within the open waveguide structure to become complex. By means of an application of the stationary-phase principle, it can be found in fact that [5]:

$$\sin \theta_n \approx \frac{\beta}{k_0} = \frac{c}{v_{ph}}$$

(3)
where \( \theta_m \) is the angle of maximum radiation taken from broadside. As is typical for a uniform LWA, the beam cannot be scanned too close to broadside \( (\theta_m = 0) \), since this corresponds to the cutoff frequency of the waveguide. In addition, the beam cannot be scanned too close to endfire \( (\theta_m = 90) \) since this requires operation at frequencies significantly above cutoff, where higher-order modes is in a bound condition or can propagate, at least for an air-filled waveguide. Scanning is limited to the forward quadrant only \( (0 < \theta_m < \frac{\pi}{2}) \) for a wave travelling in the positive z direction.

Fig. 4. Slotted guide (patented by W. W. Hansen in 1940).

This one-dimensional (1D) leaky-wave aperture distribution (see Fig. 4), results in a “fan beam” having a narrow beam in the x-z plane (H plane), and a broad beam in the cross-plane. Unlike the slow-wave structure, a very narrow beam can be created at any angle by choosing a sufficiently small value of \( \alpha \). From diffraction theory, a simple formula for the beam width, measured between half power points (3dB), is:

\[
\Delta \theta \approx \frac{\text{const}}{\frac{L}{\lambda_0} \cos \theta_m}
\]  

(4)

“const” is a parameter which is influenced by the type of aperture and illumination; for example, if at the aperture there’s a constant field, const = 0.88 and, if the structure is uniform, const = 0.91. As a rule of thumb, supposing:

\[
\Delta \theta \approx \frac{1}{\frac{L}{\lambda_0} \cos \theta_m}
\]  

(5)

a good approximation of beamwidth is yielded, where \( L \) is the length of the leaky-wave antenna, and \( \Delta \theta \) is expressed in radians. For 90% of the power radiated it can be assumed:

\[
\frac{L}{\lambda_0} \approx \frac{0.18}{\frac{\alpha}{k_0}}
\]
If the antenna has a constant attenuation throughout its length $\alpha_z(z) = \alpha_z$ results:

\[ P(z) = P(0)e^{-2\alpha_z} \]

Therefore, being $L$ the length of antenna, if a perfectly matched load is connected at the end of it, it’s possible to express antenna efficiency as:

\[ \eta_{rad} = \frac{P(0) - P(L)}{P(0)} = 1 - \frac{P(L)}{P(0)} = 1 - e^{-2\alpha_z L} \]  \hspace{1cm} (6)

Rearranging:

\[ L = \frac{\ln(1 - \eta_{rad})}{2\alpha_z} \]  \hspace{1cm} (7)

For most application, to gain a 90% efficiency, means that the antenna length is within $10\lambda_0 \div 100\lambda_0$ interval.

Fixing the antenna efficiency, using (7), makes possible to express attenuation constant in terms of antenna length, and vice versa. Using antenna efficiencies greater than 90%-95% is not advisable; in fact, supposing constant antenna cross section and, as a consequence, fixed leakage constant, the necessary length $L$ grows exactly as $\alpha_z L$, which increases asymptotically, as shown in Fig 5. If we want a 100% efficiency ($\eta_{rad} = 1$) from (6):

\[ P(L) = 0 \Rightarrow e^{-2\alpha_z L} = 0 \Rightarrow L = \infty \]

we note that is necessary an infinite antenna length.

Substituing (7) in (5), being $\lambda_0 = 2\pi / k_0$ :

\[ \Delta \theta \approx \left( \frac{-4\pi}{\ln(1 - \eta_{rad}) \cos \theta_m} \right) \frac{\alpha_z}{k_0} \]

Because $\cos \theta_m = \sqrt{1 - \sin^2 \theta_m}$, considering (7)

\[ \Delta \theta \approx \left( \frac{-4\pi}{\ln(1 - \eta_{rad}) \sqrt{1 - \left( \frac{\beta_z}{k_0} \right)^2}} \right) \frac{\alpha_z}{k_0} \]  \hspace{1cm} (8)

Since $k_0^2 = k_x^2 + k_z^2$ and having supposed the attenuation constant much smaller than the phase constant, $k_z \approx \beta_z$, getting:
\[
\Delta \theta \approx \begin{cases} 
\frac{-4\pi}{\ln(1-\eta_{rad})} \frac{\alpha_z}{k_c} \frac{k_c}{k_0} 
\end{cases} 
\]  
(9)

where \( k_c \) is the transverse propagation constant. Alternatively, considering (7):
\[
\Delta \theta \approx \frac{2\pi}{L \cdot k_c} 
\]

Using waveguide theory notation, supposing \( \lambda_c \) the cut-off wavelength:
\[
\Delta \theta \approx \frac{\lambda_c}{L} 
\]  
(10)

(3) and (10), provided the approximations used to be valid, are a valid tool for describing the main parameters of radiated beam.

Fig. 5. Variation of \( \alpha_z L \) versus antenna efficiency.

Radiation properties of leaky wave antennas are well described by dispersion diagrams. In fact since leakage occurs over the length of the slit in the waveguiding structure, the whole length constitutes the antenna’s effective aperture unless the leakage rate is so great that the power has effectively leaked away before reaching the end of the slit. A large attenuation constant implies a short effective aperture, so that the radiated beam has a large beamwidth. Conversely, a low value of \( \alpha \) results in a long effective aperture and a narrow beam, provided the physical aperture is sufficiently long.
Moreover since power is radiated continuously along the length, the aperture field of a leakywave antenna with strictly uniform geometry has an exponential decay (usually slow), so that the sidelobe behaviour is poor. The presence of the sidelobes is essentially due to the fact that the structure is finite along $z$.

When we change the cross-sectional geometry of the guiding structure to modify the value of $\alpha$ at some point $z$, however, it is likely that the value of $\beta$ at that point is also modified slightly. However, since $\beta$ must not be changed, the geometry must be further altered to restore the value of $\beta$, thereby changing $\alpha$ somewhat as well.

In practice, this difficulty may require a two-step process. The practice is then to vary the value of $\alpha$ slowly along the length in a specified way while maintaining $\beta$ constant (that is the angle of maximum radiation), so as to adjust the amplitude of the aperture distribution to yield the desired sidelobe performance.

**Radiation modes**

Let us consider a generic plane wave, whose propagation vector belongs to plane $(y-z)$, directed towards a dielectric film grounded on a perfect electric conductor (PEC) parallel to plane $(x-z)$, as shown in Fig. 6 [8-9].

![Fig. 6. Incident wave on a grounded dielectric film, whose thickness is t.](image)

If the incident wave polarization is linear and parallel to the $x$ axis, since both reflection and refraction occur:

\[
\begin{align*}
E_{x_0} &= Ae^{-jk_0(y-t)} + Ce^{jk_0(y-t)} \quad y \geq t \\
E_{x_0} &= B\cos(k_{y_0}y) + D\sin(k_{y_0}y) \quad t \geq y \geq 0
\end{align*}
\]

Being the tangent components of electric field null on a PEC surface, $B = 0$:

\[
\begin{align*}
E_{x_0} &= Ae^{-jk_0(y-t)} + Ce^{jk_0(y-t)} \quad y \geq t \\
E_{x_0} &= D\sin(k_{y_0}y) \quad t \geq y \geq 0
\end{align*}
\]

One constant can be expressed by the remaining two, as soon as continuity of tangent components of electric field is considered in $y = t$. First equation of (11) contains an exponential term which, diverging for $y \to \infty$, violates the radiation condition at infinite distance. Therefore, $C \neq 0$ only near plane $y = t$, at the incidence point. $k_z$ can assume any
value from 0 to \( k_0 \) (i.e.: radiating modes); above it, only discrete values of \( k_z \) exist, identifying the associated guided modes. Since separability condition must be satisfied, in air:

\[
k_0^2 = \omega^2 \mu_0 \varepsilon_0 = k_{y_0}^2 + k_z^2 \quad \text{where} \quad k_0 \in \mathbb{R}
\]  

(12)

For every \( k_z \), it’s now possible calculate \( k_{y_0} \). In fact, considering only positive solutions:

\[
k_{y_0} = \sqrt{k_0^2 - k_z^2}
\]

Obtaining:

<table>
<thead>
<tr>
<th>Mode</th>
<th>Wave numbers</th>
</tr>
</thead>
<tbody>
<tr>
<td>Guided</td>
<td>( k_z &gt; k_0 )</td>
</tr>
<tr>
<td>Radiating</td>
<td>( k_0 &gt; k_z &gt; 0 )</td>
</tr>
<tr>
<td>Evanescent</td>
<td>( 0 &gt; k_z &gt; -j\infty )</td>
</tr>
</tbody>
</table>

Table 1. Wave modes identified by \( k_z \).

Thus, a spectral representation of electromagnetic field near the air-dielectric interface, must contain all values of \( k_{y_0} \), from 0 to \( \infty \): the associated integral is complex and slowly convergent. Alternatively, a description, which uses leaky waves and guided modes, both discrete, can well approximate such field.

It’s been observed that it’s often enough a single leaky wave to obtain a good far field description.

Letting \( k_y = k_{y_0} \), from (2) and (12), in general:

\[
\begin{cases}
  k_0 = \beta_y^2 + \beta_z^2 - \alpha_y^2 - \alpha_z^2 \\
  0 = \beta_y \alpha_y + \beta_z \alpha_z
\end{cases}
\]

alternatively

\[
\begin{cases}
  k_0^2 = |\beta|^2 \cdot |\alpha|^2 \\
  0 = \beta \cdot \alpha
\end{cases}
\]

(13)

Having defined the attenuation and the phase vectors, respectively, as:

\[
\alpha = \alpha_y y_0 + \alpha_z z_0
\]

\[
\beta = \beta_y y_0 + \beta_z z_0
\]
Being \( k_0 \in \mathbb{R} \), from (9) \( |\beta| \neq 0 \), and \( |\beta| > |\alpha| \)

Considering waves propagating in the positive direction of z axis, \( \beta_z > 0 \) and supposing no losses in z direction, \( \alpha_z = 0 \), from (13):

\[ 0 = \beta \cdot \alpha \]

Leaving out \( \beta_y, \alpha_y = 0 \), two situations can occur: \( \alpha_y = 0 \) and \( \beta_y = 0 \). If \( \alpha_y = 0 \), equations describe a uniform plane wave passing the air-dielectric interface. On the other hand, if \( \beta_y = 0 \), two types of superficial waves exist, depending on \( \alpha_y = 0 \) sign:

<table>
<thead>
<tr>
<th>( \alpha_y &gt; 0 )</th>
<th>Confined superficial wave</th>
</tr>
</thead>
</table>

<table>
<thead>
<tr>
<th>( \alpha_y &lt; 0 )</th>
<th>Improper superficial wave</th>
</tr>
</thead>
</table>

Fig. 7. Superficial waves at air-dielectric interface when \( \beta_y = 0 \).

Because confined superficial waves amplitude decreases exponentially as distance from interface increases, when \( y \) is greater than 10 times radiation wavelength, electromagnetic field practically ceases to exist. Improper superficial wave, whose amplitude increases exponentially as distance from interface increases, are not physically possible because they violate the infinite radiation condition.

Removing the hypothesis \( \alpha_z = 0 \), both \( \alpha_y \neq 0 \), and \( \beta_y \neq 0 \).

<table>
<thead>
<tr>
<th>Losses in Dielectric</th>
</tr>
</thead>
</table>

<table>
<thead>
<tr>
<th>Leaky Wave</th>
</tr>
</thead>
</table>

Fig. 8. General mutual \( \beta \) and \( \alpha \) configurations depicting condition \( 0 = \beta \cdot \alpha \).

When losses in dielectric occur, \( \beta \) must point towards the inner part of dielectric to compensate such losses (see Fig.8). In the other configuration, when \( \beta \) points upwards, even though a non-physical solution is described, the associated wave is useful to describe electromagnetic field near air-dielectric interface.

4. LWA in microstrip

Microstrip antenna technology has been the most rapidly developing topic in antennas during the last twenty years [10]. Microstrip is an open structure that consists of a very thin metallic strip or patch of a width, \( w \), separated from a ground plate by a dielectric sheet.
called substrate (Fig. 9). The thickness of the conductor, $t$, is much less than a wavelength, and may be of various shapes. The height of the substrate, $h$, is usually very thin compared to the wavelength ($0.003 \lambda \leq h \leq 0.05 \lambda$) [11]. The substrate is designed to have a known relative permittivity, $\varepsilon_r$, that is homogeneous within specified temperature limits.

![Geometry of a microstrip transmission line.](image)

Fig. 9. Geometry of a microstrip transmission line.

The antenna can be excited directly by a microstrip line, by a coaxial cable, or a combination of the two. The antenna can also be fed from a microstrip line without direct contact through electromagnetic coupling. Feeding by electromagnetic coupling through an aperture in the ground plane tends to improve bandwidth. To maximize efficiency, the impedance of the feed must be matched to the input impedance of the antenna. There are a variety of stubs, shunts, and other devices used for matching. The major disadvantages of microstrip are lower gain, very narrow bandwidth, low efficiency and low power handling ability. In addition, antennas made with microstrip typically have poor polarization purity and poor scan performance [12].

Operating above the cutoff frequency, the field lines of microstrip extend throughout the substrate as well as into the free space region above the substrate, as seen in Fig. 10. The phase velocity of the field in the free space surrounding the structure is the speed of light, $c$, and the phase velocity of the field in the substrate is given by Equation (14)

$$v_p = \frac{c}{\sqrt{\varepsilon_r}}$$

This difference in phase velocity at the interface between the substrate and free space makes the TEM mode impossible. Instead, the fundamental mode for microstrip is a quasi-TEM mode, in which both the electric and magnetic fields have a component in the direction of propagation. Likewise, a higher order mode in microstrip is not purely TE or TM, but a hybrid combination of the two. The $n$th higher order mode is termed the $TE_n$ mode. The fundamental mode of microstrip, as seen in Fig. 10, does not radiate since the fields produced do not decouple from the structure. If the fundamental mode is not allowed to propagate, the next higher order mode will dominate. Fig. 11 shows the fields due to the first higher order mode, $TE_{10}$. A phase reversal, or null, appears along the centerline, allowing the fields to decouple and radiate.
Recently, there has been significant interest in the microstrip leaky-wave antenna which utilizes a higher order radiative microstrip mode. Since Menzel in 1979, published the first account of a travelling wave microstrip antenna that used a higher order mode to produce leaky waves [13], many microstrip leaky-wave antenna designs incorporating various modifications have been investigated. The design of Menzel antenna [13], can be seen in Fig. 12. Menzel’s antenna uses seven slots cut from the conductor along the centerline to suppress the fundamental mode allowing leaky wave radiation via the first higher order mode. Menzel’s antenna has been analyzed by a host of researchers over the past 25 years [14] and its performance is known and reproducible. Instead of transverse slots, we can use a metal wall down the centerline of the antenna to block the fundamental mode. Symmetry along this metal wall invites the application of image theory. One entire side of the antenna
is now an image of the other side, making it redundant and unneeded. This property allows to design the resulting antenna half of the width of Menzel’s antenna, as shown in Fig. 13.

As mentioned the microstrip structures do not radiate for the fundamental mode, therefore, a higher order mode must be excited to produce leaky waves. This method of producing radiation by exciting higher order modes in a transmission line has been documented since the 1950's [6]. By the 1970’s, rectangular waveguides, circular waveguides, and coaxial cables were in use as leaky traveling wave antennas. However, until Menzel, the jump to microstrip had not been made. By looking at a cross section of microstrip excited in the fundamental mode, the E field is strongest in the center and tapers off to zero at the sides, as depicted in Fig 10. If the electric field down the centerline is suppressed, the fundamental mode will be prohibited, forcing the energy to propagate at the next higher mode, $TE_{10}$. As seen in Fig. 11, $TE_{10}$ mode causes E to be strongest at the edges. Menzel attempted to force the $TE_{10}$ mode using several means. Feeding two equal magnitude waves $180^\circ$ out of phase with a “T” or “Y” feed produced $TE_{10}$ as desired, but did not fully eliminate the fundamental mode. Easier to produce and providing an even better response was given using transverse slots down the centerline (Fig. 12). The multiple feeds were not necessary to produce the $TE_{10}$ mode when the fundamental mode was suppressed. Menzel demonstrated that the beam angle can be predictively steered by input frequency if the electrical length of the antenna is at least $3\lambda$. If the length is less than $3\lambda$, too little of the incident wave is being radiated and a resonance standing wave pattern is forcing the beam toward broadside. Qualitative analysis shows that the beamwidth of Menzel’s antenna is not frequency dependent, however, it is inversely related to length. The 3 dB beamwidth approaches $10^\circ$ for electrical length of over $6\lambda$ and approaches nearly $90^\circ$ for fractions of a wavelength. Menzel’s gain varied from 7 dB for $l = 0.2\lambda$ to 14 dB for $l = 4\lambda$. 7 dB is comparable to a similar sized resonant antenna. An antenna longer than $l = 4\lambda$ would have an even higher gain as the radiation aperture increases. Lee notes that Menzel assumed that his antenna should radiate simply because the phase constant due to his operating frequency was less than $k_0$ [15]. If Menzel had considered the complex propagation constant, he would have realized that his antenna was operating in a leaky regime. The length would need to be roughly 220 mm, or more than twice as long as his design, to
radiate at 90% efficiency. Radiation patterns in Menzel’s paper clearly show the presence of a large backlobe due to the reflected traveling wave.

Now this class of printed antennas that is particularly well suited for operation at mm-wave frequencies, alleviate some of the problems associated with resonant antennas since they provide higher gain, broader bandwidth performance, and frequency scanning capabilities. These microwave and millimeter leaky wave antennas, have the same properties of the waveguide leaky wave antennas described previously. In addition, when opening a waveguide to free space, a discrete spectrum is not enough to express an arbitrary solution [16].

In fact, when considering a closed region, all characteristic solutions, individuated by the associated eigenvalues, constitute a complete and orthogonal set of modes, whose linear combination can express any field satisfying boundary conditions. As soon as the region is not perfectly bounded, an arbitrary field solution cannot be expressed only using discrete eigenmodes but, generally, a continuous spectrum of modes, which don’t necessarily have finite energy (e.g.: plane waves), must be considered, too.

Fortunately, for leaky wave antennas, an approximation that uses particular waves, called leaky, can be used instead of the continuous spectrum. Moreover, leaky waves are well described by dispersion constants (i.e.: leakage and phase constants) that strongly affect the radiated beam width and elevation.

5. Dispersion curves, spectral-gap

Dispersion curves, describing how attenuation and phase vectors, solutions of dispersion equation (12), evolve, are a valid tool to study leaky waves.

As discussed previously, the radiation mechanism of higher order modes on microstrip LWA is attributed to a traveling wave instead of the standing wave as in patch antennas and above cutoff frequency, where the phase constant equals the attenuation constant \( \alpha_c = \beta_c \), it is possible to observe three different range of propagation: bound wave, surface wave and leaky wave [15]. At low frequency, below the cutoff frequency, we have the reactive region due to evanescent property of LWA.

From (3) we can observe that the leaky mode leaks away in the form of space wave when \( \beta < K_0 \), therefore we can define the radiation leaky region from the cutoff frequency to the frequency at which the phase constant equals the free-space wavenumber \( \beta = K_0 \). For \( \beta > K_s \) we have the bound mode region and for \( K_0 < \beta < K_s \), exists a narrow frequency range \( K_s < \frac{1}{\sqrt{\epsilon_r}} \), in which we can have surface-wave leakage, where \( K_s \) is the surface wavenumber.

Moreover the transition region between surface wave leakage and space wave leakage including a small range in frequency for which the solution is non-physical, and it therefore cannot be seen. For this reason, the transition region is called a spectral gap. Such a spectral gap occurs commonly (but not always) at such transitions in printed circuits, but it also occurs in almost all situations for which there is a change from a bound mode to a leaky
Fig. 14. The typical normalized attenuation constant, $\frac{\alpha}{k_0}$, and phase constant $\frac{\beta}{k_0}$, in the direction of propagation of the first higher order mode, $TE_{10}$. There are four frequency regions associated with propagation regimes: Reactive, Leaky, Surface, and Bound.

mode, or vice versa. For example, a spectral gap will appear when the beam approaches endfire in all leaky-wave antennas whose cross section is partly loaded with dielectric material. It is necessary to employ a greatly enlarged scale, on which the dispersion plot is sketched qualitatively. The transition region itself is divided into two distinct frequency ranges, one from point A to point B and the second from point B to point C. Before point B, a leaky wave occurs. As soon as frequency reaches $f_1$ (point B), an improper superficial wave is solution of dispersion equation [9]. Because, both $\alpha_z$ and $\beta_z$ cannot increase with frequency between $f_1$ and $f_2$, their trend will change until point C, from which a confined superficial wave is an acceptable solution for increasing values of frequency.

To depict normalized constants behaviour around the spectral-gap, it’s necessary a very precise numerical method since, leaving out particular structures, its width ($Af$) is very small compared to working frequencies.

The dispersion characteristics for microstrip has been investigated by a number of authors using different full wave methods and evaluating different regimes of the dispersion characteristic.

The spectral domain analysis has proven to be one of the most efficient and fruitful techniques to study the dispersion characteristics of printed circuit lines [17]. As is explained in literature, the Galerkin method in conjunction with Parseval theorem can be used to pose the dispersion relation of an infinite printed circuit line as the zeros of the following equation:
\[ F(k_z) = \int_{C_x} \tilde{G}_{zz}(k_x, k_z) \tilde{T}(k_x) dk_x = 0 \]  

(15)

where \( \tilde{T}(k_x) \) is the Fourier transform of the basis function \( T(k_x) \) used to expand the longitudinal current density on the strip conductor as

\[ J_{sz}(x, z) = T(x)e^{-jk_zz} \]

The term \( \tilde{G}_{zz}(k_x, k_z, \omega) \) is the \( zz \) component of the spectral dyadic Green’s function, and \( C_x \) is an appropriate integration path in the complex \( k_x \) plane to allow for an inverse Fourier transform non uniformly convergent function. The spectral dyadic Green’s function has the following singularities in the complex \( k_x \) plane: branch point, a finite set of poles on the proper sheet and an infinite set of poles on the improper sheet. For a fixed frequency, the function \( F(k_z) \) is not uniquely defined because of the many possible different \( C_x \) integration paths that can be used to carry out the integral (15) [18].

Fig. 15. Transition region between leaky wave and confined superficial wave showing the spectral-gap occurring \( f_1 \) and \( f_2 \).

The different \( C_x \) paths come from the different singularities of the spectral dyadic Green’s function, that can be detoured around. For complex leaky mode solution, an integration path detouring around only the proper poles of the spectral dyadic Green’s function is associated with an surface-wave leaky mode solution. If the path also detours around the branch points, passing trough the branch cuts and, therefore, lying partly on the lower Riemann sheet, the path will be associated with an space-wave leaky mode solution (see Fig. 16). This procedure, is not trivial. We shown in the next chapters how it is possible to extract the propagation constant of a microstrip LWA more simply using an FDTD code with UPML boundary condition, who directly solves the fields in the time domain using Maxwell’s equations and with which the analysis is easy modifying the geometries of the LWAs. The results are in a good agreement with transverse resonance approximation (a full wave method) derived by Kuestner [19].
Fig. 16. Possible integration paths $C$. The three different are denoted as $C_0$ for the real-axis path (bound mode solution), $C_1$ for the path that detours around only the spectral dyadic Green's function poles (surface-wave leaky modes solution), and $C_2$ for the path that also passes around the branch points (space-wave leaky modes solution).

6. Tapered leaky wave antennas

Nowadays, some applications especially with regard to communication applications like the indoor wireless LAN (WLAN) actually are increasing the use of millimeterwave antennas like leaky-wave antennas (LWA), suited for more purpose. In detail, the transmitting/receiving antennas with relatively broadbeam and broadband can be obtained from the curved and tapered leakywave structures. In fact, the microstrips (LWA), are very popular and widely used in applications thanks to their advantages of low-profile, easy matching, narrow beamwidth, fabrication simplicity, and frequency/electrical scanning capability. Is well know that the radiation mechanism of the higher order mode on microstrip LWAs is attributed to a traveling wave instead of the standing wave as in patch antennas. Moreover the symmetry of the structure along this physical grounding structure, thanks to the image theory, allows to design only half of an antenna with the same property of one in its entirety, and reducing up to 60% the antenna’s dimensions. Using this tapered antenna we can obtained a quasi linear variations of the phase normalized constant and than a quasi linear variations of the its radiation angle. Moreover the profile of the longitudinal edges of the LWA, was designed, by means of the reciprocal slope of the cutoff curve, symmetrically to the centerline of the antenna, allows a liner started of leaky region.

Nevertheless the variation of the cross section of the antenna, allowing a non-parallel emitted rays, such as happens in a non-tapered LWA. In fact, using the alternative geometrical optics approach proposed in the tapering of the LWA, for a fixed frequency, involves the variation of the phase constant $\beta$ and the attenuation constant $\alpha$, obtained as a cut plane of 3D dispersion surface plot varying width and frequency. We can be determined a corresponding beam radiation interval with respect to endfire direction. As mentioned previously, for a tapered antenna with a curve profile (square root law profile) the radiation angle in the leaky regions, vary quasi linearly whit the longitudinal dimension, so it is possible to calculate the radiation angle of the antenna as a average of the phase constant using the simple formula.
Alternatively using the geometrical optics approach it is easy to determine the closed formula to predict the angle of main beam of a tapered LWA.

7. Design of tapered LWA

The radiation mechanism of the higher order mode on microstrip LWAs is attributed to a traveling wave instead of the standing wave as in patch antennas [13,20].

We can explain the character of microstrip LWAs through the complex propagation constant
\[ k = \beta - j\alpha \], where \( \beta \) is the phase constant of the first higher mode, and \( \alpha \) is the leakage constant. Above the cutoff frequency, where the phase constant equals the attenuation constant \( (\alpha = \beta) \), it is possible to observe three different propagation regions: bound wave, surface wave and leaky wave.

The main-beam radiation angle of LWA can be approximated by:

\[
\theta = \cos^{-1}\left( \frac{\beta}{K_0} \right)
\]

where \( \theta \) is the angle measured from the endfire direction and \( K_0 \) is the free space wavenumber. According to (16) we can observe that the leaky mode leaks away in the form of space wave when \( \beta < K_0 \), therefore we can define the radiation leaky region, from the cutoff frequency to the frequency at which the phase constant equals the free-space wavenumber \( (\beta = K_0) \). An example of tapered LWA was proposed in [21-22], using an appropriate curve design to taper LWA.

In fact through the dispersion characteristic equation, evaluated with FDTD code, we can obtain the radiation region of the leaky waves indicated in the more useful way for the design of our antenna:

\[
\frac{c}{2w_{off}\sqrt{\varepsilon_r}} = f_c < f < \frac{f_c\sqrt{\varepsilon_r}}{\sqrt{\varepsilon_r} - 1}.
\]

From equation (17) we can observe that the cutoff frequency increases when the width of the antenna decrease, shift toward high frequencies, the beginning of the radiation region as shown in Fig. 17. 1.

Therefore it is possible to design a multisection microstrip antenna [as Type I antenna in Fig. 17.a], in which each section able to radiate at a desired frequency range, can be superimposed, obtaining an antenna with the bandwidth more than an uniform microstrip antenna. In this way every infinitesimal section of the multisection LWA obtained overlapping different section should be into bound region, radiation region or reactive region, permitting the power, to uniformly radiated at different frequencies.

Using the same start width and substrate of Menzel travelling microstrip antenna (TMA) [13], and total length of 120 mm., we have started the iterative procedure mentioned in [23] to obtain the number, the width and the length of each microstrip section. From Menzel
TMA width, we have calculated the $f_{\text{START}}$ (onset cutoff frequency) of the curve tapered LWA, than, choosing the survival power ratio ($\tau = e^{-2\alpha \ell}$) opportune, at the end of the first section, we have obtained the length of this section. The cutoff frequency of subsequent section ($f_i$), was determined by FDTD code, while the length of this section was determined, repeating the process described previously. This iterative procedure was repeated, until the upper cutoff frequency of the last microstrip section.

![Graph showing cutoff frequency of multisection microstrip LWA](image)

Fig. 17.1 Cutoff frequency of multisection microstrip LWA.

The presence of ripples in return loss curve and the presence of spurious sidelobes shows the impedance mismatch and discontinuity effect of this multisection LWA that reduce the bandwidth. A simple way to reducing these effects is to design a tapered antenna in which the begin and the end respectively of the first and the last sections are linearly connected together (as the Type II antenna in Fig. 17.a).

Alternatively the ours idea was to design a LWA using a physical grounding structure along the length of the antenna, with the same contour of the cutoff phase constant or attenuation constant curve ($\alpha_c = \beta_c$), obtained varying the frequency (the cutoff frequency $f_c$ is the frequency at which $\alpha_c = \beta_c$), for different width and length of each microstrip section as shown in Fig. 17.1, employing the following simple equation (18):

$$\beta_c = c_1 f^2 + c_2 f + c_3$$

(18)

obtained from linear polynomials interpolation, where $c_1 = 0.0016$, $c_2 = 0.03$, $c_3 = -15.56$.

The antenna layout (as the Type III antenna in Fig. 17.a), was optimized through an 3D electromagnetic simulator, and the return loss and the radiation pattern was compared with Type I antenna and Type II antenna.
8. Simulation results

An asymmetrical planar 50 Ω feeding line was used to excite the first higher-order mode while a metal wall down the centerline connecting the conductor strip and the ground plate was used to suppress the dominant mode for Type I - III. The chosen substrate had a dielectric constant of 2.32 and a thickness of 0.787 mm, while the total length of the leaky wave antenna was chosen to be 120 mm.

The leaky multisection tapered antenna Type I was open-circuited, with a 15 mm start width, and 8.9 mm of final width obtained according to [23]. For LWA layout Type I, we used four microstrip steps, for layout Type II we tapered the steps linearly, while the curve contour of the LWA layout Type III, was designed through equation (18).

Fig. 17.b shows the simulated return loss of three layouts. We can see that the return loss (S11) of Type I is below -5 dB from 6 to 10.3 GHz, but only three short-range frequencies are below -10 dB. S11 of Type II is below -5 dB from 6.1 to 9.1 GHz, and below -10 dB from 6.8 to 8.6 GHz. At last, S11 of Type III is below -5 dB from 6.8 to 11.8 GHz, and below -10 dB from 8.0 to 11.2 GHz. In Fig.17.c a are shows the mainlobe direction at 9.5 GHz for the different Type I to Type III. We can see a reduction of sidelobe and only few degrees of mainlobe variation between Type I to Type III. Moreover, in Fig. 18 is shown the variation of mainlobe of antenna Type III, for different frequency, while in Fig. 19 is shown the trend of gain versus frequency of the same antenna. It is clear that, the peak power gain is more than 12 dBi, which is almost 3 dBi higher than uniform LWAs.

Finally the simulated VSWR is less than 2 between 8.01 and 11.17 GHz (33%), yielding an interesting relative bandwidth of 1.39:1, as shown in Fig. 20, compared with uniform microstrip LWAs (20% for VSWR < 2) as mentioned in [24].
These results indicate a high performance of Type III LWA: high efficiency excitation of the leaky mode, increases of the bandwidth, improves the return loss and reduction of 19% of metallic surface with respect to uniform LWA. Moreover, these results are in a good agreement with the experimental results of return loss and radiation pattern of a prototype made using a RT/Duroid 5880 substrate with thickness of 0.787 mm and relative dielectric constant of 2.32, as shown in Fig.21 and Fig.22.
Fig. 17c. Radiation patterns of Electric field (H plane) of Type I-III, LWA at 9.5 GHZ.

Fig. 18. a) Simulated radiation patterns of E field of LWA Type III for different frequency. b) 3-D radiation pattern of Electric field.

Fig. 19. The gain versus frequency of the LWA Type III.
Fig. 20. Simulated VSWR of LWA Type III.

Fig. 21. A prototype of tapered LWA Type III with holes made in the centerline of the antenna.

Fig. 22. a) Measurement set-up of LWA Type III. b) Experimental and simulated return loss of LWA Type III.
Moreover the use of a physical grounding structure along the length of the antenna, as suggested in [21-22], allows the suppression of the dominant mode (the bound mode), the adoption of a simple feeding, and due to the image theory, it is also possible to design only half LWA (see Fig. 23) with the same property of one entire, as shown in Fig. 24 and in Fig. 25, reducing up to 60% the antenna’s dimensions compared to uniform LWAs [24].

Fig. 23. A prototype of half tapered LWA.

Fig. 24. Measured return loss of full and half Leaky Wave Antennas

Fig. 25. The measured and simulated radiation patterns of E field of half tapered LWA at 8 GHz.
9. Focusing-diverging property

As described in [21-22], the profile of the longitudinal edges of the LWA, was designed, by means of the reciprocal slope of the cutoff curve, symmetrically to the centerline of the antenna, allows a liner started of leaky region. Using this tapered antenna we can obtained a quasi linear variations of the phase normalized constant and than a quasi linear variations of the its radiation angle as we can see in Fig. 26 and in Fig. 27. Nevertheless the variation of the cross section of the antenna, allowing a non-parallel emitted rays, such as happens in a non-tapered LWA (see Fig. 28). In fact, as was described in the alternative geometrical optics approach proposed in [24] the tapering of the LWA, for a fixed frequency, involves the variation of the phase constant $\beta$ and the attenuation constant $\alpha$, as shown in Fig. 29, obtained as a cut plane of 3D dispersion surface plot varying width and frequency (see Fig. 30).

![Graph](image1)

Fig. 26. The variation of the main beam radiation angle versus length of the antenna, at $f=8$ GHz, for linear, square and square root profile of the LWA.

![Graph](image2)

Fig. 27. The variation of the phase constant versus length of the antenna, at $f=8$ GHz, for linear, square and square root profile of the LWA.
From (16) can be determined in the leaky regions of the antenna, a corresponding beam radiation interval \([\theta_{\text{min}}, \theta_{\text{max}}]\), with respect to endfire direction.

As mentioned previously, for a tapered antenna with a curve profile (square root law profile) the radiation angle in the leaky regions, vary quasi linearly with the longitudinal dimension, so it is possible to calculate the radiation angle of the antenna as an average of the phase constant using the simple equation (19).

\[
\theta_m = \sin^{-1}\left(-\frac{1}{K_0 L} \int_0^L \beta(z) dz\right)
\]  

(19)

Alternatively using the geometrical optics it is easy to determine the closed formula to predict the angle of main beam of a tapered LWA. Through simple mathematical passages, the main beam angle \(\theta_m\) can be obtained by the equation (20).

\[
\theta_m = \sin^{-1}\left(\frac{A \sin \theta_{\text{min}}}{2 \sqrt{(2 A \sin \theta_{\text{min}})^2 + (L + 2C \cos \theta_{\text{max}})^2}}\right)
\]

(20)

Where \(A\) and \(C\) are respectively the distance between real focus \(F\) and the beginning and the end of the length of the antenna \(L\). Therefore, if we know the begin width and the end width of the antenna, from the curves of normalized phase and attenuation constant at fixed frequency, we can determine the beam radiation range from (16), and the main beam angle through (20).

\[\text{Fig. 28. The ray optical model for a tapered Leaky Wave antenna.}\]

Furthermore this focusing phenomena of a tapered LWA can determine a wide-beam pattern in a beam radiation range which is evident when the antenna length is increased \((L \approx 50\lambda_0)\) [25].
To obtain a broad beam pattern without the use of a longer LWA, we can bend a tapered LWA (see Fig. 31), leading the electromagnetic waves to diverge. This, increases the beam of the radiation pattern and reduce furthermore the back lobes as we can see compared the curves of Fig. 32. Finally in Fig. 33 is shown the measured return loss of half bend LWA Type III.

![Graph of normalized phase and attenuation constants versus the width](image1)

**Fig. 29.** The curve of normalized phase and attenuation constants versus the width, at 8 GHz for the LWA with the angular range $[28^\circ, 76^\circ]$. The leaky region start from 10.8 mm. (cutoff frequency).

![Graph of 3D normalized phase constant and attenuation constant](image2)

**Fig. 30.** The 3D normalized phase constant and attenuation constant of tapered LWA versus frequency and width.
Fig. 31. a) Layout of a bend tapered LWA. b) A prototype of bend half LWA Type III made using Roger 5880 RT/Duroid.

Fig. 32. a) The radiation patterns of E field of tapered LWA at f= 8 GHz. b) The radiation patterns of E field of bend tapered LWA at f= 8 GHz.
10. Tapered composite right/left-handed transmission-line (CRLH-TL) leaky-wave antennas (LWAs)

Recently composite right/left-handed (CRLH) leaky-wave antennas (LWAs) have been shown as one of the applications of the CRLH transmission line (TL) metamaterials thanks to their advantages of fabrication simplicity and frequency/electrically scanning capability without any complex feeding network. Nevertheless the fixed geometrical size of a unit cell of the CRLH-TL Leaky-wave antennas, prevents the possibility to improve the antenna bandwidth “tapering” the geometrical size of unit cell.

It is well known as a composite right/left-handed transmission-line (CRLH-TL) metamaterials, used for the leaky-wave antennas (LWAs) allow to obtain a superior frequency scanning ability than its conventional counterpart [26-27]. The leaky-wave antennas possess the advantages of low-profile, easy matching, fabrication simplicity, and frequency/electrically scanning capability without any complex feeding network.

However, the conventional leaky-wave antennas suffer from major limitations in their scanning capabilities. In fact the radiation pattern is restricted to strictly positive $\theta$ for uniform configurations, or to a discontinuous range of negative or positive $\theta$ excluding broadside direction, for periodic configurations. The CRLH LWAs have essentially suppressed these limitations, being able to scans the entire space from $\theta = -90^\circ$ to $\theta = +90^\circ$ and thereby paved the way for novel perspectives for leaky-wave antennas.

Although actually the designs of CRLH-TL for LWAs available in the literature, are developed as a different number of unit cell with a fixed geometrical size for all the unit cells of the entire antenna.

These design prevents the possibility to improve the antenna bandwidth “tapering” the geometrical size of unit cell. In order to obtain an improvement of the antenna bandwidth a novel design of CRLH LWAs was used in our work. The simulation results of the the CRLH...
unit-cell with different size, obtained by a commercial 3D EM simulator has shown the good performance of this antenna compared with the performance of the uniform CRLH TL LWA antenna.

The good performance of this composite right/left-handed LWA are also demonstrated by measured results, which shown a good agreement with simulation results paving the way for the future applications of the antenna.

11. Antenna design

It has been shown that the leakage rate of the CRLH-TL LWA can be altered by using different sizes of the unit-cell [27] as shown in Fig.34.

![Fig. 34. Different size and number of fingers of CRLH-TL unit cell.](image)

In detail the radiation resistance, of the unit-cell having four fingers and the unit-cell of six fingers, both the unit-cells designed to have the phase origin at the same frequency, shows two different bandwidth as mentioned in [27-28].

The radiation resistance of the four finger antenna is always higher than that of the six-finger one, which implies faster decay of power (more leakage) along the structure for the former.

Moreover it should be noted that increasing the number of fingers the size of the unit-cell has to be reduced in order to have the same centre-frequency for the antenna antennas, otherwise, the centre-frequency for the antenna with unit-cell which have the larger number of fingers will shift down to a lower frequency [29-30].

As shown in [21-22] for a simple microstrip leaky wave antenna the radiation bandwidth is governed by the line width once the substrate is fixed. The bandwidth can be improved by adopting a tapered line structure (Fig.35), where, the radiation of different frequency regions leaks from different parts of the antenna.

![Fig. 35. A taper layout of LWA with a different frequency regions leaks from different parts of the antenna.](image)
In fact from the propagation characteristics of the leaky wave antenna, we known that the leakage radiate phenomena, can only be noted above the cutoff frequency of higher order mode, and below the frequency such that, the phase constant is equal at the free space wave number. Decreasing the width of the antenna for a microstrip leaky-wave antenna the cutoff frequency increases shift toward high frequency. This behaviour allows to design a multisection microstrip LWA according [21-22] superimposing different section, in which each section can radiate in a different and subsequence frequency range, obtaining a broadband antennas. In this way each section should be into bound region, radiation region or reactive region, permitting the power, to uniformly radiated at different frequencies.

Following these idea in the our developed procedure we have applied a process to get the dimension of the physical parameters of the unit cell shows in Fig. 36 whit different optimized number of fingers (see Fig. 37). Naturally we have calculated the extraction parameters of every cell of CRLH implementation: LR, CR, LL, and CL using the equation mentioned in [26].

In the case of CRLH transmission line based LWA the amount of radiation by the unit cell can be related to the beam shape required and thus can be used to determine the total size of the structure as mentioned in [31].

Given the unit cell equivalent circuit in Fig. 36, we have the per unit length series impedance and per unit length shunt admittance as follows [31]:

\[
Z' = R_a' + R_I' + j\omega L_R' - \frac{j}{\omega C_L'}
\]

\[
Y' = G' + R_I' + j\omega C_R' - \frac{j}{\omega L_L'}
\]

Where \( R_a' \) represents radiation resistance per unit length, \( R_I' \) represents the per unit length resistance associated with transmission loss, \( L_R' \) and \( C_R' \) denotes per unit length parasitic inductance and capacitance respectively, \( C_L' \) and \( L_L' \) denotes times unit cell length left-hand capacitance and inductance respectively.

Propagation constant and characteristics impedance are given by the following relations:
\[ \gamma = \alpha + j\beta = \sqrt{ZY} \] (23)

\[ Z_c = \sqrt{\frac{Z}{Y}} \] (24)

From the above expression of propagation constant and line impedance we can find the centre frequency of the CRLH LWA [31].

These procedure was applied for subsequence frequency range of interest able to obtain a broadband antenna and a narrow-beam radiation pattern more than the uniform CRLH-TL LWA.

Fig. 37. Layout of a single unit cell of CRLH-TL LWA were \( p \) is the length of the unit cell period, \( l_c \) is the length of the capacitor \( w \) and \( w_s \) represent, the overall width of its finger and the width of the stub respectively.

The optimized antenna design as we can see in Fig. 38 was obtained considering the sequence of 16 cells composed respectively by 4 cell with 12 fingers, 4 cells with 10 fingers, 4 cells with 8 fingers, and 4 cells with 6 fingers.

Fig. 38. Layout of the 16 unit-cell CRLH-TL LWA with cells of 10, 8 and 6 fingers.
4 cell with 8 fingers and 4 cell with 6 fingers for the entire length of the antenna of 207.55 mm and width between 2.9 mm (cells with 12 fingers) and 5.9 mm (cells with 6 fingers).

12. Simulation and experimental results

In the following Fig. 39 and Fig. 40 are showing the simulation data of the return loss obtained with a 3D EM commercial software, of the uniform 16 unit-cell CRLH-TL LWA of 10 fingers compared with the results of tapered 16 unit-cell CRLH-TL LWA. Instead in Fig. 41 and in Fig. 42, are shown the results of the radiation pattern of the uniform CRLH-TL LWA compared with 16 unit-cell of 10 fingers and tapered 16 unit-cell CRLH-TL LWA. It is evident the good performance of the tapered 16 unit-cell CRLH-TL LWA compared with uniform CRLH-TL LWA in term of broadband and narrowbeam.

![Fig. 39. Return loss (S11) of the uniform 16 unit-cell CRLH-TL LWA with 10 fingers.](image1)

![Fig. 40. Return loss (S11) of the 16 unit-cell CRLH-TL LWA with cells of 12, 10, 8 and 6 fingers.](image2)
Fig. 41. Radiation pattern of the E field of the uniform CRLH-TL LWA for f=1.12 GHz (red line), f=2.30 GHz (brown line), f=3.20 GHz (blue line).

Fig. 42. Radiation pattern of the E field of the tapered CRLH-TL LWA for f=1.12 GHz (red line), f=2.30 GHz (brown line), f=3.20 GHz (blue line).

The simulation results were compared with experimental results made on a prototype of CRLH-TL LWA (see Fig. 43) designed with 16 unit-cell on Rogers RT/duroid 5880 substrate with dielectric constant $\varepsilon_r = 2.2$ and thickness $h = 62$ mil (loss tangent = 0.0009) showing a quite good agreement with simulated results of tapered 16 unit-cell CRLH-TL LWA as we can see in Fig. 44 and Fig. 45.
Nowadays, miniaturization of electronic devices is the main request that productions have to fulfil. In this process, the reduction of the antenna size is the crucial challenge to face, being its dimensions related to the working frequency.

The rapid developing of the modern society has become to a crescent interest for the wireless communications. Nowadays, everybody wants to be connected everywhere...
without the use of cumbersome devices. The current tendency goes towards portable terminals that have to be light and hand pocket. A suitable antenna for the portable terminals should be low cost, low profile, light weight and especially small size.

Printed antennas are commonly used for their simple structure and easy fabrication. As applications are space limited, it is challenging to design an antenna of small size but with simple tunable feature. For microstrip antennas, some techniques, such as making slots in their structure or using high dielectric constant substrates, can be used to reduce the antenna size. However, it results in the narrow bandwidths for its high Q factor and the low radiation efficiency.

In the following sentences is described an antenna printed on a substrate with low dielectric constant in order to get a reliable bandwidth. Moreover, the meander configuration allows us to reduce the antenna size keeping good radiation performance.

Meander dipole antennas have been already designed through numerical techniques that apply either time- or frequency-domain algorithms demanding high computational efforts and long-time processing. The common approach in the design of meander antenna is to draw a meander path with a suited length to the working frequency in commercial software and run simulations. Nevertheless, This empirical approach may lead to several consecutive trials and verifications. In order to decrease the long-time processing and avoid these cut and try methods, it would be convenient to start simulations with a commercial software having an antenna size close to its optimized dimensions. Thus, a good initial configuration can strongly affect the numerical convergence efficiency and the design process would be quicker.

This paper presents a transmission line model that provides an initial geometrical configuration of the antenna that allows us a computational improvement in the design of meander antennas. The dimensions obtained from the model have been used to run a simulation with a commercial software and an antenna resonating very close to that working frequency has been achieved. Finally, a quick optimization has been performed to definitely tune the antenna according to the ISM band.

14. TL model for meander antennas

Commercial and military mobile wireless systems demand for high compactness devices. An important component of any wireless system is its antenna. Whereas significant efforts have been devoted towards achieving low power and miniaturized electronic and RF components, issues related to design and fabrication of efficient, miniaturized, and easily integrable antennas have been overlooked. In this paper a novel approach for antenna miniaturization is presented. The meander topology is proposed as a good approach to achieve miniaturization and a transmission line model for the analysis and synthesis of meander antennas is developed.

Indeed, the miniaturization of an antenna can be accomplished through loads placed on the radiating structure. [32-33]. For example, monopoles were made shorter through center loaded (inductive) or top loaded (capacitive). Hence appropriate loading of a radiating element can drastically reduce the size, however, antenna efficiency may be reduced as well. To overcome this drawback, lumped elements of large dimensions can be created using
distributed reactive elements. For this reason, we propose a meander topology that allows us to distribute loading through short-circuited transmission lines.

In the past, meander structures were suitably introduced to reduce the resonant length of an antenna without great deterioration of its performances [34-36].

To exploit the meander topology to miniaturize printed antennas and develop a transmission line model for the analysis and the synthesis of this kind of antennas is proposed an antenna shown in Fig 46. It is a meander printed on the same side of the chassis of a circuit board on a FR4 substrate with $\varepsilon_r = 3.38$ and thickness 0.787 mm. The feeding is between the meander structure and the ground plane. Even if the antenna is a printed monopole, it can be studied as an asymmetric dipole and its input reactance has been studied through a transmission line model. It is well known that the resonance condition is obtained when the input impedance is purely resistive [37-39]. The antenna has been modelled as a transmission line periodically loaded from inductive reactances $X_m$ represented by the half meanders shown in Fig 46. We have named half-meander the shorted transmission line of length $w/2$.

![Fig. 46. Meander antenna monopole printed on the same side of the ground plane of the substrate.](image)

The height $b$ of each half meander and their total number $2n$ are related to the total length of the monopole $L_{ax}$ with the following formula:

$$L_{ax} = (2n + 1)b$$  \hspace{1cm} (25)

Each half meander was studied as a short transmission line $w/2$ long with a characteristic impedance $Z_{cm}$ obtained as:

$$Z_{cm} = 120\ln(b/a)$$  \hspace{1cm} (26)

and terminating with a metallic strip having an inductance $L_{sc}$:

$$L_{sc} = 2 \times 10^7 b[\ln(8b/a) - 1].$$  \hspace{1cm} (27)
The inductance $L_{sc}$ of the strip with the length $b$ and width $a$ was substituted by a line $L_{all}$ long terminating with a short circuit. The length $L_{all}$ was properly chosen because this line had the same inductance of the strip ($L_{sc}$).

At the end, the inductance of each meander $X_m$ was obtained by the formula (28):

$$X_m = Z_{cm}tg\left[2\pi \sqrt{\frac{\varepsilon_{e}}{\varepsilon_{0}} (w / 2 + L_{all} - a / 2)}\right]$$

(28)

The total characteristic impedance of the transmission line with a length $L_{ax}$ and loaded by $2n$ half meanders was:

$$Z_c = 120[\ln(8L_{ax} / a) - 1]$$

(29)

In Fig. 47 the normalized length $L_{ax}$ of the printed monopole versus the normalized thickness $a$ according to the transmission line model for $w / b = 1$ is shown. It is pointed out from the figure that, when $b=w$, the meander length is smaller than the conventional monopole at its resonant frequency.

In Fig 48, for several values of the parameter $x=w/\lambda$, the resonant length $L_{ax}/\lambda$ versus the ratio $w/b$ is plotted.

It can be seen that, for each value of $w/b$, a remarkable reduction of the antenna length is obtained by increasing the values of $w$ at the resonant frequency. Therefore, by choosing a value of $w/b$, the model allows to detect the correspondent resonant length of the antenna.

![Fig. 47](www.intechopen.com)
Fig. 48. Transmission line model for meander antenna printed on substrate with $\epsilon_r = 3.38$ and $s = 0.81$ mm for different $x = w/\lambda$.

15. Simulated and experimental results

To test the validity of the model, simulations were run with full wave commercial software CST Microwave Studio © at a frequency of 2.45 GHz with appropriate model as shows in Fig 49.

Fig. 49. Top and bottom model of meander antenna monopole designed with CST Microwave Studio ©.

The transmission line model (TLM) and the full wave simulation were in a good agreement and the difference between the resonant length obtained by TLM and the full wave
simulations was within 250 MHz as it has been summarised in Table 2. Figs 47 and Fig. 48 show, respectively, the normalized length $L_{ax}$ versus antenna thickness $a$ for different values of $w/b$ and the normalized length $L_{ax}$ versus $w/b$ for different values of $x = w/\lambda$.

<table>
<thead>
<tr>
<th>$w/b$=1.4</th>
<th>model</th>
<th>1° run</th>
<th>2° run</th>
</tr>
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<tr>
<td>$w/\lambda$</td>
<td>$n$</td>
<td>$L_{ax}/\lambda$</td>
<td>fr sim.</td>
</tr>
<tr>
<td>[GHz]</td>
<td>[GHz]</td>
<td>[GHz]</td>
<td>[GHz]</td>
</tr>
<tr>
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<td>3</td>
<td>0.158</td>
<td>2.26</td>
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<tr>
<td>0.025</td>
<td>4</td>
<td>0.177</td>
<td>2.13</td>
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<tr>
<td>0.021</td>
<td>5</td>
<td>0.185</td>
<td>2.12</td>
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<tr>
<td>0.017</td>
<td>6</td>
<td>0.180</td>
<td>2.23</td>
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</table>

<table>
<thead>
<tr>
<th>$w/b$=1</th>
<th>model</th>
<th>1° run</th>
<th>2° run</th>
</tr>
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<tbody>
<tr>
<td>$w/\lambda$</td>
<td>$n$</td>
<td>$L_{ax}/\lambda$</td>
<td>fr sim.</td>
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<td>[GHz]</td>
<td>[GHz]</td>
<td>[GHz]</td>
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<td>0.169</td>
<td>2.41</td>
</tr>
</tbody>
</table>

Table 2. Resonant frequencies calculated with FIT method.

The antenna sizes derived from the model allow us to obtain a design very close to the final project which can be quickly optimized by avoiding long simulations with commercial software.

Table 2 shows that the antenna sizes derived from the model allow us to get antenna sizes close to the final structure as the antenna resonates almost at 2.45 GHz. Moreover, in order to get exactly 2.45GHz, a quick optimization has to be carried out by running few simulations with a commercial software.

To validate the proposed TLM method, simulations and measurements have been performed. The antenna has been printed on a Rogers R04003C with $\varepsilon_r = 3.38$ and thickness 0.81 mm. A prototype is presented in Fig 50. The geometrical sizes chosen were $a=0.5$ mm, $b=8$ mm and $w=b$ that has led to a length $L_{ax} = 56$ mm by considering 6 half meanders (Fig 50). The board total size is $L1=72$ mm and $W1=32$ mm, by considering also the chassis. The antenna is fed by a microstrip printed on the back of the chassis by terminating with a stub for achieving good matching. The microstrip is 20 mm length and the stub is $L2=8$ mm and $W2=4$ mm. The dimensions of the microstrip line has been optimized using full wave software to provide better impedance matching for the frequency antenna-resonance.

The simulated and measured return loss is shown in Fig 51. Simulation has been performed by using CST Microwave Studio © 2009 and it has shown a value of -44dB at 2.45 GHz.
Fig. 50. Meander antenna monopole printed on the Rogers R04003C substrate.

The measurements were carried out in an anechoic chamber by connecting the antenna at a network analyser through coaxial cables.

The measured return loss in Fig 51 shows a slight shift of the antenna resonant frequency towards lower frequencies from 2.45 GHz to 2.42 GHz. Nevertheless, a good matching is still observed because the reflection coefficient assumes the value -26 dB instead of -44 dB.

![Graph of S11 simulation results vs measured results.](image)

**Fig. 51.** Comparison of S11 simulation results with measured results.

Fig. 52 shows the E field radiation patterns of the antenna at 2.45 GHz on two principal planes, xz plane (Φ=0°) and yz plane (Φ=90°). The comparison of the radiation patterns shows that simulations and measurements are in a good agreement.
Fig. 52. Comparison of measured and simulated E-field at 2.45 GHz for a) $\Phi=0^\circ$ and b) $\Phi=90^\circ$.

Fig 53 shows the current distribution on the antenna. It can be observed that the current is particularly intense at the end of each half meander. Full wave simulations confirm that each half meander can be studied as a transmission line terminating in a short circuit.
Fig. 53. Current distribution on the meander antenna.

16. Reference


This book will provide a comprehensive technical guide covering fundamentals, recent advances and open issues in wireless communications and networks to the readers. The objective of the book is to serve as a valuable reference for students, educators, scientists, faculty members, researchers, engineers and research strategists in these rapidly evolving fields and to encourage them to actively explore these broad, exciting and rapidly evolving research areas.

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