1. Introduction

These days, nano (1 kg – 10 kg) - and micro (10 kg – 100 kg) - satellites, which are smaller than conventional large satellite, provide space access to broader range of satellite developers and attract interests as an application of the space developments because of shorter development period at smaller cost. Several new nano- and micro-satellite missions are proposed with sophisticated objectives such as remote sensing and observation of astronomical objects. In these advanced missions, some nano- and micro-satellites must meet strict attitude requirements for obtaining scientific data or high resolution Earth images. Example of these small satellites are nano remote sensing satellite PRISM, which should be stabilized to 0.7 deg/s (Inamori et al, 2011(a)), and nano astronomy satellite “Nano-JASMINE”, which should be stabilized to 1 arcsec (Inamori et al, 2011(b)). Most of these small satellites have the strict constraint of power consumption, space, and weight. Therefore, magnetometers which are lightweight, reliable, and low power consumption sensors are used in the most of these small satellite missions as a sensor for an attitude determination system. In addition, most of these satellites use magnetometers for the attitude control systems with magnetic actuators to calculate required output torque. Furthermore, in some nano- and micro-satellite missions, a magnetic moment is estimated using magnetometers to compensate the magnetic moment and magnetic disturbance. In these small satellite missions, magnetometers play a more important role than conventional large satellites to achieve the attitude control. Although the magnetometers are useful for nano- and micro-satellite attitude control systems, these sensors which are not calibrated are not suitable for an accurate attitude control because of the measurement noises which are caused from magnetized objects and current loops in a satellite. For a precise attitude estimation, many satellites use heavier and higher power consumption sensor such as star truckers and gyro sensors, which are difficult to be assembled to some small satellites. To achieve the accurate attitude control in the small satellite missions, the magnetometers should be calibrated precisely for the accurate attitude control system. This chapter will present what is the requirement for magnetometers in the nano- and micro-satellite missions, how these magnetometers are used in these small satellite missions.

2. Magnetic sensors in nano- and micro-satellite missions

In many nano- and micro-satellite missions, magnetometers are indispensable for attitude control systems and assembled to most of these satellites. In many cases, these small
satellites use magnetometers to satisfy the following three requirements: 1) attitude determination using magnetometers, 2) attitude control using magnetic torquers, and 3) estimation of the satellite residual magnetic moment. The magnetometers in most preceding missions featuring large to small sized satellites had the first two requirements. The third requirement is for precise attitude control of the nano- and micro-satellites. In nano- and micro-satellite missions, the magnetic moment, which causes magnetic attitude disturbance, should be compensated to achieve precise attitude control, because the magnitude of magnetic attitude disturbance is larger than the other disturbances in these missions. This chapter presents each requirement of magnetometers in nano- and micro-satellite missions and the methods to achieve these requirements.

2.1 Attitude determination using magnetometers

Magnetometers are generally used for many conventional Low Earth Orbit (LEO) satellite missions for the attitude determination system. For the attitude determination system, the satellites use not only a magnetometer, but also a sun or earth sensor, which can sense the direction of the respective celestial bodies, because satellites cannot get three-axis attitude information with only a three-axis magnetometer. The transformation from a satellite body frame to the reference frame using direction cosine matrix should satisfy the following equation:

\[ \mathbf{C}_{bi} \mathbf{V}_k = \mathbf{W}_k \quad (k = 1, \ldots, n) \]  

(1)

where \( \mathbf{V}_k \) is a set of reference unit vectors, which point in the direction of the geomagnetic field, the Sun, and the Earth in the reference coordinate system. These directions are generally calculated with an onboard model such as the International Geomagnetic Reference Field (IGRF) model. \( \mathbf{W}_k \) is the observation unit vector, which points in the direction observed by the satellite sensors in the body coordinate system. The problem of estimating the attitude from more than two sets of the attitude sensors is referred to as the Wahba’s problem (Wahba, 1966). Wahba proposes the following loss function:

\[ L(\mathbf{C}_{bi}) = \frac{1}{2} \sum_k a_k | \mathbf{W}_k \cdot \mathbf{C}_{bi} \mathbf{V}_k | \]  

(2)

where \( a_k \) are positive values, which define the weight of the sensor information. The problem can be solved with the TRIAD or the QUEST algorithm (Shuster & Oh, 1981) in many satellite missions. The estimated attitude \( \mathbf{C}_{bi} \) is used for attitude control of a satellite. PRISM and Nano-JASMINE use these methods with a magnetometer and sun sensors for attitude determination. Because it is difficult to remove the effect of the bias noise caused by the residual magnetic moment of the satellite, the satellite generally uses magnetometers for coarse attitude determination.

2.2 Attitude control using magnetic torquers and magnetometers

Magnetic torquers (MTQ) are useful actuators for nano- and micro-satellite attitude control because they are small, lightweight, and low cost actuators with low power consumption.
MTQs are composed of electromagnetic coils, which cause a magnetic dipole moment, interfering with the geomagnetic field, inducing torque for attitude control. The actuator generates torque only in the direction perpendicular to the geomagnetic field. Therefore, the magnetic torquer is not useful for precise attitude control. Most satellites use this actuator for coarse attitude control in an initial phase as a reliable actuator with low power consumption. The actuator is also useful for unloading reaction wheels (Camillo and Markley, 1980).

In this attitude control system using MTQs, the satellites cannot control torque directly, but make use of the magnetic moment to generate torque. Therefore the satellite needs the geomagnetic field information to be able to output the required torque with MTQs. The magnetic moment which should be generated by the MTQs is calculated with measurements performed by magnetometers. A famous attitude control method using a magnetometer is the Bdot method, in which a satellite can stabilize attitude using only a magnetometer in an initial phase when it is difficult to estimate the attitude using sensors after the releasing from a rocket. In accordance with the Bdot method, the magnetic moment of a MTQ is controlled as follows in the PRISM mission.

\[
M_k = K_p \left( \frac{B_k - B_{k-1}}{\Delta t} \right)
\]

where \( K_p \) is the control gain, \( B_k \) is the magnetic field vector obtained by a magnetometer at time step \( k \), and \( \Delta t \) is the step time. Another famous method is the Cross product control method. In this method, an output magnetic moment from a MTQ is computed as follows:

\[
M_k = K_c \left( \frac{T \times B_k}{|B_k|} \right)
\]

where \( K_c \) is the control gain for the Cross product method, \( B \) is the magnetic field vector obtained by a magnetometer, and \( T \) is the torque requirement calculated by the onboard computer. The method for calculating \( T \) depends on the objective of the attitude control. For an attitude stabilization with PD controller, \( T \) can be calculated as follows:

\[
T_c = K_p \left( \omega_k - \omega_{ref} \right) + K_d \left( \frac{\omega_k - \omega_{k-1}}{\Delta t} \right)
\]

where \( K_p, K_d \) are control gains, \( \omega_k \) is an estimated angular velocity at time step \( k \), and \( \omega_{ref} \) is the target angular velocity. In the Bdot method, the satellite can control angular velocity only to zero and cannot control attitude, but the satellite can stabilize attitude using only a magnetometer. In contrast, using the Cross product method, the satellite can control angular velocity to an arbitrary rate and can also control the direction of the attitude. However, in this case, the satellite requires not only a magnetometer, but also other attitude sensors for the attitude control system. Hence, the Bdot method is useful for attitude stabilization in the phase following ejection from a launcher, when the satellite cannot use many attitude sensors, while the Cross product method is useful for coarse attitude control after this initial phase.

### 2.3 Residual magnetic moment estimation using magnetometers

Several attitude disturbances are considered for an attitude control system of a nano- or micro-satellite in LEO: magnetic disturbance; air pressure disturbance; solar disturbance; and...
gravity gradient disturbance. Although, for larger satellites, the effect of the magnetic disturbance is smaller and is therefore not considered in those satellite missions, the magnetic disturbance is larger than the other attitude disturbances for LEO nano- and micro-satellite missions. This is because of the relatively large magnetic moment in satellites with a small moment of inertia and because of the large magnitude of the geomagnetic field in LEO (Inamori et al, 2011(c)). In order to satisfy the strict attitude requirements for LEO nano- and micro-satellite missions, the effect of the magnetic disturbance should be mitigated to achieve a precise attitude control. Because the magnetic disturbance has only a small effect on larger satellites and is not considered in those missions, magnetometers are not used for magnetic compensation. Thus, the magnetic compensation is the new requirement for a magnetometer to achieve precise attitude stabilization for nano- and micro-satellites.

The magnetic disturbance is caused by the interaction of the geomagnetic field and the residual magnetic moment of a satellite. If a satellite estimates the residual magnetic moment and compensates for the magnetic moment with the steady output of a MTQ, the satellite compensates the effects of the magnetic disturbance.

![Fig. 1. Overview of the magnetic moment compensation (Inamori et al, 2011(c)).](image)

Fig.1 shows an overview of the magnetic disturbance compensation. In order to compensate for the magnetic disturbance precisely, a satellite must estimate the residual magnetic moment accurately and must have an accurate actuator to generate a magnetic moment. The satellite can estimate a magnetic moment using an extended Kalman filter with magnetometers and gyro sensors. This section presents an estimation technique for the residual magnetic moment using the extended Kalman filter (Inamori et al, 2011(d)). The model of attitude dynamics can be expressed as follows:

\[
I \dot{\omega} = M \times B - \omega \times (I \omega + h) - \dot{h}
\]

(6)

\[
\dot{M} = \text{diag} \left( -\frac{1}{\tau}, -\frac{1}{\tau}, -\frac{1}{\tau} \right) M
\]

(7)

where \(I\) is a tensor of inertia of a satellite, \(h\) is the angular momentum of reaction wheels, \(M\) is the residual magnetic moment of the satellite, \(\tau\) is the time constant of the residual magnetic moment, and \(B\) is the geomagnetic field vector. The magnetic moment of a satellite is assumed to change over the orbital period, therefore the time constant \(\tau\) is set to be the orbital period duration. The state vector of the filter can be expressed as follows:
The linearized equations are expressed as follows:

$$\Delta \dot{\omega} = \mathbf{I}^{-1} \left( [(\mathbf{I} \omega_{\text{ref}} + \mathbf{h}) \times] - [\omega_{\text{ref}} \times \mathbf{I}] \Delta \omega \right) - \mathbf{I}^{-1} [(\mathbf{B} \times) \Delta \mathbf{M}]$$

$$\Delta \mathbf{M} = \text{diag}(-\frac{1}{\tau}, -\frac{1}{\tau}, -\frac{1}{\tau}) \Delta \mathbf{M}$$

which can be arranged in matrix form as

$$\Delta \mathbf{x} = \mathbf{A} \Delta \mathbf{x}$$

$$\Delta \mathbf{z} = \mathbf{H} \Delta \mathbf{x}$$

where the state vector is defined as

$$\Delta \mathbf{x} = \begin{pmatrix} \Delta \omega \\ \Delta \mathbf{M} \end{pmatrix}$$

Matrix \( \mathbf{A} \) and \( \mathbf{H} \) can be expressed as follows:

$$\mathbf{A} = \begin{pmatrix} \mathbf{I}^{-1} \left( [(\mathbf{I} \omega_{\text{ref}} + \mathbf{h}) \times] - [\omega_{\text{ref}} \times \mathbf{I}] \right) & -\mathbf{I}^{-1} [\mathbf{B} \times] \\ 0 & \text{diag}(-\frac{1}{\tau}, -\frac{1}{\tau}, -\frac{1}{\tau}) \end{pmatrix}$$

$$\mathbf{H} = \begin{pmatrix} \mathbf{E} & \mathbf{O} \end{pmatrix}$$

where the skew-symmetric matrix \([\mathbf{a} \times]\) is defined as follows,

$$[\mathbf{a} \times] = \begin{pmatrix} 0 & -a_z & a_y \\ a_z & 0 & -a_x \\ -a_y & a_x & 0 \end{pmatrix}$$

The extended Kalman filter can be computed using the linearized model mentioned above. In the following text, the ‘-’ and ‘+’ superscripts on \( \hat{x} \) and \( P \) refer to pre-updated and post-updated values, respectively. The over bar indicates an estimate. The time update equation for the state can be expressed as follows:

$$\hat{x}_k^- = f(\hat{x}_{k-1}^-)$$

$$\mathbf{P}_k^- = \Phi_k \mathbf{P}_{k-1} \Phi_k^T + \Gamma_k \mathbf{Q}_{k-1} \Gamma_k^T$$

where, \( \Phi_k \) and \( \Gamma_k \) can be expressed as follows:
The measurement update equations are calculated as follows:

\[
K_k = P_k H_k^T R_k^{-1} 
\]

\[
\hat{x}_k = \hat{x}_k + K_k (z_k - H_k \hat{x}_k) 
\]

\[
P_k = P_k' - P_k' H_k^T (H_k P_k' H_k^T + R_k)^{-1} H_k P_k' 
\]

The estimated value of residual magnetic moment is applied to the magnetic compensation in orbit. The method is used for PRISM and Nano-JASMINE, which will be presented in section 4.1 and section 4.2.

3. Precise estimation of the geomagnetic field in nano- and micro-satellite missions

As shown in section 2, a magnetometer is used for attitude estimation, attitude control using electromagnetic actuation, magnetic moment estimation in nano- and micro-satellite missions. In these applications of the magnetometers, the effect of the bias error, which is generally caused by surrounding magnetized objects, electrical current loops, and ferromagnetic materials of a satellite, should be cancelled to get accurate magnetic field information. For the precise estimation of the geomagnetic field, calibration of magnetometers is indispensable.

The magnetometer calibration for nano- and micro-satellite missions is not easy on the ground because of two reasons. Firstly, the magnetic sensor should be calibrated with a flight model configuration and flight modes to evaluate the effect of magnetized objects and current loops of devices in a satellite. The calibration of a magnetic sensor assembled in a satellite requires a large facility which has a large magnetic shield to cancel the effect of magnetic field disturbance from devices external to the satellite. Furthermore, the facility should have a device such as a turntable to control the direction between the direction of uniform magnetic field and sensitivity axis of the magnetometer. Such experiments result in a higher cost for the development of the satellite. Secondly, the properties of magnetized objects and current loops of satellite devices can change in orbit after the launch. Some satellite missions reported a change of the residual magnetic moment of the satellites (Sandau et al, 2008, Sakai et al, 2008). This effect can cause a change of the bias error in orbit. For these two reasons, the calibration on ground is not suitable for precise magnetometer calibration. This section will focus on the low-cost, in-orbit calibration for nano- and micro-satellite development.

For in-orbit calibration, several methods have been proposed. These methods can be categorized into the following three groups. The first group is comprised of magnetometer only calibration without attitude sensors. In this method, the norm of the magnetometer measurement vector is compared to the expected norm calculated by geomagnetic filed
models. From this comparison, the bias error of a magnetic sensor is estimated (Alonso and Shuster, 2002(a), 2002(b)). In the second group, the predicted magnetic field from geomagnetic field models is transformed to the body coordinate system with attitude information provided by other attitude sensors (Lerner and Shuster, 1981). In the third group, the methods use several magnetometers to estimate the magnetic moment of a satellite, and then estimate the bias of the magnetometers. In addition, each group has two ways for magnetometer calibration, in-orbit estimation using an onboard computer and offline estimation with telemetry data using a computer on the ground. In offline estimations, magnetometers are calibrated using complicated algorithms on the high performance ground station computers. However, the estimation and compensation of the noise error which have non-steady bias is difficult. This is because the required estimated parameters cannot be updated until the next satellite operation. The effect of time variable bias is caused from current loops of satellite devices and solar batteries. Ferromagnetic materials also cause non-steady bias, because the strength of the bias depends on the direction of the geomagnetic field. These non-steady biases are difficult to estimate using offline estimation. On the other hand, in on-line estimation, time-variable noises can be estimated and compensated, because the parameters for the compensation are updated on-line. In this case, high-spec onboard computers are required for the estimation. With the consideration of the satellite requirements and performance of the onboard computer, satellites must choose the optimal method for magnetometer calibration. This section shows examples with offline estimation using a magnetic model which can be categorized to the first group for the PRISM mission in section 3.1 and on-line estimation using star tracker which is categorized to the second group for the Nano-JASMINE mission in section 3.2.

3.1 Magnetometer only off-line estimation

This subsection presents an example of magnetometer only, offline bias estimation. Because the bias error is as assumed to be a time constant in this method, time variable bias error which is caused from current loops cannot be estimated. The method also cannot compensate for the effect of magnetic anomalies, which is the difference between the Earth magnetic field model and the actual geomagnetic field. Because the method uses the magnetic field model as a reference for the estimation, the magnetic anomaly is observed as bias noise. Although the method is not useful for compensation of the time-variable bias and magnetic anomaly, the method is useful for bias estimation in an initial phase when the satellite cannot use attitude sensors, because the method does not use any other attitude sensors.

In this method, the bias and scale factor errors of magnetometers are estimated using a least squared method. The norm of the IGRF vector should be equal to the norm of magnetometer measurement vector. The difference between the norm of the IGRF model and that of magnetometer shows the bias and the scale factor errors. Using this disagreement information, the bias and the scale factor errors of the magnetometer are estimated by the least squared method on the ground station (Inamori et al, 2011(b)). Cost function $J$ for the least squared method is written as follows,

$$
J(s_m, b_m) = \sum_{k=0}^{N} \left( |\text{IGRF}(x, y, z, t)_k| - |B(s_m, b_m)_k| \right)^2
$$

(24)
where $x$, $y$, and $z$ are the position of a satellite in the reference frame, which can be calculated using two line elements and the SGP4 algorithm. $\text{IGRF}(\cdot)$ is a function for the IGRF model. $s_m$, $b_m$ are the scale factor and bias of a magnetometer. Magnetometer measurements are modelled as follows,

$$B_k = s_m V_{mk} + b_m$$  \hspace{1cm} (25)

where $B$, $s_m$, $M_V$, and $b_m$ are the magnetometer measurements, scale factors, the output data of an AD converter, and bias noises, respectively. The objective of the method is to estimate the scale factor $s_m$ and the bias noise $b_m$. These parameters are estimated to minimize the cost function $J$ in equation 24 by the least squared method.

In the PRISM mission, the bias and scale factor errors of a gyro sensor are also estimated using the calibrated magnetometer. The following equations show how to estimate the parameters for the gyro sensor with the calibrated magnetometer. The relationship between the time derivative of the geomagnetic field vector in the body frame and in the reference frame can be expressed as follows:

$$C_{bi} \frac{dB_i}{dt} = \frac{dB_b}{dt} + \omega \times B_b$$  \hspace{1cm} (26)

where $C_{bi}$ is the direction cosine matrix from a reference frame to a body frame, $B_i$ and $B_b$ are the geomagnetic field vector in the reference frame and the body frame, respectively. $B_i$ changes slowly throughout the orbital period (about 6000 s in LEO). The time derivative of the geomagnetic field in the reference frame is treated as a constant value in a step time in this method. Thus, equation 26 can be written as follows:

$$\frac{dB_i}{dt} = -\omega \times B_b$$  \hspace{1cm} (27)

In this equation, the term $\frac{dB_i}{dt}$ should be equal to the term $-\omega \times B_b$. If there are bias and scale factor errors in magnetometer measurements, $\frac{dB_i}{dt}$ and $-\omega \times B_b$ are not equal. In this case, the bias and the scale factor of the gyro are estimated by a least squared method. The cost function $J$ for the gyro calibration is expressed as follows:

$$J(s_g, b_g) = \sum_{k=0}^{N} \left( \frac{dB_k}{dt} - (B_{kx} \omega_{kx} - B_{ky} \omega_{ky}) \right)^2 + \sum_{k=0}^{N} \left( \frac{dB_k}{dt} - (B_{kz} \omega_{kz} - B_{ky} \omega_{ky}) \right)^2$$

$$+ \sum_{k=0}^{N} \left( \frac{dB_k}{dt} - (B_{kx} \omega_{kx} - B_{kz} \omega_{kz}) \right)^2$$  \hspace{1cm} (28)

where $\omega_k$ can be expressed as follows,

$$\omega_k = s_g V_{gk} + b_g$$  \hspace{1cm} (29)

where $s_g$, $b_g$, $V$ are the scale factor, bias noise, and the voltage of the gyro sensors, respectively. These parameters are estimated for calculating minimized the cost function $J$. 

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These calibrated magnetometer and gyro sensor measurements are used for attitude estimation and magnetic attitude control system using a MTQ in PRISM mission. The result of the in-orbit calibration in PRISM will be presented in section 4.1.

3.2 Calibration method (on-line estimation with an attitude sensor)

This section presents an example of magnetometer on-line bias estimation using an attitude sensor. For precise attitude control in nano- and micro-satellite missions, a magnetic moment should be estimated and compensated for in order to cancel the effect of the magnetic disturbance. For the accurate magnetic moment estimation, the effect of magnetometer bias should be compensated for. Fig.2. shows simulation results of the magnetic moment estimation of Nano-JAMINE using magnetometer measurement with bias errors. In Nano-JAMINE mission, the magnetic moment should be estimated and compensated for to an accuracy of $1\times10^{-4}$ Am$^2$. Fig.2. shows that the bias error should be compensated for to an accuracy of 50 nT. In order to achieve accurate geomagnetic field measurements, some satellites used a magnetometer installed on the tip of a boom in order to remove the effect of the residual magnetic moment of the satellite; however the booms which generally have flexible structure cause attitude disturbances and attitude instability; therefore the booms are not useful for the satellites which aim for precise attitude control. In order to estimate bias error to this accuracy, the effect of time-variable bias and magnetic anomaly should be considered. For this reason, Nano-JAMINE uses on-line bias estimation method using an attitude sensor. Because the method uses the accurate attitude sensor for the calibration, the method is not useful for calibration achieved for attitude determination in the initial phase when accurate attitude sensors are not available.

![Simulation result of magnetic moment estimation with magnetometer bias noise.](image)

Fig. 2. Simulation result of magnetic moment estimation with magnetometer bias noise.

In this estimation, an Unscented Kalman Filter (Wan et al, 2000) is introduced to estimate the bias noise of magnetometer accurately (Inamori et al, 2010). Firstly, following sets of sigma points are computed.

\[
\chi_0 = \hat{x}_{k-1}
\]

\[
\chi_i = \hat{x}_{k-1} + \left( \sqrt{(n + \kappa)(P_{k-1} + Q_{k-1})} \right)_i \quad i = 1, \ldots, n
\]

\[
\chi_i = \hat{x}_{k-1} - \left( \sqrt{(n + \kappa)(P_{k-1} + Q_{k-1})} \right)_i \quad i = n + 1, \ldots, 2n
\]
where the matrix \( Q \) is the process noise covariance, \( n \) is the dimension of the state vector, and \( \kappa \) is a scaling parameter. The term \( \sqrt{(n + \kappa)(P_{k-1} + Q_{k-1})} \) is calculated using the Cholesky decomposition method. Note that the matrix dimensions are \([2n \times n]\). In this filter, each sigma points calculated in Equation 30-32 are propagated in every filter computation steps. After the propagation of each sigma points, the results are averaged to obtain state vector and covariance matrix accurately in non linear model. The state vector can be expressed as follows in this estimation filter:

\[
x = \begin{pmatrix} q \\ b \\ h \end{pmatrix}
\]  

(33)

where \( q \) is quaternion, \( b \) is the bias error of magnetometer measurement, and \( h \) is the magnetic anomaly of the geomagnetic field. In each step, the state vector and the covariance matrix of the state vector are propagated with dynamics models in an onboard computer. Time update equation is expressed as follows:

\[
\chi_{i,k} = f(\chi_{i,k-1})
\]

(34)

\[
\hat{x}_{k,1} = \sum_{i=0}^{2n} W_i \chi_{i,k}
\]

(35)

\[
\bar{P}_k = \sum_{i=0}^{2n} W_i (\chi_{i,k} - \hat{x}_k)(\chi_{i,k} - \hat{x}_k)^T
\]

(36)

where \( W_i \) is the weight for the sigma points. The weight \( W_i \) can be expressed as follows in this filter:

\[
W_0 = \frac{\lambda}{n + \lambda}
\]

(37)

\[
W_i = \frac{\lambda}{2(n + \lambda)} \quad i = n + 1, \ldots, 2n
\]

(38)

The function \( f(x) \) is obtained by integration using the following differential equations,

\[
\dot{q} = \frac{1}{2} \begin{pmatrix} -[\omega \times] & \omega \\ \omega^T & 0 \end{pmatrix} q
\]

(39)

\[
b = \text{diag}\left(-\frac{1}{\tau_b}, -\frac{1}{\tau_b}, -\frac{1}{\tau_b}\right) b
\]

(40)

\[
h = \text{diag}\left(-\frac{1}{\tau_h}, -\frac{1}{\tau_h}, -\frac{1}{\tau_h}\right) h
\]

(41)
where $b$ and $h$ are the magnetometer bias and magnetic anomaly of the geomagnetic field, respectively. The both values, $b$ and $h$, are assumed to be change in time constant $\tau_b$ and $\tau_h$, respectively. After the time update, the state vector is updated with sensor measurements.

The predicted observation vector $\hat{y}_{k-1}$ and its predicted covariance $P_{k|k-1}^y$ are calculated as follows:

$$Y_{i,k} = h(x_{i,k-1})$$  \hspace{1cm} (42)

$$\hat{y}_{k-1} = \sum_{i=0}^{2n} W_i Y_{i,k}$$  \hspace{1cm} (43)

$$P_{k}^y = \sum_{i=0}^{2n} W_i (Y_{i,k} - \hat{y}_{k}) (Y_{i,k} - \hat{y}_{k})^T$$  \hspace{1cm} (44)

where $h(x)$ is defined as follows:

$$\hat{y}_k = h(\hat{x}_k)$$  \hspace{1cm} (45)

where $y_k$ is the measurement vector. In this filter, measurements can be obtained as follows:

$$y_k = B_k = C_{hi}(q_k)(H_{igrf} + h_k) + b_k$$  \hspace{1cm} (46)

where $B_k$ and $H_{igrf}$ are the geomagnetic field vector calculated with the state vector or obtained by a magnetic sensor, and geomagnetic field vector calculated with the IGRF model, respectively. the $C_{hi}$ is transformation from a satellite body frame to the reference frame, which is calculated from quaternion. The filter gain is computed by the following equation.

$$K_k = P_{k}^y (P_{k}^{yy})^{-1}$$  \hspace{1cm} (47)

where the innovation covariance is computed by

$$P_{k}^{yy} = P_{k}^y + R_k$$  \hspace{1cm} (48)

The cross correlation matrix is calculated as follows:

$$P_{k}^{xy} = \sum_{i=0}^{2n} W_i (\chi_{i,k} - \hat{x}_k) (Y_{i,k} - \hat{y}_k)^T$$  \hspace{1cm} (49)

With the calculated gain in Equation 47, the state vector and covariance matrix are updated with sensor measurement. In this update, the estimated state vector and updated covariance are given by

$$\hat{x}_k = \hat{x}_k + K_k (y_k - \hat{y}_k)$$  \hspace{1cm} (50)
\[ P_k = P'_k + K_k P_k^v K_k^T \]  \hspace{1cm} (51)

where \( y_k \) and \( \hat{y}_k \) are obtained by a magnetometer measurement and the calculation using the state vector with Equation 46.

These calibrated magnetometer measurements are applied to magnetic moment estimation in the Nano-JASMINE mission. The result of the calibration in Nano-JASMINE will be presented in section 4.2.

4. Example of magnetometer applications for small satellite missions

This section presents the attitude control system of the remote sensing nano-satellite PRISM and micro astronomy satellite Nano-JAMSINE to show examples of the application of magnetometers for nano- and micro-satellite missions. PRISM has three-axis low power consumption magneto-impedance sensor. The magnetometer measurements are used for the attitude estimation and an MTQ is used for attitude control. After completing the main mission, the satellite conducted an in-orbit experiment to demonstrate magnetic moment compensation. Nano-JASMINE has two types of magnetic sensors, a three-axis magneto-resistive magnetometer and a three-axis fluxgate magnetometer. The satellite attitude should be stabilized to within 1 arcsec during observation. In order to satisfy this requirement, the satellite should estimate the magnetic moment and compensate precisely. The fluxgate magnetometer is used for this purpose. The satellite also uses a magnetometer for attitude estimation and magnetic attitude control in initial phase, when the power consumption is limited. A low power consumption magneto-resistive magnetometer is used for this initial phase in this satellite mission. The following subsections show detailed magnetometer application for nano- and micro-satellites with in-orbit data and simulation results.

4.1 Nano remote sensing satellite PRISM

Pico-satellite for Remote-sensing and Innovative Space Missions (PRISM) is a remote sensing nano-satellite, developed at the University of Tokyo. The mission objective of PRISM is to obtain 30 m resolution earth images with a 8.5 kg nano-satellite. The satellite has an extensible boom for an optical system to reduce the total mass of the telescope and to design a compact, light-weight optics system (Fig. 3.). Table 1 shows the specification of the PRISM satellite. PRISM has been launched into a Sun-Synchronous LEO as a piggy-back satellite of the GOSAT by a H-IIA rocket in 2009. The satellite attitude should be stabilized to better than 0.7 deg/s during observation. PRISM has gyro sensors and magnetometers for attitude sensors and MTQs as actuators. In the design phase of the project, the attitude was intended to be controlled passively, using only the gravity gradient torque after the boom extension. However, the satellite would have difficulties achieving the attitude requirement because of the magnetic disturbance. To meet the mission requirements, the attitude is determined by sun sensors and magnetometers and controlled actively with MTQs (Inamori et al, 2011(b)).

PRISM has been launched to LEO in January 2009. After extending the boom, PRISM calibrated a magnetometer with the method explained in section 3.1. Fig. 4 shows the result...
Satellite Size 192×192×400 [mm³] (Boom folded)

<table>
<thead>
<tr>
<th>Satellite</th>
<th>Size</th>
<th>Total mass</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>35 [kg]</td>
</tr>
</tbody>
</table>

| Orbit     | Sun-Synchronous LEO  
           | Altitude 660 [km]  
           | Local time 13:00   |

| Mission   | Remote sensing       |

<table>
<thead>
<tr>
<th>CDH</th>
<th>CPU</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>SH7145F (Renesas Technology)</td>
</tr>
<tr>
<td></td>
<td>H8-3048F (Renesas Technology)</td>
</tr>
<tr>
<td></td>
<td>PIC-16F877 (Microchip)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Communication</th>
<th>Down</th>
</tr>
</thead>
</table>
|               | AFSK: 1200 [bps]  
               | GMSK: 9600 [bps]   |

| Up            | AFSK: 1200 [bps] |

<table>
<thead>
<tr>
<th>AOCS</th>
<th>Attitude rate requirement</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0.7 [deg/s]</td>
</tr>
</tbody>
</table>

| Sensor        | Magnetometer (AMI204, three axis)  
               | Gyro sensor (tukasa21, three axis)  
               | Sun sensor (in-house, two axis)×5 |

| Actuator      | Magnetic torquer (in-house, , three axis) |

<table>
<thead>
<tr>
<th>Optics</th>
<th>Architecture</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Refractive</td>
</tr>
</tbody>
</table>

| Diameter      | 90 [mm]      |

| Focal length  | 500 [mm]     |

| FOV           |              |

| Detector      | IBIS-5A, CMOS 1.3 M Pixel |

Table 1. Specification of the PRISM satellite.

Fig. 3. Overview of the remote sensing nano-satellite “PRISM” (a) with boom folded, (b) with boom extended.

of the magnetometer and gyro sensor calibration in orbit. In Fig.4, the magnetometer measurements before the calibration had a bias error. In PRISM project, it was difficult to calibrate assembled magnetometer with a ground facility, thus bias and scale factor were
estimated in orbit. After the calibration, magnetometer measurements did not correspond to the IGRF mode in 2000 nT accuracy, because bias of the magnetometer assembled in PRISM had a temperature dependency, which is not considered in the calibration method. After the magnetometer calibration, the bias and scale factor of the gyro sensor was estimated using the least squared method, which is mentioned in section 3.1. Fig. 4 shows the angular velocity before and after the sensor calibration. Fig. 5 shows the in-orbit result of attitude stabilization before and after the calibration. After the calibration, the satellite attitude was stabilized to an accuracy of 0.3 deg/s, which meets the attitude requirement for the PRISM mission.

![Fig. 4. Result of (a) magnetometer, (b) gyro sensor calibration in-orbit. With permission from ASCE. (Inamori et al, 2011(a)).](image)

![Fig. 5. Result of attitude stabilization in orbit (a) after the sensor calibration, (b) before the sensor calibration.](image)

After the main mission, the satellite conducted an experiment to demonstrate the method to estimate a residual magnetic moment of the satellite. In this experiment, magnetometer and gyro measurement were downloaded to a ground station, then the magnetic moment was estimated using a computer on the ground. After the estimation, the estimated parameters were uploaded to compensate for the magnetic disturbance in orbit. Fig. 6 shows the history of angular velocity of a satellite with the magnetic compensation and without the magnetic compensation, respectively. The satellite attitude was stabilized more precisely with the magnetic compensation.
Fig. 6. Angular velocity (a) without the magnetic compensation, (b) with the magnetic compensation (Inamori et al, 2011(d)).

4.2 Micro astronomy satellite Nano-JASMINE

Nano Japan Astrometry Satellite Mission for INfrared Exploration (Nano-JASMINE) is a nano astrometry satellite, developed at the Intelligent Space Systems Laboratory (ISSL), the University of Tokyo cooperation with National Observatory of Japan (NAOJ). The launch is scheduled in 2013. The objective of the Nano-JASMINE mission is to measure the three-dimensional position of stars to an accuracy of 1.8 mas (milliarcsecond), using stellar annual parallax, which is measured by the observed positions of stars at different times of a year. Table 2 shows the specification of the Nano-JASMINE satellite. Nano-JASMINE is outfitted with a telescope with a 5 cm effective diameter and a CCD (Charge Coupled Device Image Sensor) with Time Delay Integration (TDI) which is sensitive to z-band (wavelength ~ 0.9 μm). The satellite measures the position of twenty thousands of stars with a magnitude of larger than 7.5 for all-sky with an accuracy of 1.8 mas. The measurement is used to update the three-dimensional positions and proper motions of the stars in the Hipparcos catalogue. The satellite also demonstrates the space compliancy of the novel type of CCD in which TDI is embedded.

![Fig. 7. Overview of the nano astronomy satellite Nano-JASMINE](https://example.com/fig7)

For the Nano-JASMINE mission, there are two attitude requirements: control the orientation of the telescope and the angular velocity of the satellite. For the requirement of the orientation, the attitude must be controlled to an accuracy of 0.05 degrees. The attitude requirement can be achieved using a star tracker (STT) and a fibre optical gyro (FOG), which
have been used in many satellite missions. For the requirement of the angular velocity, the angular rate must be controlled to the Time Delay Integration (TDI) rate in the CCD. The error of the angular velocity with respect to the TDI rate must be smaller than $4 \times 10^{-7} \text{ rad/s}$. This requirement implies attitude sensing and actuation capabilities that are beyond the current state of the art of small satellites. To achieve the mission requirement, the satellite determines the attitude using blurred star images obtained from the mission telescope. Specifically, this method assesses the quality of star images based on how blurred it appears. To get star images using the telescope, the satellite must stabilize the attitude with attitude sensors such as the FOG before using the telescope. Nano-JASMINE stabilizes the attitude using several sensors and actuators before the observation.

<table>
<thead>
<tr>
<th>Satellite</th>
<th>Size</th>
<th>$508 \times 508 \times 512 \text{ [mm}^3 \text{]}$ (When the boom is folded)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total mass</td>
<td></td>
<td>35 [kg]</td>
</tr>
<tr>
<td>Orbit</td>
<td></td>
<td>Sun-Synchronous LEO</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Altitude 750 [km]</td>
</tr>
<tr>
<td>Mission</td>
<td></td>
<td>Infrared Astrometry</td>
</tr>
<tr>
<td>CDH</td>
<td>CPU</td>
<td>MicroBraze micro processors×6</td>
</tr>
<tr>
<td></td>
<td></td>
<td>configured in Virtex-5×2</td>
</tr>
<tr>
<td>Communication</td>
<td>Down</td>
<td>S-band 100 [kbps]</td>
</tr>
<tr>
<td></td>
<td>Up</td>
<td>S-band 1 [kbps]</td>
</tr>
<tr>
<td>AOCs</td>
<td>Attitude rate requirement</td>
<td>740 mas/8.8s</td>
</tr>
<tr>
<td>Attitude requirement</td>
<td></td>
<td>0.05 [deg]</td>
</tr>
<tr>
<td>Sensor</td>
<td>Coarse Magnetometer (HMC2003, three axis)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Precise Magnetometer (AMI204, three axis)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Mems gyro sensor (three axis)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Fiber optic gyro (three axis)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Sun sensor (in-house, two axis)×6</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Star trucker×2</td>
<td></td>
</tr>
<tr>
<td>Actuator</td>
<td>Magnetic torquer (in-house, three axis)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Magnetic canceller (in-house, three axis)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Reaction wheel×4</td>
<td></td>
</tr>
<tr>
<td>Optics</td>
<td>Architecture</td>
<td>Refractive</td>
</tr>
<tr>
<td>Diameter</td>
<td></td>
<td>90 [mm]</td>
</tr>
<tr>
<td>Focal length</td>
<td></td>
<td>500 [mm]</td>
</tr>
<tr>
<td>FOV</td>
<td></td>
<td>0.5 deg×0.5 deg</td>
</tr>
</tbody>
</table>

Table 2. Specifications of the Nano-JASMINE satellite.

The satellite uses magneto-resistive magnetometer for attitude estimation and an MTQ for actuation in the initial phase after the launch. In this phase, the satellite estimates the attitude using the QUEST method with the magnetometer and sun sensors. After controlling attitude coarsely using the magnetic attitude control system, the satellite calibrates the magnetometer for the estimation of a magnetic moment. Fig.8(a) and Fig.8(b) are simulation results of the bias and magnetic anomaly estimation, respectively. In the simulation, the bias
noise is assumed to change throughout an orbital period, because time-variable bias noise
has a relationship to temperature and current loops of batteries, which change throughout
an orbital period. The magnetic anomaly observed from a satellite is also assumed to change
throughout an orbital period, because the magnetic anomaly is fixed with respect to the
Earth coordinate system and constant within several days.

In this estimation, both bias and magnetic anomaly errors are estimated with an accuracy of
50 nT. After the estimation of the bias noise, the magnetic moment of Nano-JASMINE is
estimated using the extended Kalman filter which is presented in section 2.3. Fig. 9. shows a
simulation result of the magnetic moment estimation. In this simulation, the magnetic
moment is assumed to change in an orbital period, because the magnitude of current in
batteries changes in an orbital period. Based on this estimated value, the satellite
compensates for the magnetic disturbance.

![Simulation results of the on-line bias estimation. (a) Estimation of the bias. (b) Estimation of the magnetic anomaly.](image)

![Simulation result of the magnetic moment estimation (Inamori et al, 2011(c)).](image)

**5. Conclusion**

This chapter shows the application of magnetometers in nano- and micro-satellite missions.
Previously, most of satellites had magnetometers for coarse attitude estimation and attitude
control. The magnetometers are also used on nano- and micro-satellite for attitude
determination and control system. These days, these small satellites are applied to more
sophisticated objectives such as remote-sensing and astronomy missions, which require
precise attitude stabilization. For the achievement of the requirements, the satellite must
control attitude precisely. Because the small satellites have a small moment of inertia, the
magnetic moment which causes magnetic disturbance should be compensated for achievement of accurate attitude control. For the compensation of the magnetic disturbance, the satellites estimate a magnetic moment using a magnetometer. This is the new requirement for magnetometers in the space applications. Magnetometers are indispensable for attitude control and determination as well as magnetic disturbance compensation to achieve the sophisticated objectives in nano- and micro-satellite missions.

6. References


This book provides an introductory overview of the research done in recent years in the area of magnetic sensors. The topics presented in this book range from fundamental theories and properties of magnets and their sensing applications in areas such as biomedicine, microelectromechanical systems, nano-satellites and pedestrian tracking. Written for the readers who wished to obtain a basic understanding of the research area as well as to explore other potential areas of applications for magnetic sensors, this book presents exciting developments in the field in a highly readable manner.

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