PPCeA: A Domain-Specific Language for Programmable Parameter Control in Evolutionary Algorithms

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1. Introduction

An Evolutionary Algorithm (EA) is a meta-heuristic and stochastic optimization search process that mimics Darwinian evolution theory and Mendel's Genetics. Each process facilitates (a) population(s) evolve into fittest and/or convergence by setting parameters of selection, mutation, crossover, population resizing, and/or many other variant operators. However, due to two primary identified factors, EAs are still a challenging research topic: (1) Value choices/ranges for parameters (i.e., parameter settings) will greatly influence the evolution performance of a search process in terms of fittest and/or convergence; and (2) Parameter settings that are good for one fitness function do not guarantee the same evolution performance of another fitness function. Namely, parameter settings are function-specific. Different functions may have various characteristics that request specific attention. In order to better organize and overcome the parameter setting problem, Eiben et al. have classified parameter settings into parameter tuning and parameter control (Eiben et al., 1999): Parameter tuning determines parameter values before a search process begins while parameter control changes parameter values during a search process. More specifically, parameter control adjusts parameters on-the-fly using three different approaches: (1) Deterministic approach alters parameters based on certain pre-determined rules or formulae; (2) Adaptive approach strategically adjusts parameter values based on the feedbacks of a search process. Such feedbacks could be fitness, diversity, distance, among others; and (3) Self-adaptive approach encodes parameters to be adapted and evolves them along with a search process. Yet, even with such a classification, to our best knowledge there is no existing tool to assist researchers with conducting experiments of parameter settings with ease. Namely, researchers need to find out appropriate places out of thousand lines of EA source code to introduce and update specific parameters (including feedbacks) as well as formulae and adaptive strategies. Additionally, a number of revisions for EA source code will be also required for different kinds of experiments. To EA experimenters, such endeavor is time consuming and error prone. To EA developers, complex and tangling source code, resulted from different
parameter and strategy introductions, may also cause inflexibility for further extension and inevitability of faulty EA source code. In order to solve the aforementioned problems, a programmable approach, called PPCea (Programmable Parameter Control for Evolutionary Algorithms) (Liu et al., 2004), is presented in this book chapter.

PPCea is a Domain-Specific Language (DSL) (Mernik et al., 2005) for EAs. It uplifts the abstraction layer to a higher (i.e., domain-specific) level and introduces domain-specific notations (e.g., parameters and statements) as well as common linguistic elements. Namely, the implementation details of Genetic Algorithms (GAs) and Evolution Strategies (ESs) are encapsulated and hidden so that EA experimenters are able to experiment with evolutionary algorithms and obtain statistical results by programming a few PPCea statements. Additionally, the flexible programming fashion also enhances the possibility of reproducing existing EA experiments in a simpler PPCea source code and likely introducing new experiments to facilitate even better optimization search or faster convergence.

For EA experimenters, the first part of this book chapter introduces PPCea with examples to demonstrate PPCea’s capabilities and usability. Famous existing parameter tuning and parameter control examples are reproduced using PPCea (e.g., Fogarty’s formula (Fogarty, 1989), PROFIGA (Eiben et al., 2004), and 1/5 success rule (Bäck & Schwefel, 1995)). Additionally, new examples are also demonstrated to show the flexibility of PPCea. For example, introducing new metrics as feedbacks for parameter control and adaptively switching among different operators during an evolutionary process can be done with ease.

For EA developers, design and implementation of PPCea are covered in the second part of the book chapter. In this part, DSL patterns and design patterns are utilized. Coding and/or UML examples are presented and discussed to show how such patterns lessen the extension problems during development and maintenance phases. Software metrics are also measured to prove the effectiveness of design patterns for modularization and extension. In summary, PPCea is a domain-specific tool that is “win-win” to both EA experimenters and developers: For EA experimenters, the programmable fashion and high level abstraction allow EA users to conduct EA experiments in a productive manner. For EA developers, the design and implementation of PPCea allow evolutionary algorithms, operators, algorithms of operators (i.e., strategies), and parameters to be introduced or revised painlessly.

The book chapter is organized as follows. By using grammars, code snippets, and UML diagrams, Sections 2 and 3 respectively introduce PPCea from the perspectives of experimenters and developers. Section 4 discusses related work on parameter settings in Evolutionary Algorithms. PPCea’s capabilities, limitations, and future directions are concluded in Section 5.

2. PPCea: A Painless Problem Curer for EA users

Because of the meta-heuristic and stochastic characteristics towards searching optimization, experimenters or users of EAs are inevitably requested to perform a sufficient number of experiments. Needless to say, there are numerous combinations and scopes of domain-specific parameters (e.g., mutation rate, crossover rate, and selection pressure) need to be tuned or controlled so that fittest and/or convergence can be discovered. A primary objective of PPCea is to become a problem curer for EA users/experimenters to conduct experiments painlessly. We first introduce PPCea through a number of examples categorized by Eiben et al.’s classification suggestions. The grammar of PPCea is appended at the end of the chapter for interested readers.
2.1 PPCea for parameter tuning

Parameter tuning is an approach for EA experiments classified in (Eiben et al., 1999). Such a kind of experiments determines the parameters of an evolutionary process before it runs and will not change the parameter values during the process. Many of the existing EAs are classified into this category. Per their endeavors, common guidelines for setting mutation and crossover rates in GAs are as follows: mutation rate ($p_m$) $\approx \frac{1}{\text{the bit length of an individual in genetic algorithms}}$ and crossover rate ($p_c$) $\approx 0.75$–$0.95$. PPCea can reproduce such experiments easily. Figure 1 shows that twenty experiments of Ackley’s function from (Yao et al., 1999) with different parameter tuning settings are defined using Grefenstette’s guideline (Grefenstette, 1986). Also, if one does not want to reset different values for $p_m$, $p_c$, or any domain-specific parameters for each experiment, formulae may be defined to adjust the values of such parameters as seen in the italic part of Figure 1, where the if-statement within the while-statement adjusts $p_m$ every 5 experiments. The experimental results of three reproduced parameter tuning-based experiments are available at (Liu, 2010).

```
genetic
readfile weightF10.txt; //load coeff. of Ackley's function from Yao et al., 1999
Function := 10; //load Ackley's function from Yao et al., 1999
Round := 20; //number of experiments
Maxgen := 1000; //maximum generation of an evolutionary process
pm := 0.001; //set mutation rate
pc := 0.95; //set crossover rate
r := 0;
while ( r < Round ) do
    init; //initialize population
    callGA; //invoke an evolutionary process of GA
    if ( ( r % 5) == 0) then
        pm := pm + 0.001 //change pm every 5 experiments
        r := r + 1
    end;
    writeresult //output the experimental results to text and Excel files
end genetic
```

Fig. 1. Parameter tuning using PPCea

2.2 PPCea for deterministic parameter control

```
genetic
//skip initializing Round, Maxgen, Popszie, Epoch, pm, alpha, beta, gamma, length, r, g
while ( r < Round ) do
    init; //initialize population
    while ( g < Maxgen ) do
        callGA; //invoke an evolutionary process of GA
        pm := sqrt(alpha / beta) * exp((0 – gamma)*g/2) / (Popszie / length);
        // the above formula is from Hessen & Manner
        // pm := 1 / (2+(( length-2 )/Maxgen)* g )
        // the above formula is from Bäck & Schütz
        g := g + Epoch //Generation stride for parameter control adaptation
        r := r + 1
    end;
    writeresult //output the experimental results to text and Excel files
end genetic
```

Fig. 2. Deterministic parameter control using PPCea
An important advantage of PPCell over other EA frameworks or software is its capability of performing parameter changes on-the-fly through a programmable fashion. Deterministic parameter control is an approach that defines how to change parameters during an evolutionary process using formulae. Fogarty (Fogarty, 1989) proposed one of the earliest deterministic approaches that adjusts mutation rate to a smaller value along with generations in order to tend from exploration towards exploitation. Liu et al. has published the experimental results of five unimodal and seven multimodal functions using Fogarty’s mutation rate formula in (Liu et al., 2009). Figure 2 reproduces (Hesser & Männer, 1991)’s and (Bäck & Schütz, 1996)’s mutation formulae to show that PPCell is capable of representing more sophisticated cases.

2.3 PPCell for adaptive parameter control
Different from deterministic parameter control that does not interact with the evolutionary process that it controls, adaptive parameter control utilizes the analysis results from the evolutionary process and then determines which directions the evolutionary process may move forward by changing the parameters of associated operators. PPCell has reproduced 1/5 success rule (Bäck & Schwefel, 1995) and population resizing (Smith & Smuda, 1995) and introduced an entropy-driven approach (Liu et al., 2009) to adapt an evolutionary process. Figure 3 shows that PROFIGA (Eiben et al., 2004) is reproduced by PPCell. PROFIGA is a GA that utilizes population resizing to balance between exploration and exploitation. As seen in the first if-statement in the figure, if the best fitness is improved, then population size will be increased proportionally so that more exploration can be promoted. Similarly, if the evolutionary process is not improved every kgen generations, the population size will be proportionally increased using the same factor (growFactorX). The second if-statement performs such an objective. Note that growFactorX is a negative value so that the formula within the second resize uses subtract operator. Lastly, the last if-statement shows that if neither the first nor the second conditions hold, the evolutionary process will tend to exploitation by shrinking the population size.

Of course, PPCell is not almighty. For example, GAVaPS (Arabas et al., 1994) and APGA (Bäck et al., 2000) perform population resizing based on aging concept. Such algorithms cannot be reproduced by current PPCell due to absence of age in individuals. Yet, once age is introduced along with associated operators, PPCell is capable of performing GAVaPS and APGA without a doubt. Similarly, parameter-less GA (Harik & Lubo, 1999) introduces a number of populations with different sizes to compete with each other. Because PPCell currently does not introduce multi-populations, reproducing parameter-less GA is also questionable. Because the design and implementation of PPCell facilitate extension and evolution, new algorithms like GAVaPS, APGA, parameter-less GA, and other EAs may be introduced with ease. More discussions on how to utilize such design and implementation advantages to introduce new algorithms will be covered in Section 3.

2.4 PPCell for adaptive operator control
Adapting parameters on-the-fly is not new in EAs. What about adapting operators on-the-fly? Adapting operators may be classified into three categories:
1. Operator adaptation is delegated to parameter control. Such an adaptation is done by adjusting parameters associated to specific operators. For example, 1/5 success rule utilizes mutation success rate to determine if mutation rate needs to be tuned up or
down. Similarly, selection pressure assists in adjusting the performance of selection operator in terms of fitting offspring. Usually adaptation in this category is classified as parameter control (Eiben et al., 1999);

2. Instead of focusing on the effectiveness of a specific operator using parameter control, an evolutionary process may switch among different operators based on certain real-time feedbacks. For example, Ursem (Ursem, 2002) introduced Diversity-Guided Evolutionary Algorithm (DGEA) that splits an evolutionary process into exploration and exploitation modes based on diversity. Under exploitation mode, recombination and selection are active. Otherwise, mutation is in charge;

3. Adaptation can be also done by switching among different variants of the same type of operators (Herrera & Lozano, 1996). For example, switching from one-point mutation to N-point mutation may result in more exploration during an evolutionary process, and switching from linear selection to non-linear one may change the influence weight of certain portion of individuals.

For (1), it has been discussed in the previous subsection. This subsection first reproduces DGEA falling into category (2) and then proposes how PPCea expresses experiments in category (3).

DGEA introduces a new diversity metric that computes the distance of all individuals to the average point of an N-dimensional search space. Exploration mode is identified if the diversity metric is lower than a predefined lower bound, and exploitation mode is recognized as the metric is higher than a predefined higher bound. Selection and crossover are applied to explore search space while mutation is treated as exploitation operator. Figure 4 shows the reproduction of DGEA, where dLow and dHigh are user-defined parameters and DistanceToAvgPt is computed by PPCea. changeStrategy is a PPCea statement.
that switches between operators. For example, within exploration mode, tournament selection and 1-point crossover are active and mutation is halted. Conversely, mutation is the only active operator while selection and crossover are halted by the two keywords specified within the second changeStrategy.

```
// initialize all needed parameters including dLow, dHigh
init;
while ( g < Maxgen ) do
    callGA;
    if ( DistanceToAvgPt < dLow ) then // exploration mode
        changeStrategy(TOURNAMENT_SELECTION, GA_HALT_MUTATION, ONE_PT_CROSSOVER)
    fi;
    if ( DistanceToAvgPt > dHigh ) then // exploitation mode
        changeStrategy(GA_HALT_SELECTION, ONE_PT_MUTATION, GA_HALT_CROSSOVER)
    fi;
    g := g + 1
end
```

Fig. 4. DGEA reproduction using PPCea

The previous example shows that PPCea can swap between different operators when needed. Halting an operator under a specific condition is also feasible by setting GA_HALT_SELECTION, GA_HALT_MUTATION, and GA_HALT_CROSSOVER, among others. When PPCea interpreter identifies such keywords, the operators will not be executed until they are reactivated by next changeStrategy statement. More details about how these are implemented will be covered in Section 3.

As mentioned before, DGEA is within category (2). A PPCea example classified within category (3) is introduced in Figure 5. Initially, context, a PPCea statement, defines specific operators will be executed by the evolutionary process. Line 1 shows that linear selection, 1-point mutation, and n-point crossover are picked to perform optimization search at the beginning. Lines 5 to 10 shows that two operator pairs (TOURNAMENT_SELECTION, N_PT_MUTATION) and (RANK_SELECTION, ONE_PT_MUTATION) will be swapped every 10 generations until 95th generation. Mutation will be stopped at the last 5 generations. Because N_PT_CROSSOVER never appears in the pairs of changeStrategy, this operator will remain active during the entire evolutionary process. How PPCea interpreter executes such operator adaptation will be also covered in Section 3.

2.5 Summary

As can be seen in the previous examples, the programming fashion of PPCea facilitates introducing a number of experiments with same or different settings by writing a few lines of code. Each evolutionary process run by PPCea can also be controlled deterministically or adaptively through parameter and/or operator adaptation. For space consideration, the experimental results of the examples, acting as a proof of feasibility of PPCea, are available at (Liu, 2010). Note that the previous examples also show some EAs cannot be reproduced easily derived from lacking needed attributes, multi-populations, parameters analyzed from an evolutionary process or operators. Section 3 attempts to address such problems from the perspective of EA developers. Lastly, categories of adaptive representation and adaptive fitness are also introduced in (Herrera & Lozano, 1996). They could be also potentially addressed by PPCea. Due to time constraint, they are left as one of our future work.
Conducting parameter control experiments is always a time consuming task due to a variety of possible parameter combinations that may affect the convergence and optimization of an evolution process in different magnitudes. One may concentrate on a limited set of parameters to “de-scope” the problem (Harik & Lobo, 1999). Even so, a sufficient number of experiments are still needed due to heuristic nature of EAs. Per Aristotle, the aforementioned problems are essential difficulties (Brooks, 1987) inherent in EAs. Conversely, code snippets for computing metrics and programming logics for adapting an evolution process on-the-fly based on such metrics still scatter and tangle with other EA source code. Such inflexibility for further extension and inevitability of faulty EA source code are accidental difficulties (Brooks, 1987) that may be solved by the approaches hiding such difficulties.

A DSL is a modeling/programming language that shields accidental difficulties by introducing a higher level abstraction. It has been proved that DSLs may facilitate productivity (up to 10 times improvement), reliability, maintainability, and portability to domain users (Mernik et al., 2005). However, DSLs that are implemented by compiler or interpreter approaches may result in extension and evolution difficulties (Gray et al., 2008). For example, if a new mutation operator is introduced to PPCea, not only new syntax and semantics need to be introduced, but existing source code may be also affected due to inappropriate modularization in many compiler/interpreter-based DSLs including PPCea. Moreover, as mentioned in (Harik & Lobo, 1999), Holland would have never thought of a plentiful number of parameters are presented – Parameters are good for assisting in getting insight of an evolution process or helping control the process. Yet, EA computation may become overwhelmingly slow resulted from parameter explosion. In summary, an objective of this section is to remedy the obstacles derived from the introduction, extension, or evolution of parameters and operators in PPCea.

3.1 Design of PPCea

In order to design and implement PPCea in a manageable and systematic way, DSL patterns (Mernik et al., 2005) and design patterns (Gamma et al., 1995) are followed. Table 1 summarizes the DSL patterns that PPCea applies.
Decision patterns specify when and why a new DSL is essential. In order to provide an adaptable mechanism to solve such parameter control/setting problems, task automation and system front-end decision patterns are chosen. Task automation decision pattern hides the implementation details of EAs. Without browsing and understanding lengthy source code encapsulated in EAs, users omit the complex implementation but concentrate on the parameters and operators that lead to the optimization and/or convergence of EAs. Secondly, PPCEa follows system front-end decision pattern that primarily handles configurations. Time-consuming and error-prone overhead can be reduced or avoided. As for analysis, PPCEa utilizes Feature-Oriented Domain Analysis (Kang et al., 1990) to perform formal domain analysis so that common and variable features of EAs can be systematically identified. With such, PPCEa can be formally defined using denotational semantics (Aho et al., 2007) and designed using design patterns (Gamma et al., 1995). Lastly, interpreter pattern is utilized to implement PPCEa. An overview of PPCEa interpreter is shown in Figure 6.

The interpreter is constructed with the assists of JFlex (Klein, 2010) and Construction of Useful Parsers (CUP) (Hudson, 2010). JFlex is a fast scanner generator for Java whose purpose is to generate a lexer that performs tokenization process for PPCEa programs. CUP is a parser generator that introduces a bottom-up parser that performs syntax analysis. Such a parser may be integrated with user-defined semantics written in Java, accompanying with options to introduce syntax trees and symbol tables. The linguistic elements include commonly-seen constructs such as if-else, loop, and assignment statements as well as expressions and operators to perform necessary parameter adjustments. Additionally, domain-specific elements to describe an EA are presented: init statement initializes a population, callGA statement performs a GA, callES statement performs an ES, resize statement allows population resizing, changeStrategy statement offers the potentials to switch between different operators on-the-fly, context statement determines the operators that constitutes an EA, and require statement determines which domain-specific parameters to be computed. Such parameters are either the results from an evolutionary process that can be also acted as metrics or feedbacks to assist parameter control. There are also miscellaneous statements for various purposes (e.g., IOStatement). Interested readers may find more information on the PPCEa web page (Liu, 2010). All the above linguistic elements

<table>
<thead>
<tr>
<th>Workflow</th>
<th>Pattern</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Decision</td>
<td>Task automation System front-end</td>
<td>When and why to have PPCEa</td>
</tr>
<tr>
<td>Analysis</td>
<td>FODA (Kang et al., 1990)</td>
<td>Find the common and variable features of EAs</td>
</tr>
<tr>
<td>Design</td>
<td>Denotational Semantics Design Patterns (Gamma et al., 1995)</td>
<td>Formally define syntax and semantics of PPCEa PPCEa applies composite, visitor, strategy, decorator and singleton patterns to address introduction, extension, and evolution problems.</td>
</tr>
<tr>
<td>Implementation</td>
<td>Interpreter</td>
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</tr>
</tbody>
</table>

Table 1. The DSL patterns applied in PPCEa
are represented as Java classes embedded with associated semantics. The interpreter currently accepts parameter tuning, deterministic, and adaptive PPCea programs as inputs, as seen at the top of the figure. The outputs, at the bottom of the figure generated by the interpreter, comprise best, average, worst fitness, standard deviation and Euclidean distance (i.e., diversity), entropy (Liu et al., 2009), and the success rates of crossover and mutation, among others. More domain-specific constructs and parameters can be introduced, extended and evolved following the design patterns introduced in the subsequent subsections.

3.2 Evolutionary Algorithm and operator introductions
Since Evolutionary Algorithms (EAs) were coined, there have been a variety of algorithms, operators, and parameters proposed in order to apply to a various number of applications and experiments as well as further improve optimal results and/or convergence rate of such algorithms. For example, different from the general sketches of GAs in (Michalewicz, 1996), Bi-population GA (Tsutsui et al., 1997), aGA (Ghosh et al., 1996), and PROFIGA (Eiben et al., 2004), among others are variations that respectively introduces new algorithmic strategies (e.g., splitting populations into exploration and exploitation modes), new attributes (e.g., ages for individuals) or new operators (population resizing) to facilitate optimization and/or convergence. Additionally, DGEA, Evolution Strategies using Cauchy Distribution (Yao et al., 1999), Particle Swarm Optimization (Kennedy and Eberhart, 2001), and Differential Evolution (Storn & Price, 1997), to name a few, are also categorized in EAs that solve optimization problems from other perspectives. In addition to algorithm
introductions, many variations of existing operators and domain-specific parameters are also introduced (e.g., tournament selection, linear selection, uniform crossover, intermediate crossover, diversity-to-average measure (Ursem, 2002), and cluster entropy (Liu et al., 2009)). PPCea has anticipated such extension and evolution potentials and hence adopted design patterns so that future changes can be addressed with ease.

3.2.1 Evolutionary Algorithm and operator introductions using composite pattern
Because PPCea is developed by following the interpreter/compiler pattern (Mernik et al., 2005), inevitably, the syntactical representation of a PPCea program is expressed as a syntax tree structure (Aho et al., 2007). However, a commonly-seen implementation issue existing in such a tree structure is to deal with the composite-atomic hierarchies (i.e., whole-part hierarchies). For example, PPCea comprises if-else and loop statements that may embrace zero or more composite and/or atomic statements as child nodes (e.g., a nested if-else statement); and conversely, assignment and domain-specific statements are atomic ones that cannot hold any statement nested within their bodies. Because composite statements are derived from recursive productions defined in PPCea grammar (see appendix), they do not possess concrete semantics as other statements do. To reduce implementation complexity, a synergistic objective needs to be fulfilled: How to uniformly treat composite and atomic language constructs in the tree structure (i.e., hide the differences), while distinctions between these two types of language constructs can still be easily made if necessary (i.e., behave as atomic and composite ones as supposed).

A primary objective of composite pattern (Gamma et al., 1995) is to represent whole-part hierarchies and achieve the synergistic objective mentioned above. Figure 7 shows the implementation of composite pattern applied to PPCea interpreter, where IStmt is an abstract class that defines the interface and common behavior of both atomic (i.e., Stmt) and composite (i.e., Series) statements. The advantages of composite pattern mainly lie in the introduction of IStmt and the composition between Series and zero to more IStmt objects, which will be later identified as Series or Stmt concrete objects using polymorphism.

Fig. 7. Composite pattern applied to PPCea interpreter
Composite pattern also follows open-close principle (Meyer, 2000). Such a principle advocates “open for extension and close for modification”: New statements can be added through inheritance; and modification on interface is closed and modification on implementation is isolated to associated methods only. For example, if one requests to introduce callPSO statement for Particle Swamp Optimization (Kennedy & Eberhart, 2001) in PPCea, three steps will be needed at the lexical, syntactical and semantic levels: (1) callPSO needs to be introduced as a token in PPCea.jlex (as seen in Figure 6); (2) A terminal that represents callPSO statement and the associated syntax are requested in PPCea.cup (can be found in Figure 6 too); and (3) Introduce a CallPSOSmt class inherited from CallEASmt. Such a class defines the semantics/algorithms of Particle Swamp Optimization. A new operator that does not relate to any specific algorithm may be also introduced in the same manner. With such, introducing new algorithms or operators will not interfere with the remaining parts of PPCea. Extension and evolution of evolutionary algorithms and operators will be introduced next. Introducing evolutionary operators and parameters comprises the same steps as mentioned. For example, because ResizeStmt and ChangeStrategyStmt are two operators that can be applied to various EAs, they are not encapsulated into specific EA statements. For EA-specific operators, from the implementation’s perspective, they can be introduced as standalone statements like resize and changeStrategy or they can be encapsulated as methods in associated EA statement classes. For the sake of better design to satisfy high cohesion and responsibility driven concepts (Schach, 2010), such operators are encapsulated into EA associated statements.

3.3 Evolutionary Algorithm and operator extensions/evolutions using visitor pattern

Although composite pattern achieves the synergistic objective that allows uniformed treatments and making distinctions on atomic and composite statements when needed, extending or evolving methods encapsulated in EA statements is difficult. (Ironically, they are resulted from following good design principles as mentioned in the previous section). For example, semanticWithConfiguration in CallEASmt is derived from Stmt that defines the semantics of a statement by executing a set of evolutionary operators (e.g., mutation, crossover, and selection). If a new operator, e.g., elite or n-point mutation, is introduced in CallEASmt and invoked by semanticWithConfiguration, all CallEASmt’s subclasses will be affected and recompilation is requested. Additionally, any evolution change to the existing algorithms and operators may be scattered around the entire class, which could be error-prone and resulted in regression faults. Because visitor pattern (Gamma et al., 1995) has succeeded in solving such tree-related problems with composite pattern (e.g., Wu et al., 2005), PPCea adopts visitor pattern so that the aforementioned extension and evolution problem can be solved.

As shown in Figure 8, PPCea introduces a super class, called StmtVisitor, which comprises two subclasses: EASmtVisitor and GenericStmtVisitor, where the former one is to define the semantics of EA-specific operators and the latter one is to define the semantics of generic or non-EA-specific operators. For EA-specific operators, three important evolutionary operators (selection, crossover, and mutation) and two utility operators (eval and getStat) are introduced as EASmtVisitor’s subclasses, where eval is to compute the fitness value of each individual and getStat is to compute the statistical data of an EA that are shown at the bottom of Figure 6. For generic operators, population initialization (init), population resizing
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(resize), strategy changing (changeStrategy) for adapting different evolutionary operators on-the-fly, are introduced. Note that Context class introduced in Figure 8 is initialized by ContextStmt in Figure 7 that will store the current statement (or EA operator) that PPCea interpreter is executing and the resultant population. The usage of this class will be explained in more details in the next subsection.

Fig. 8. Visitor pattern applied to PPCea

Readers who are not familiar with design patterns may find it difficult to see how composite and visitor patterns work together to tackle introduction, extension, and evolution problems by decoupling the syntax tree structure and operators within each statement, while at the same time allow the semantics of each statement as well as the entire program to be functioned correctly. To explain such correlation, the first step is to understand how CUP works with associated semantics written in Java classes. Because CUP is a compiler generator that generates a bottom-up parser, when each non-terminal is traversed, the corresponding Java class is instantiated. All the necessary classes (statements, expressions, and operators as seen in Figure 6) that define associated semantics will be available after the root of the parse tree is traversed. Then the root node will trigger semantics of each line of program to be interpreted and executed. When a statement, called init, is reached, the semanticWithConfiguration method within such a class will invoke a private method, called accept with an object of InitVisitor class passed in (see Figure 7). Within the accept method, visitInitStmt method of InitVisitor class will perform node/statement identification, called double dispatch (Gamma et al., 1995). If the current statement to be executed is init, visitInitStmt will execute the semantics of population initialization accordingly. Similarly, if callGA (or callES) is executed, objects of EvalVisitor, SelectionVisitor, MutationVisitor, CrossoverVisitor, and GetStatVisitor will be passed as parameters of accept method. The semantics defined in each visitor subclass will be executed after callGA statement is identified by double dispatch.

Important advantages that visitor pattern is capable of attacking extension and evolution problem can be expressed as the following three examples:
1. If a new EA-related operator is requested (e.g., clone or repair), we do not introduce an operator in \textit{CallEASmt}, \textit{CallGASmt} or \textit{CallESSmt}, which will result in recompilation of almost the entire composite class hierarchy of Figure 7, as mentioned in the previous subsection. Instead, a subclass of \textit{EASmtVisitor} that defines the semantics of the newly introduced operator can be extended/introduced without affecting the remaining part of PPCea. There is no need to revise any part of JFlex and CUP files of PPCea either;

2. If a new generic operator is needed (e.g., randomize that introduces new random individuals into current population), a subclass that defines such an operator can be inherited from \textit{GenericStmtVisitor} without editing other parts. If the new operator is also requested to be added to PPCea grammar, there is a need to introduce an associated token, syntax, and a subclass of \textit{Stmt} respectively at the lexical, syntactical and semantic levels. Note, however, such extensions will still not interfere other parts of the existing code; and

3. If an existing EA-specific or generic operator is requested to be changed (i.e., evolution), the focus will be only on the specific subclass. Other parts will not be emphasized so the opportunities of regression faults will be minimized.

Although utilizing composite and visitor patterns to solve tree structure problems is not new, our implementation slightly varies the traditional solution and results in an additional advantage that can be observed in Figure 8: Even though introducing an EA at the statement level (e.g., \textit{callGA}) may give readers impression that it is inflexible to control lower level evolutionary operators. Instead, it is a wrong impression! The visitor pattern utilized in PPCea is a variant - it is implemented along with strategy pattern (Gamma et al., 1995), where different evolutionary operators can be controlled through \textit{changeStrategy} at the granularity of operator rather than algorithm. Such implementation avoids possible frequent recompilation while allowing ease of extension and evolution. Namely, only when a new EA, for example, \textit{callPSO}, is introduced, existing subclasses of \textit{EASmtVisitor} need to add and compile a new operator, called \textit{visitCallPSO}. More discussions will be covered in Section 3.5.

### 3.4 Strategic operator adaptation

Section 2.4 introduced three categories of operator adaptation: (1) Adaptation delegated to parameters (i.e., parameter control); (2) Adaptation among different types of operators; and (3) Adaptation among same types of operators. Strategy pattern (Gamma et al., 1995) is applied and integrated with visitor pattern to realize categories (2) and (3).

A primary objective of strategy pattern is to introduce a set of functionalities that can be interchanged upon request. Different kinds of evolutionary operators for GAs and ESs are introduced as subclasses of \textit{Strategy} class in Figures 9 and 10, respectively. For example, we have implemented linear, non-linear, ranking, tournament and roulette wheel selections as subclasses of \textit{GASelectionStrategy}. Similarly, the implementation of one-point and n-point mutation/crossover is defined in the associated subclasses of \textit{GAMutationStrategy/GACrossoverStrategy}. If there is more than one way to initialize population, subclasses that specify such differences can be inherited from \textit{GAInitStrategy}.

Extension and evolution to different algorithms of an operator can be also easily done by introducing subclasses. For example, fitness proportional selection may be introduced as a subclass of \textit{GASelectionStrategy} without interfering the remaining parts of the source code;
and revising existing strategies will be isolated in their own classes – Again, this design follows open-close principle.

Figure 5 in Section 2.4 has presented how to adapt operators using PPCea. The dynamics of such code snippet with respect to strategy pattern is summarized as follows. Figure 10 is a simplified version of Figure 5 for ease of reading. Line 1 sets the default operators for selection, mutation, and crossover into context. A Context object will be instantiated with the Strategy objects of linear selection, 1-point mutation and n-point crossover as parameters.

Fig. 9. Strategy pattern applied to GAs in PPCea

Fig. 10. Strategy pattern applied to ESs in PPCea
Line 2 initializes a population for the GA. Then callGA performs the GA using such strategies. Namely, CallGA statement in Figure 7 will invoke its semanticWithConfiguration method that accepts objects of SelectionVisitor, MutationVisitor, CrossoverVisitor, EvalVisitor, and GetStatVisitor shown in Figure 8. Each visitor object accesses the Context object and executes the associated Strategy object within visitCallGASmt method. For example, the object of SelectionVisitor by default will execute an object of LinearSelection set in Line 1 of Figure 11. Between two if-statements, by using changeStrategy selection operator switches between tournament and rank selections every 10 generations. Additionally, mutation also switches between 1-point and n-point mutations every 10 generations. Crossover, on the other hand, will remain during the entire evolutionary process. Such behaviour is performed based on the following steps: (1) ChangeStrategy statement accepts an object of ChangeStrategyVisitor, which allows new Strategy objects (e.g., rank selection and n-point mutation at generation 10) to interchange with the existing Strategy object (e.g., linear selection and 1-point mutation). After exchange, Context object will execute new strategies. Note that, to avoid class explosion, Singleton pattern (Gamma et al., 1995) is applied to force each operator only has one associated object instantiated all the time. So that when the strategy pairs (tournament selection and n-point mutation) and (rank selection and 1-point mutation) are swapped every 10 generations, there is no new object instantiated, but the existing ones are reused. Halting an operator temporarily is also a feasible solution by replacing the current Strategy object to HaltSelection, HaltMutation, or HaltCrossover, which simply choose not to execute the current strategies. With such, EAs categorized as uni-process approaches in (Liu et al., 2009) can be reproduced using PPCea (e.g., DGEA in Figure 4).

```
1 context (LINEAR_SELECTION, ONE_PT_MUTATION, N_PT_CROSSOVER);
2    //... skip some code
3 callGA;
4 if (( t % 10) == 0) then
5     changeStrategy (TOURNAMENT_SELECTION, N_PT_MUTATION) then
6     fi;
7 if (( t % 20) == 0) then
8     changeStrategy (RANK_SELECTION, ONE_PT_MUTATION) then
9     fi;
10    //...skip some code
```

Fig. 11. A simplified version of Figure 5.

### 3.5 Parameter extension and evolution

Domain-specific parameters are those predefined in a DSL grammar and may facilitate productivity and other advantages of DSLs mentioned before. In PPCea, domain-specific parameters, shown in Table 2, can be categorized in two groups: (1) Parameters that are used for controlling an evolutionary process; and (2) Parameters that are computed at the end of each generation and may be treated as feedback to adjust an evolutionary process. As seen in Table 2, parameters in group (1) are quite diverse. Some may be accessed across the entire project (e.g., Popsize, Maxgen, and Epoch) and others may be used by specific operators (e.g., Alpha, Beta, Miu, and Lamda). From the perspective of compiler/interpreter implementation, this kind of parameters usually already has identities stored in a symbol table (i.e., predefined). When such parameters are initialized by assignment statement, their values are stored in the symbol table accordingly. Whenever and wherever needed, the
values can be accessed through the symbol table. Extension of parameters falling in group (1) usually means introducing new domain-specific notations at the lexical, syntactical and semantic levels, which therefore has the same way of implementing domain-specific statements. Conversely, evolution for such a kind of parameters is usually renaming and

<table>
<thead>
<tr>
<th>Group</th>
<th>Parameter Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1)</td>
<td>Function</td>
<td>Fitness function to be evaluated (Obtained from (Yao et al., 1999))</td>
</tr>
<tr>
<td></td>
<td>Popszie</td>
<td>Number of individuals of a population</td>
</tr>
<tr>
<td></td>
<td>Maxgen</td>
<td>Maximum number of generation for an evolutionary process</td>
</tr>
<tr>
<td></td>
<td>Epoch</td>
<td>Generation stride for parameter control adaptation</td>
</tr>
<tr>
<td></td>
<td>pm</td>
<td>Mutation rate</td>
</tr>
<tr>
<td></td>
<td>pc</td>
<td>Crossover rate</td>
</tr>
<tr>
<td></td>
<td>psr</td>
<td>Stochastic ranking rate</td>
</tr>
<tr>
<td></td>
<td>Alpha</td>
<td>Selection pressure ($\alpha$) for linear/nonlinear selection</td>
</tr>
<tr>
<td></td>
<td>Beta</td>
<td>Selection pressure ($\beta$) for linear/nonlinear selection</td>
</tr>
<tr>
<td></td>
<td>Miu</td>
<td>Selection parameter ($\mu$) for ESs</td>
</tr>
<tr>
<td></td>
<td>Lambda</td>
<td>Selection parameter ($\lambda$) for ESs</td>
</tr>
<tr>
<td></td>
<td>TourQ</td>
<td>Selection parameter for tournament selection</td>
</tr>
<tr>
<td></td>
<td>KMeans</td>
<td>Number of centroids for clustering entropy</td>
</tr>
<tr>
<td>(2)</td>
<td>Best</td>
<td>Best fitness value of all individuals</td>
</tr>
<tr>
<td></td>
<td>Average</td>
<td>Average fitness value of all individuals</td>
</tr>
<tr>
<td></td>
<td>Worst</td>
<td>Worst fitness value of all individuals</td>
</tr>
<tr>
<td></td>
<td>RatioM</td>
<td>Success mutation rate</td>
</tr>
<tr>
<td></td>
<td>RatioC</td>
<td>Success crossover rate</td>
</tr>
<tr>
<td></td>
<td>Stdv</td>
<td>Standard deviation of all individuals</td>
</tr>
<tr>
<td></td>
<td>Euclidean</td>
<td>Euclidean distance of all individuals</td>
</tr>
<tr>
<td></td>
<td>LinearEntropy</td>
<td>Linear Entropy (Liu et al., 2009)</td>
</tr>
<tr>
<td></td>
<td>RoscaEntropy</td>
<td>Rosca Entropy (Liu et al., 2009)</td>
</tr>
<tr>
<td></td>
<td>GaussianEntropy</td>
<td>Gaussian Entropy (Liu et al., 2009)</td>
</tr>
<tr>
<td></td>
<td>FitProEntropy</td>
<td>Fitness Proportional Entropy (Liu et al., 2009)</td>
</tr>
<tr>
<td></td>
<td>ClusterEntropy</td>
<td>Clustering Entropy (Liu et al., 2009)</td>
</tr>
</tbody>
</table>

Table 2. Current domain-specific parameters introduced in PPCEa
changing valid scope based on our experience. Hence, refactoring (Fowler, 1999) may be applied to the lexical, syntactical and semantic levels to tackle evolution. Parameters in group (2) are computational results analyzed from population either after every (several) generation(s) or at the end of an entire evolutionary process. However, not all of such parameters are needed all the time. For example, for parameter tuning approaches, readers may be interested in fitness-related parameters only. Similarly, for non-entropy-driven approaches, one may avoid the computation of the five entropies shown in Table 2 and hence improve the performance. To achieve such a “pay-as-you-go” objective, decorator pattern is applied. As seen in Figure 12, Parameter class is introduced as a super class that applies singleton pattern to avoid more than one instance instantiated during an evolutionary process. Decoratee class is a “decoratee” super class, which means that all the objects of the subclasses inherited from Decoratee are mandatory to be provided by PPCea interpreter. Conversely, DecoratorParameter represents a super class whose subclass objects can be optionally computed upon requests.

The dynamics of how “pay-as-you-go” is achieved may be further observed by the code snippet shown in Figure 13: visitCallGAStmt is a method defined within GetStatVisitor class, accepted by CallGAStmt as described before, whose purpose is to analyze statistical results of a population. Lines 3 to 5 specify the mandatory domain-specific parameters to be computed. From lines 6 to 20, users may determine if any object of Decorator requires computation or not either directly defined in PPCea code (e.g., require(LINEAR_ENTROPY, FITPRO_ENTROPY, ROSCA_ENTROPY);) or through the graphical user interface we developed for PPCea interpreter. For example, if linear, fitness proportional and Rosca entropies are.

Fig. 12. Decorator pattern applied to PPCea.
selected by users (as seen above), when line 21 of Figure 13 is invoked, the calculate methods in Best, Worst, Average, LinearEntropy, FitProEntropy, and RoscaEntropy will be executed in a cascading and sequential order (see the notes in Figure 12).

How does decorator pattern address the extension and evolution problems of parameters in group (2)? For extension, if a new parameter is mandatory, a subclass should be inherited from Decoratee class. Conversely, if users are in charge of the computation necessities of newly introduced parameters, subclasses of Decorator will be introduced. The computational algorithms of the new parameters will be defined in their own calculate methods, along with an invocation to its super class’ calculate method. One drawback of applying Decorator pattern is that when extension (i.e., introducing a new domain-specific parameter of group (2)) occurs, inevitably Figure 13 needs to be revised to incorporate such a change. It is because the purpose of the if-statements is to retrieve the answer of optional parameters that users determine to include. As for evolution, if any computational algorithm of a parameter changes, it is isolated in the associated calculate method.

```java
1 Individual[] visitCallGAStmt(CallGAStmt gaStmt)
2 /* skip the code of retrieving parameters from symbol table ...*/
3 Parameter decorator = new Best(); //required parameter
4 decorator = new Worst(decorator); //required parameter
5 decorator = new Average (decorator); //required parameter
6 if (Linear_Entropy == 1) {
7   decorator = new LinearEntropy(decorator); //optional parameter
8 }
9 if (Gaussian_Entropy == 1) {
10   decorator = new GaussianEntropy(decorator); //optional parameter
11 }
12 if (FitPro_Entropy == 1) {
13   decorator = new FitProEntropy(decorator); //optional parameter
14 }
15 if (Rosca_Entropy == 1) {
16   decorator = new RoscaEntropy(decorator); //optional parameter
17 }
18 if (Cluster_Entropy == 1) {
19   decorator = new ClusterEntropy(decorator); //optional parameter
20 }
21 decorator.calculate(population);
22 return population;
23 }
```

Fig. 13. Decorator pattern applied to PPCEa.

### 3.6 Software metrics

Software metrics (Lincke et al., 2008) are measures that assist in providing comprehensibility of software being assessed. Therefore, the quality of the software can be observed through such metrics. PPCEa utilizes Eclipse Metrics plug-in (Sauer, 2010) to compare the current version implemented with DSL and design patterns and the original version introduced in (Liu et al., 2004), shown in Figure 14.

As seen in the figure, PPCEa using patterns has much higher design and implementation quality in terms of Method lines of code, McCabe cyclomatic complexity (suggested maximum value: 10), and weighted methods per class. All other metrics listed in Figure 14 surpass the suggested maximum values. Namely, the design and implementation of PPCEa with patterns is in good quality and refactoring may not be necessary.
3.7 Potentials of PPCea

The first five subsections discuss how to overcome introduction, extension and evolution problems in four specific levels: (1) Evolutionary algorithms; (2) Evolutionary and generic operators; (3) Functionalities (i.e., strategies) of an operator; and (3) Domain-specific parameters. For (1), composite pattern facilitates the introduction/extension of evolutionary algorithms by introducing EAs as domain-specific statements, subclasses inherited from $IStmt$. For (2), visitor pattern promotes introduction/extension of evolutionary and generic operators by introducing subclasses of $StmtVisitor$. If evolutionary algorithms or its operators evolve, the changes will be isolated in the subclasses of $StmtVisitor$ (or associated strategies), because such subclasses define the semantics of PPCea statements. Additionally, the decision of not introducing EA-specific operators at the PPCea statement level reduces the possibility of frequent changes/recompilation of the $StmtVisitor$ and its subclasses. For (3), strategy pattern assists introduction/extension of different algorithmic strategies of an operator by introducing subclasses of $Strategy$. Evolution of such strategies is also isolated in associated classes. Also, PPCea is capable of adapting with operators on-the-fly under the support of strategy pattern. Lastly, decorator pattern addresses the problem of introduction/extension and evolution of domain-specific parameters by introducing subclasses of $Decorator$ and $Decoratee$. Users are also allowed to determine which parameters to be analyzed so that unnecessary computation cost can be reduced.

To illustrate how a new EA can be introduced or an existing EA can be reproduced, let us use GAVaPS as an example. The algorithm of GAVaPS is as follows.
Based on (Arabas et al., 1994), recombine in Figure 15 performs normal mutation and crossover and then selection chooses offspring from all individuals with equal opportunity. As for remove, it will kill all individuals older than a predefined lifetime threshold. The population will be then resized based on the formula defined in the paper. To realize GAVaPS using PPCea, age attribute needs to be introduced in Individual class. Also, lifetime parameter may be introduced as a parameter in group (1). With such, users can adjust the value of lifetime by PPCea code. Then GAVaPSSelection, inherited from GASelectionStrategy in Figure 9, implements selection mechanism with equal opportunity and increments age if needed. Because there is more than one resize algorithm, a ResizeStrategy subclass may be inherited from Strategy. Then ResizeByAge may be introduced as a subclass of ResizeStrategy that kills all overage individuals and randomly introduces the number of new individuals using the formula if needed. Figure 16 is a pseudo PPCea code to simulate Figure 15 under the assumption all necessary subclasses are introduced in PPCea. Another possible implementation option is to introduce an entire new PPCea statement, called callGAVaPS. Nothing is really different except that callGAVaPS encapsulates all needed Visitor objects, which invoke objects of GAVaPSSelection, OnePointMutation, OnePointCrossover, and ResizeByAge.

```pseudocode
begin
t=0
initialize P(t)
evaluate P(t)
while (not termination-condition) do
    begin
        t = t + 1
        increase the age of each individual by 1
        recombine P(t)
evaluate P(t)
        remove from P(t) all individuals with age greater than the lifetime
    end
end

begin
initialize P(t)
evaluate P(t)
while (not termination-condition) do
    begin
        t = t + 1
        increase the age of each individual by 1
        recombine P(t)
evaluate P(t)
        remove from P(t) all individuals with age greater than the lifetime
    end
end

Fig. 15. The GAVaPS algorithm from (Arabas et al., 1994)

Fig. 16. The pseudo PPCea code that reproduces GAVaPS
```
4. Related work

Evolving Objects (Keijzer et al., 2002) is an evolutionary computation framework that constructs an EA through component composition. Namely, each EA operator/statement is considered as a component and users need to select which specific components (similar to strategies) to be filled in to a specific spot of an evolutionary process. User defined parameters can be introduced to a file, which will be interpreted by the framework. ECJ (Luke et al., 2010) is a Java-based evolutionary computation system that requests users to describe an EA in Java by reusing/invoking a great number of packages for different EA operators. A set of predefined parameters with fixed identities also need to be defined in a specific file, acting like domain-specific parameters in PPCea. ESDL (Dower & Woodward, 2010) is a DSL that introduces SQL-like syntax for users to construct EAs. Name conventions for both EA operators and parameters need to be followed, which is same as PPCea. Because of interoperability advantage of XML, Veenhuis et al. introduced EAML (Veenhuis et al., 2000), a modeling language that utilizes XML to represent an EA. With such, different EA framework/software may introduce their own evolutionary processes by interpreting EAML files. There are also many EA framework or software that the book chapter is not able to fully cover. We leave this part to interested readers.

5. Conclusion

Controlling parameter settings to reach optimization and/or convergence of an EA has been a challenging topic in the evolutionary computation community. Firstly, due to meatheuristic and stochastic nature, there is a need to conduct a sufficient number of experiments of an EA under different parameter settings. Additionally, many practitioners and scholars have put forth various algorithms, operators, and parameters to improve the optimization and/or convergence. Without automatic tools for EA users, conducting EA experiments would become tedious and error-prone. Without capabilities to extend and evolve automatic tools, EA developers would not be able to invent new algorithms, operators, strategies, and parameters. PPCea offers a synergistic solution to address the aforementioned problems from the perspectives of both users and developers. The contributions of PPCea are three-folds: (1) PPCea is an automatic EA tool in a language format that assists EA users to conduct experiments using three parameter setting approaches introduced by Eiben et al.; (2) PPCea is an open-ended EA tool that allows EA developers to introduce, extend and evolve EA constructs in algorithm, operator, strategy and parameter levels; and (3) PPCea offers a fair platform to perform EA comparison – both reproduced algorithms and new algorithms can be described in PPCea code and run under PPCea interpreter.

We have identified several future directions: (1) Multi-populations and multi-objective EAs are missing in current version. With such, more EAs can be reproduced (e.g., parameter-less GA) and invented; (2) As can be seen in Figure 6, PPCea currently cannot handle self adaptation algorithms. How to represent such algorithms and still offer open-end solutions is an emerging issue to tackle; (3) With the metrics from (Črepinšek et al., in press) introduced to PPCea, explicit balance between evolutionary and exploitation in a programmable fashion can be foreseen; and (4) Existing algorithms, operators, and strategies are effective in the individual granularity. Similar algorithms, operators, and
strategies working at the genotypical level may result in finer-grained experiments. With the aforementioned issues resolved, more EA users and developers may be benefited by PPCea.

Appendix: PPCea Grammar

```
Program  ->  genetic Series end genetic
Series   ->  Series Statement ; Statement
Statement ->  if Cond then Series fi | if Cond then Series else Series fi |
           | while Cond do Series end | ID := E |
           | init | callGA | callES | resize( N ) |
           | context( Strategies ) | changeStrategy( Strategies ) |
           | require( Parameters ) |
           | read Ids | write Ids |
           | readFile FileName | writeresult |
           | validateMsg | invalidateMsg
Condition ->  (Expression RelationOp Expression)
Expression ->  Expression Operator Expression | (Expression) |
             | sqrt( Expression ) | exp( Expression ) | Number | Double | ID |
Operator  ->  + | - | * | / | && | ||
RelationOp ->  < | > | <= | >= | != |
Strategies ->  Strategies , Strategy
Selection  ->  LINEAR_SELECTION | NON_LINEAR_SELECTION |
             | TOURNAMENT_SELECTION | RANK_SELECTION |
             | ROULETTEWHEEL_SELECTION | GA_HALT_SELECTION |
             | MIU_AND_LAMDA_SELECTION | MIU_PLUS_LAMDA_SELECTION |
             | ES_HALT_SELECTION
Mutation  ->  ONE_PT_MUTATION | TWO_PT_MUTATION | N_PT_MUTATION |
             | GA_HALT_MUTATION | CEP_MUTATION | FEP_MUTATION |
             | ES_HALT_MUTATION
Crossover  ->  ONE_PT_CROSSOVER | TWO_PT_CROSSOVER | N_PT_CROSSOVER |
             | GA_HALT_CROSSOVER | INTERMEDIATE_CROSSOVER |
             | UNIFORMCROSSOVER | ES_HALT_CROSSOVER
Parameters ->  Parameters , Parameter | ε |
Parameter   ->  RATIO_M | RATIO_C | STDV | EUCLIDEAN | LINEAR_ENTROPY |
             | ROSCA_ENTROPY | GAUSSIAN_ENTROPY | FITPRO_ENTROPY |
             | CLUSTER_ENTROPY
Number      ->  integer
Double      ->  double
Fliname     ->  string
```

6. References


http://www2.cs.tum.edu/projects/cup/
http://www.zimmer.csufresno.edu/~shliu/research/PPCea.html


Evolutionary algorithms are successively applied to wide optimization problems in the engineering, marketing, operations research, and social science, such as include scheduling, genetics, material selection, structural design and so on. Apart from mathematical optimization problems, evolutionary algorithms have also been used as an experimental framework within biological evolution and natural selection in the field of artificial life.

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