Chapter from the book *Electric Vehicles - Modelling and Simulations*
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1. Introduction

The electric vehicle (EV) was conceived in the middle of the previous century. EV’s offer the most promising solutions to reduce vehicular emissions. EV’s constitute the only commonly known group of automobiles that qualify as zero-emission vehicles. These vehicles use an electric motor for propulsion, batteries as electrical-energy storage devices and associated with power electronics, microelectronics, and microprocessor control of motor drives. The doubly fed induction motor (DFIM) is a wound rotor asynchronous machine supplied by the stator and the rotor from two external source voltages. This machine is very attractive for the variable speed applications such as the electric vehicle and the electrical energy production. Consequently, it covers all power ranges. Obviously, the requested variable speed domain and the desired performances depend of the application kinds (Vicatos & Tegopoulos, 2003, Akagi & Sato, 1999, Debiprasad et al., 2001, Leonhard, 1997, Wang & Ding, 1993, Morel et al., 1998 and Hopfensperger et al., 1999).

The use of DFIM offers the opportunity to modulate power flow into and out of the rotor winding in order to have, at the same time, a variable speed in the characterized super-synchronous or sub-synchronous modes in motor or in generator regimes. Two modes can be associated to slip power recovery: sub-synchronous motoring and super-synchronous generating operations. In general, while the rotor is fed through a cycloconverter, the power range can attain the MW order which presents the size power often reserved to the synchronous machine (Vicatos & Tegopoulos, 2003, Akagi & Sato, 1999, Debiprasad et al., 2001, Leonhard, 1997, Wang & Ding, 1993, Morel et al., 1998, Hopfensperger et al, 1999a, 1999b, Metwally et al., 2002, Hirofumi & Hikaru, 2002 and Djurovic et al., 1995). The DFIM has some distinct advantages compared to the conventional squirrel-cage machine. The DFIM can be controlled from the stator or rotor by various possible combinations. The disadvantage of two used converters for stator and rotor supplying can be compensated by the best control performances of the powered systems (Debiprasad et al., 2001). Indeed, the input-commands are done by means of four precise degrees of control freedom relatively to the squirrel cage induction machine where its control appears quite simple. The flux orientation strategy can transform the non linear and coupled DFIM-mathematical model into a linear model leading to one attractive solution for generating or motoring operations (Sergeial, 2003).
It is known that the motor driven systems account for approximately 65% of the electricity consumed in the world. Implementing high efficiency motor driven systems, or improving existing ones, could save over 200 billion kWh of electricity per year. This issue has become very important especially following the economic crisis due to the oil prices raising, the new energy saving technologies are appearing and developing rapidly in this century (Leonhard, 1997, Longya & Wei, 1995, Wang & Cheng, 2004, Zang & Hasan, 1999, David, 1988 and Rodriguez et al., 2002). In this framework, the DFIM continues to find great interest since the birth of the idea of the double flux orientation (Drid et al., 2005a, 2005b). The philosophy of this idea is to get a simpler machine model expression (ideal machine) (Drid et al., 2005a). Consequently, in the same time, we can solve a non linear problem presented by the DFIM control and step up from many digital simulations toward the experimental test by the use of the system dSPACE-1103. This method gives entire satisfaction and consolidates our theory, especially using the Torque Optimization Factor TOF strategy (Drid et al., 2005b). Always the search for a solution has more optimal, us nap leans towards the minimization of the copper losses in the DFIM.

In this chapter we developed an optimization factor Torque Copper Losses Optimization TCLO. The chapter will be organized as follows. The DFIM mathematical model is presented in section 3. In section 4, the robust nonlinear feedback control is exposed. Section 5 concerns the two energy torque optimization strategies TOF and TCLO. In the section 6, simulation results are exposed and comparative illustration shows the performances in energy saving between TOF and TCLO.

2. The DFIM model

Its dynamic model expressed in the synchronous reference frame is given by Voltage equations:

\[
\begin{align*}
\vec{u}_s &= R_s \vec{i}_s + \frac{d}{dt} \vec{\phi}_s + j\omega_s \vec{\phi}_s \\
\vec{u}_r &= R_r \vec{i}_r + \frac{d}{dt} \vec{\phi}_r + j\omega_r \vec{\phi}_r
\end{align*}
\]

(1)

Flux equations:

\[
\begin{align*}
\vec{\phi}_s &= L_s \vec{i}_s + M \vec{i}_r \\
\vec{\phi}_r &= L_r \vec{i}_r + M \vec{i}_s
\end{align*}
\]

(2)

From (1) and (2), the state-all-flux model is written like:

\[
\begin{align*}
\vec{u}_s &= \frac{1}{\sigma T_s} \vec{\phi}_s - \frac{M}{\sigma T_s L_r} \vec{\phi}_r + \frac{d}{dt} \vec{\phi}_s + j\omega_s \vec{\phi}_s \\
\vec{u}_r &= -\frac{M}{\sigma T_r L_s} \vec{\phi}_s + \frac{1}{\sigma T_r} \vec{\phi}_r + \frac{d}{dt} \vec{\phi}_r + j\omega_r \vec{\phi}_r
\end{align*}
\]

(3)

The electromagnetic torque is done as
The copper losses are given as:

\[ P_{cl} = R_s i_s^2 + R_r i_r^2 \] (5)

The motion equation is:

\[ C_e - d = j \frac{d\omega}{dt} \] (6)

In DFIM operations, the stator and rotor mmf's (magneto motive forces) rotations are directly imposed by the two external voltage source frequencies. Hence, the rotor speed becomes depending toward the linear combination of these frequencies, and it will be constant if they are too constants for any load torque, given of course in the machine stability domain. In DFIM modes, the synchronization between both mmf’s is mainly required in order to guarantee machine stability. This is the similar situation of the synchronous machine stability problem where without the recourse to the strict control of the DFIM mmf’s relative position, the machine instability risk or brake down mode become imminent.

3. Nonlinear vector control strategy

3.1 Double flux orientation

It consists in orienting, at the same time, stator flux and rotor flux. Thus, it results the constraints given below by (7). Rotor flux is oriented on the d-axis, and the stator flux is oriented on the q-axis. Conventionally, the d-axis remains reserved to magnetizing axis and q-axis to torque axis, so we can write (Drid et al., 2005a, 2005b)

\[
\begin{align*}
\phi_{sq} &= \phi_s \\
\phi_{rd} &= \phi_r \\
\phi_{sd} &= \phi_{rq} = 0
\end{align*}
\] (7)

Using (7), the developed torque given by (4) can be rewritten as follows:

\[ C_e = k_c \phi_s \phi_r \] (8)

where, \( k_c = \frac{PM}{\sigma L_s L_r} \)

\( \phi_s \) appears as the input command of the active power or simply of the developed torque, while \( \phi_r \) appears as the input command of the reactive power or simply the main magnetizing machine system acting.
3.2 Vector control by Lyapunov feedback linearization

Separating the real and the imaginary part of (3), we can write:

\[
\begin{align*}
\frac{d\phi_{sd}}{dt} &= f_1 + u_{sd} \\
\frac{d\phi_{sq}}{dt} &= f_2 + u_{sq} \\
\frac{d\phi_{rd}}{dt} &= f_3 + u_{rd} \\
\frac{d\phi_{rq}}{dt} &= f_4 + u_{rq}
\end{align*}
\]

(9)

Where \( f_1, f_2, f_3 \) and \( f_4 \) are done as follows:

\[
\begin{align*}
-f_1 &= \gamma_1 \phi_{sd} - \gamma_2 \phi_{rd} - \omega_s \phi_{sq} \\
-f_2 &= \gamma_1 \phi_{sq} - \gamma_2 \phi_{rq} + \omega_s \phi_{sd} \\
-f_3 &= -\gamma_3 \phi_{sd} + \gamma_4 \phi_{rd} - \omega_r \phi_{rq} \\
-f_4 &= -\gamma_3 \phi_{sq} + \gamma_4 \phi_{rq} + \omega_r \phi_{rd}
\end{align*}
\]

(10)

With:

\[
\gamma_1 = \frac{1}{\sigma_{T_s}}; \quad \gamma_2 = \frac{M}{\sigma_{T_s} L_r}; \quad \gamma_3 = \frac{M}{\sigma_{T_s} L_s}; \quad \gamma_4 = \frac{1}{\sigma_{T_r}}
\]

Tacking into account of the constraints given by (7), one can formulate the Lyapunov function as follows

\[
V = \frac{1}{2} \phi_{sd}^2 + \frac{1}{2} \phi_{rq}^2 + \frac{1}{2} (\phi_{sq} - \phi_s)^2 + \frac{1}{2} (\phi_{rd} - \phi_r)^2 > 0
\]

(11)

From (11), the first and second quadrate terms concern the fluxes orientation process defined in (7) with the third and fourth terms characterizing the fluxes feedback control. Where its derivative function becomes

\[
\dot{V} = \phi_{sd} \dot{\phi}_{sd} + \phi_{rq} \dot{\phi}_{rq} + (\phi_{sq} - \phi_s)(\dot{\phi}_{sq} - \dot{\phi}_s) + \\
(\phi_{rd} - \phi_r)(\dot{\phi}_{rd} - \dot{\phi}_r)
\]

(12)

Substituting (9) in (12), it results

\[
\dot{V} = \phi_{sd} (f_1 + u_{sd}) + \phi_{rq} (f_4 + u_{rq}) + \\
(\phi_{sq} - \phi_s) (f_2 + u_{sq} - \phi_s) + \\
(\phi_{rd} - \phi_r) (f_3 + u_{rd} - \phi_r)
\]

(13)

Let us define the following law control as (Khalil, 1996):
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\[
\begin{align*}
    u_{sd} &= -f_1 - K_1 \phi_{sd} \\
    u_{rq} &= -f_4 - K_2 \phi_{rq} \\
    u_{sq} &= -f_2 + \phi_s - K_3 (\phi_{sq} - \phi_s) \\
    u_{rd} &= -f_3 + \phi_r - K_4 (\phi_{rd} - \phi_r)
\end{align*}
\]  

(14)

Hence (14) replaced in (13) gives:

\[
\dot{V} = -K_1 \phi_{sd}^2 - K_2 \phi_{rq}^2 - K_3 (\phi_{sq} - \phi_s)^2 - K_4 (\phi_{rd} - \phi_r)^2 < 0
\]  

(15)

The function (15) is negative one. Furthermore, (14) introduced into (9) leads to a stable convergence process if the gains \(K_i\) (i=1, 2, 3, 4) are evidently all positive, otherwise:

\[
\begin{align*}
    \lim_{t \to +\infty} \phi_{sd} &= 0 \\
    \lim_{t \to +\infty} \phi_{rq} &= 0 \\
    \lim_{t \to +\infty} (\phi_{rd} - \phi_r^*) &= 0 \\
    \lim_{t \to +\infty} (\phi_{sq} - \phi_s^*) &= 0
\end{align*}
\]  

(16)

In (16), the first and second equations concern the double flux orientation constraints applied for DFIM-model which are define above by (7), while the third and fourth equations define the errors after the feedback fluxes control. This latter offers the possibility to control the main machine magnetizing on the d-axis by \(\phi_{rd}\) and the developed torque on the q-axis by \(\phi_{sq}\).

### 3.3 Robust feedback Lyapunov linearization control

In practice, the nonlinear functions \(f_i\) involved in the state space model (9) are strongly affected by the conventional effect of induction motor (IM) such as temperature, saturation and skin effect in addition of the different nonlinearities related to harmonic pollution due to the supplying converters and to the noise measurements. Since the control law developed in the precedent section is based on the exact knowledge of these functions \(f_i\), one can expect that in real situation the control law (14) can fail to ensure flux orientation. In this section, our objective is to determine a new vector control law making it possible to maintain double flux orientation in presence of physical parameter variations and measurement noises. Globally we can write:

\[
f_i = \hat{f}_i + \Delta f_i
\]  

(17)

On, \(\hat{f}_i\) : True nonlinear feedback function (NLFF)  
\(f_i\) : Effective NLFF  
\(\Delta f_i\) : NLFF variation around \(f_i\).

Where: \(i = 1, 2, 3\) and 4.
The $\Delta f_i$ can be generated from the whole parameters and variables variations as indicated above. We assume that all the $\Delta f_i$ are bounded as follows: $|\Delta f_i| < \beta_i$ where are known bounds. The knowledge of $\beta_i$ is not difficult since, one can use sufficiently large number to satisfy the constraint $|\Delta f_i| < \beta$.

The $\Delta f_i$ can be generated from the whole parameters and variables variations as indicated above. Replacing (17) in (9), we obtain

$$
\begin{align*}
\frac{d\phi_{sd}}{dt} &= \dot{\phi}_1 + \Delta f_1 + u_{sd} \\
\frac{d\phi_{sq}}{dt} &= \dot{\phi}_2 + \Delta f_2 + u_{sq} \\
\frac{d\phi_{rd}}{dt} &= \dot{\phi}_3 + \Delta f_3 + u_{rd} \\
\frac{d\phi_{rq}}{dt} &= \dot{\phi}_4 + \Delta f_4 + u_{rq}
\end{align*}
$$

(18)

The following result can be stated.

**Proposition:** Consider the realistic all fluxes state model (18). Then, the double fluxes orientation constraints (7) are fulfilled provided that the following control laws are used

$$
\begin{align*}
u_{sd} &= -\dot{\phi}_1 - K_{11} \phi_{sd} - K_{12} \phi_{rd} - K_{13} \phi_{rq} - K_{14} \phi_{sq} - K_{15} \phi_{r} \\
u_{rq} &= -\dot{\phi}_4 - K_{21} \phi_{rd} - K_{22} \phi_{rq} - K_{23} \phi_{sq} - K_{24} \phi_{s} \\
u_{sq} &= -\dot{\phi}_2 + \phi_{s} - K_{31} \phi_{sd} - K_{32} \phi_{rd} - K_{33} \phi_{rq} - K_{34} \phi_{sq} \\
u_{rd} &= -\dot{\phi}_3 + \phi_{r} - K_{41} \phi_{sd} - K_{42} \phi_{rd} - K_{43} \phi_{rq} - K_{44} \phi_{sq}
\end{align*}
$$

(19)

where $K_{ii} \geq \beta_i$ and $K_{ii} > 0$ for $i=1; 4$.

**Proof.** Let the Lyapunov function related to the fluxes dynamics (18) defined by

$$
V_1 = \frac{1}{2} \phi_{sd}^2 + \frac{1}{2} \phi_{rd}^2 + \frac{1}{2} \phi_{sq}^2 + \frac{1}{2} \phi_{rq}^2 + \frac{1}{2} (\phi_{r} - \phi_{r})^2 > 0
$$

(20)

One has

$$
\dot{V}_1 = \phi_{sd} \left( \Delta f_1 - K_{11} \phi_{sd} \right) + \phi_{rd} \left( \Delta f_3 - K_{33} \phi_{sq} \right) + \phi_{rq} \left( \Delta f_2 - K_{22} \phi_{rq} \right) + \phi_{sq} \left( \Delta f_3 - K_{33} \phi_{sq} \right) + \phi_{r} \left( \Delta f_4 - K_{44} \phi_{rd} \right) + \dot{\phi}_{s} \left( \phi_{s} - \phi_{s} \right) + \dot{\phi}_{r} \left( \phi_{r} - \phi_{r} \right) + \dot{\phi}_{d} \left( \phi_{d} - \phi_{d} \right) + \dot{\phi}_{q} \left( \phi_{q} - \phi_{q} \right)
$$

(21)

where $\dot{V}$ is given by (15). Hence the $\Delta f_i$ variations can be absorbed if we take:
The latter inequalities are satisfied since $K_i > 0$ and $|\Delta f_i| < \beta_i < K_{ii}$.

Finally, we can write:

$$\dot{V}_1 < \dot{V} < 0$$

Hence, using the Lyapunov theorem (Khalil, 1996), we conclude that

$$\lim_{t \to +\infty} \phi_{sd} = 0$$
$$\lim_{t \to +\infty} \phi_{rq} = 0$$
$$\lim_{t \to +\infty} (\phi_{rd} - \phi_r^*) = 0$$
$$\lim_{t \to +\infty} (\phi_{sq} - \phi_s^*) = 0$$

The design of these robust controllers, resulting from (19), is given in the following figure 2.

The indices $w$ can be: $sd$, $sq$, $rd$ and $rq$, ($i = 1, 2, 3$ and $4$).

4. Energy optimization strategy

In this section, we will explain why and what is the optimization strategy used in this work. Fig. 1 illustrates the problem which occurs in the proposed DFIM vector control system when the machine magnetizing excitation is maintained at a constant level.

4.1 Why the energy optimization strategy?

Considering an iso-torque-curve (hyperbola form), drawn from (8) for a constant torque in the $(\phi_r, \phi_r)$ plan and lower load machine (Fig.1), on which we define two points $A$ and $B$, respectively, corresponding to the two machine magnetizing extreme levels. Theses points concern respectively an excited machine ($\phi_r = 1\text{Wb} = \text{Const}$) and an under excited machine ($\phi_r = 0.1\text{Wb} = \text{Const}$). Both points define the steady state operation machine or equilibrium points. The machine rotates to satisfy the required reference speed acted by a given slope speed acceleration $\alpha = \frac{d\Omega}{dt} = \text{Const}$. So, the machine in both magnetizing cases must develop a transient torque such as:
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Fig. 1. Illustration of the posed problem in the DFIM control system with constant excitation.

\[ C_{eT} = C_{r0} + J \frac{d\Omega}{dt} = C_{r0} + J\alpha \]  \hspace{1cm} (25)

On the same graph, we define a second iso-torque-curve \( C_{eT} = \text{Const} \) in the \((\phi_s, \phi_r)\) plan. This curve is a transient one on which we place two transient points \( A' \) and \( B' \). Here we distinguish the first transitions \( A - A' \) and \( B - B' \) due to the acceleration set, respectively for each magnetizing case. Both transitions are rapidly occurring in respect to the adopted control.

Once the machine speed reaches its reference, the inertial torque is cancelled (\( \alpha = 0 \)), then the developed torque must return immediately to the initial load torque \( C_{ro} \) characterized by the second transitions \( A' - A \) and \( B' - B \) towards the preceding equilibrium points \( A \) and \( B \). One can notice that during the transition \( B - B' \), corresponding to the under excited machine, the stator flux can attain very high values greater than the tolerable limit \( \phi_{s\text{max}} \), and can tend to infinite values if the load torque \( C_{ro} \) tends to zero. So the armature currents expressed by the following formula deduced from (2) and (7) are strongly increased and can certainly destruct the machine and their supplied converters.

\[
\begin{align*}
\bar{i}_s &= \lambda \phi_r + j\gamma \phi_s \\
\bar{i}_r &= \chi \phi_r + j\lambda \phi_s
\end{align*}
\]  \hspace{1cm} (26)

Where, \( \lambda = -\frac{M}{\sigma L_s L_r} \); \( \gamma = \frac{1}{\sigma L_s} \); \( \chi = \frac{1}{\sigma L_r} \).

In the other hand, for the case \( A \) (excited machine), if the \( A - A' \) transition remains tolerable, the armature currents can present prohibitory magnitude in the steady state operation due to the orthogonal contribution of stator and rotor fluxes at the moment that the machine is sufficiently excited. The steady state armature currents can be calculated by (26), where we can note the amplification effect of the coefficients \( \lambda, \gamma \) and \( \chi \).
4.2 Torque optimization factor (TOF) design

In the previous sub-section, the problem is in the transient torque, especially when the machine is low loaded. So it becomes very important to minimize the torque transition such as (Drid, 2005b):

\[
\frac{dC_e}{dt} \rightarrow 0
\]

(27)

where,

\[
dC_e = \frac{\partial C_e}{\partial \phi_S} d\phi_S + \frac{\partial C_e}{\partial \phi_R} d\phi_R
\]

(28)

This condition should be realized respecting the stator flux constraint given by

\[
\phi_S \leq \phi_{S\text{ max}}
\]

(29)

In this way the rotor and stator fluxes, though orthogonal, their modulus will be related by the so-called TOF strategy which will be designed from the resolution of the differential equations (27-28) with constraint (29) as follows:

\[
\begin{align*}
\dot{\phi}_S \phi_R + \dot{\phi}_R \phi_S &= 0 \\
\phi_S &\leq \phi_{S\text{ max}}
\end{align*}
\]

(30)

from (29) we can write

\[
-\dot{\phi}_S \phi_R = \dot{\phi}_R \phi_S \leq \dot{\phi}_R \phi_{S\text{ max}}
\]

(31)

thus,

\[
-\frac{\dot{\phi}_S}{\phi_{S\text{ max}}} \leq \frac{\dot{\phi}_R}{\phi_R}
\]

(32)

the resolution of (32) leads to

\[
-\frac{\phi_S}{\phi_{S\text{ max}}} + C \leq \ln \phi_R
\]

(33)

where \(C\) is an arbitrary integration constant, therefore

\[
\phi_R \geq e^{\frac{\phi_S}{\phi_{S\text{ max}}}-C}
\]

(34)

Since, the main torque input-command in motoring DFIM operation is related to the stator flux, it becomes dependent on the speed rotor sign and thus we can write

\[
\phi_{S\Omega} = \phi_S \operatorname{sgn}(\Omega) = \begin{cases} 
\phi_S & \text{if } \Omega > 0 \\
-\phi_S & \text{if } \Omega < 0
\end{cases}
\]

(35)
with (35), (34), the rotor flux may be rewritten as follows

\[ \phi_r = e^{\frac{\phi_{sq}}{\phi_{s,max}}} - C \]  

(36)

The resolution of (32) gives place to the arbitrary integration constant C from which the TOF-relationship (36) can be easily tuned. This one can be adjusted by a judicious choice of the integration constant, while figure 2 presents TOF effect on armature DFIM currents with C-tuning. Note that this method offers the possibility to reduce substantially the magnitude of the armature currents into the machine and we can notice an increase in energy saving. Hence using TOF strategy, we can avoid the saturation effect and reduce the magnitude of machine currents from which the DFIM efficiency could be clearly enhanced.

![Fig. 2. TOF effect on armature DFIM currents](image)

**4.3 Torque-copper losses optimization (TCLO) design**

In many applications, it is required to optimize a given parameter and the derivative plays a key role in the solution of such problems. Suppose the quantity to be minimized is given by the function \( f(x) \), and \( x \) is our control parameter. We want to know how to choose \( x \) to make \( f(x) \) as small as possible. Let’s pick some \( x_0 \) as the starting point in our search for the best \( x \). The goal is to find the relation between fluxes which can optimize the compromise between torque and copper losses in steady state as well as in transient state, (i.e. for all \( |C_e| \) find \( (\phi_r, \phi_s) \) let \( \min(P_{cl}) \) (Drid, 2008). From (5), (8) and (26), the torque and copper losses can be written as:

\[
\begin{align*}
C_e &= k_c \phi_r \phi_s \\
P_{cl} &= a_1 \phi_r^2 + a_2 \phi_s^2
\end{align*}
\]  

(37)
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\[ a_1 = \left( \frac{R_r}{(\sigma L_r)^2} + \frac{R_s M^2}{(\sigma L_r L_s)^2} \right) \]

with:

\[ a_2 = \left( \frac{R_r M^2}{(\sigma L_r L_s)^2} + \frac{R_s}{(\sigma L_s)^2} \right) \]

The figure 3 represents the layout of (37) for a constant level of torque and copper losses in the \((\phi_s, \phi_r)\) plan. These curves present respectively a hyperbole for the iso-torque and ellipse for iso-copper-losses. From (37) we can write:

\[ a_1 k_c^2 \phi_r^4 - k_c^2 \phi_r^2 \Delta P_{cl} + a_2 C_{el}^2 = 0 \]  

(38)

To obtain a real and thus optimal solution, we must have:

\[ \Delta = k_c^4 \Delta P_{cl}^4 - 4 a_1 k_c^2 a_2 C_{el}^2 = 0 \]  

(39)

The equation (39) represents the energy balance in the DFIM for one working DFIM point as shown in fig.3. Then, one can write:

\[ \Delta P_{cl} = \frac{4 a_1 a_2 C_{el}^2}{k_c^2} \]  

(40)

This equation shows the optimal relation between the torque and the copper losses.

![Fig. 3. The iso–torque curves and the iso–losses curves in the plan \((\phi_s, \phi_r)\)](image-url)
4.4 Finding minimum Copper-losses values

The Rolle’s Theorem is the key result behind applications of the derivative to optimization problems. The second derivative test is used to finding minimum point.

We can rewrite (37) as:

\[
\phi_s = \frac{C_e}{k_c \phi_r} \\
P_{cl} = a_1 \phi_r^2 + a_2 \frac{C_e^2}{k_c \phi_r^2} = a_1 k_c^2 \phi_r^4 + a_2 C_e^2 \\
\]

(41)

The computations of the first and second derivatives show that the critical point is given by:

\[
\phi_{rc} = \pm \left(\frac{C_e^2 a_2}{a_1 k_c^2}\right)^{\frac{1}{4}}
\]

(42)

For which:

\[
\frac{d^2 P_{cl}(\phi_{rc})}{d \phi_r^2} = \frac{2a_1 k_c^2 \phi_{rc}^4 + 6a_2 C_e^2}{k_c^2 \phi_{rc}^4} = 8a_1 > 0
\]

(43)

We can see that the second derivative is positive and conclude that the critical point is a relative minimum.

5. Simulation

Figure 4 illustrates a general block diagram of the suggested DFIM control scheme. Here, we can note the placement of optimization block, the first estimator-block which evaluates torque and the second estimator-block which evaluates firstly the modulus and position fluxes, respectively \(\phi_s, \phi_r, \rho_s, \rho_r\), from the measured currents using (2) and secondly the feedback functions \(f_1, f_2, f_3, f_4\) given by (10). Optimization process allows adapting the main flux magnetizing defined by rotor flux to the applied load torque characterized by the stator flux. With the analogical switch we can select the type of the reference rotor flux. The switch position 1, 2 gives respectively TCLO and TOF for optimized operation and the position 3 for a magnetizing constant level.

The Figure 5 shows the speed response versus time according to its desired profile drawn on the same figure. Figure 6 illustrate the fluxes trajectory of the closed-loop system. It moves along manifold toward the equilibrium point. We can notice the stability of the system. Figures 7 and 8 show respectively the stator and the rotor input control voltages versus time during the test. Figure 9 present the copper losses according to the stator flux variations in steady state operation and we can see the contribution of the TCLO compared to the TOF. Finally figure 10 present the dissipated energy versus time from which we can observe clearly the influence of the three switch positions on the copper losses in transient state. We can conclude that the TCLO is the best optimization.
Fig. 4. General block diagram of control scheme

Fig. 5. Speed response
Fig. 6. Fluxes trajectories of the closed-loop system

Fig. 7. The input control stator voltage response in the stator reference frames with TCLO
Fig. 8. The input control rotor voltage response in the stator reference frames with TCLO

Fig. 9. Minimized copper losses in steady state operation with TOF and TCLO
6. Conclusion

In this chapter was presented a vector control intended for doubly fed induction motor (DFIM) mode. The use of the state-all-flux induction machine model with a flux orientation constraint gives place to a simpler control model. The stability of the nonlinear feedback control is proven using the Lyapunov function.

The simulation results of the suggested DFIM system control based on double flux orientation which is achieved by the proposed DFIM control demonstrates clearly the suitable obtained performances required by the references profiles defined above. The speed tracks its desired reference without any effect of the load torque. Therefore the high control performances can be well affirmed. To optimize the machine operation we chose to minimize the copper losses. The proposed TCLO factor performs better than the already designed TOF. Indeed, the energy saving process can be well achieved if the magnetizing flux decreases in the same way as the load torque. It results in an interesting balance between the core losses and the copper losses into the machine, so the machine efficiency may be largely improved. The simulation results confirm largely the effectiveness of the proposed DFIM control system.

7. Appendix

The machine parameters are:
Rs =1.2 Ω; Ls =0.158 H; Lr =0.156 H; Rr =1.8 Ω; M =0.15 H; P =2 ; J = 0.07 Kg.m² ; Pn = 4 Kw ; 220/380V ; 50Hz ; 1440tr/min ; 15/8.6 A ; cosϕ = 0.85.

8. Nomenclature

s, r Rotor and stator indices.
d, q Direct and quadrature indices for orthogonal components
\( \bar{x} \) Variable complex such as: \( \bar{x} = \text{Re}[\bar{x}] + j \text{Im}[\bar{x}] \).
It can be a voltage as \( \bar{u} \), a current as \( \bar{i} \) or a flux as \( \bar{\phi} \).

\( \bar{x} \): Complex conjugate

\( R_s, R_r \): Stator and rotor resistances

\( L_s, L_r \): Stator and rotor inductances

\( T_s, T_r \): Stator and rotor time-constants \((T_s = L_s / R_s)\)

\( \sigma \): Leakage flux total coefficient \((\sigma = 1 - M^2 / L_r L_s)\)

\( M \): Mutual inductance

\( \theta \): Absolute rotor position

\( p \): Number of pairs poles

\( \delta \): Torque angle

\( \rho_s, \rho_r \): Stator and rotor flux absolute positions

\( \omega \): Mechanical rotor frequency \((\text{rd/s})\)

\( \Omega \): Rotor speed \((\text{rd/s})\)

\( \omega_s \): Stator current frequency \((\text{rd/s})\)

\( \omega_r \): Induced rotor current frequency \((\text{rd/s})\)

\( J \): Inertia

\( d \): Unknown load torque

\( C_e \): Electromagnetic torque

\( \sim \): Symbol indicating measured value

\( \wedge \): Symbol indicating the estimated value

\( ^* \): Symbol indicating the command value

DFIM: Doubly Fed Induction Machine

TOF: Torque Optimization Factor

TCLO: Torque Copper Losses Optimization

9. References


In this book, modeling and simulation of electric vehicles and their components have been emphasized chapter by chapter with valuable contribution of many researchers who work on both technical and regulatory sides of the field. Mathematical models for electrical vehicles and their components were introduced and merged together to make this book a guide for industry, academia and policy makers.

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