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Metal Foam Effective Transport Properties

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1. Introduction

Solid foams are a relatively new class of multifunctional materials that present attractive thermal, mechanical, electrical and acoustic properties. Moreover, they also promote mixing and have excellent specific mechanical properties. They are widely quoted to present a random topology, high open porosity, low relative density and high thermal conductivity of the cell edges, large accessible surface area per unit volume (Ashby et al., 2000). Usually, geometric properties such as high tortuosity and high specific surface are proposed to explain their properties, although fluid tortuosity is close to 1 and specific surface is usually smaller than 10000m\textsuperscript{2}/m\textsuperscript{3}. They are nowadays proposed for their use in numerous applications such as compact heat exchangers, reformers, biphasic cooling systems and spreaders. They are also used in high-power batteries for lightweight cordless electronics, and catalytic field application such as fuel cells systems (Catillon et al., 2004; Dukhan et al., 2005; Mahjoob & Vafai, 2008; Tadrist et al., 2004). In this chapter, we expose experimental and numerical tools to determine effective transport properties of metal foam for mono-and-biphasic flow.

2. Representative volume element

Definitions of a continuous medium equivalent to the real porous structure, as well as the definition of the applicability level of the macroscopic model, constitutes a tricky problem that has long been debated (Auriault, 1991; Baveye & Sposito, 1984; Marle, 1982; Quintard & Whitaker, 1991) among others. The forms of the used phenomenological laws have been obtained from correlations resulting from experiments and not from physical laws. The valuable expressions are much diversified and the choice for one or the other is only justified when compared with specific experiments. We thus consider, classically, that the foam could be assimilated to a homogeneous equivalent medium (Dullien, 1992). Thus, each measured quantities will not describe the foam sample itself, but rather a homogeneous media which has the same properties. There is yet no theoretical evidence to justify this assumption. Thus, we only consider that this condition is satisfied when the considered phenomenon occurs on a sufficient distance. Determination of a Rve is thus evaluation of the relevant distance for the considered observation.
2.1 Rve determination procedure
A definition of the Rve was proposed by (Drugan & Willis, 1996): “It is the smallest material volume element of the composite for which the usual spatially constant (overall modulus) macroscopic constitutive representation is a sufficiently accurate model to represent mean constitutive response”. We propose to qualitatively identify Rve associated to both geometrical and physical macroscopic properties using a pragmatic statistical approach (Kanit et al., 2003).

The property considered is calculated for a large number of fixed-size boxes (n=100 to 1000) randomly located in the sample. We obtain a distribution of mean values for a given size of box. We then studied the influence of the box size on the standard deviation of these distributions. The size of the Rve is defined as the volume for which the distribution of the mean values present a standard deviation below a given threshold. We could also define the size of the Rve as the volume for which the maximum difference is below a given threshold; it would be a much robust criteria since Standard statistics could hide a Maximum Difference (MD) far greater than standard deviation (Std Dev). In our case both quantities vary similarly and thus Std. Dev threshold is sufficient.

For all studied quantities, the standard deviation decrease roughly exponentially with the box size. For a Std Dev of 10% we observe that maximum differences (MD) between two realizations could exceed 25%. At 5% Std Dev, MD stay around 15%. This value is indeed rather important but the available samples do not permit to be more precise.

To compare the different foams, the size of the box was normalized by the pore diameter. Moreover the standard deviation and the maximum difference are normalized with the mean value of the property studied for the considered foam.

2.2 Geometrical Rve
Porosity and specific surface are estimated from the 3D density images obtained with X-ray tomography. Porosity is trivially obtained by counting the voxels of the different phase. The "Marching Cubes" algorithm uses the 3D density images to obtain the mesh of solid surface (Lorensen & Cline, 1987). The mesh data triangles are ordered so that each triangle is included into a unique cubic mesh composing the 3D sample. Once the mesh has been generated for the sample, it is then easy to calculate a specific surface area within a small volume taken in the sample: the cubes composing the volume are retrieved and the surface area of the triangles contained in these cubes is summed.

Figure 1 shows the influence of the box size on standard deviation and on the maximum difference of both porosity (a) and specific surface (b) area distribution. For porosity we can define a unique Rve for these samples. We observe similar standard deviation variations for several manufacturers. According our 5% criteria the Rve of porosity is a cube of 0.7 pore diameter side.

Similar behavior in standard deviation variation is observed for the Rve of specific surface. A single size of Rve can be defined for all these samples: similar standard deviation variations are also observed for the foams from different manufacturers. According to our 5% criteria, the Rve for specific surface is a cube roughly 3 dp in side length.

The absence of differences between foams from different manufacturer can be explained by the fact that the manufacturing processes are roughly similar (replication of polymer foam) and lead to the same solid volume fraction (porosity around 90% is a manufacturer goal). Plateau law gives globally struts shape but local variations in the cells organization induce different shapes of struts inter-connection and strut cross section (roughly curved triangle).
These perturbations may be due to several effects (gravity, drainage, deposition, casting...) during manufacturing process. This gives insight on the fact that specific surface REV size is far greater than porosity one, but further investigation needed to clarify this point.

Fig. 1. Geometrical REV determination. (a) porosity. (b) specific surface. Hollow symbol: Std. dev.; Filled ones: max. difference.

2.3 Physical REV
Concerning velocity, the method for obtaining REV is the same as for geometrical properties. But determining the local averaged pressure gradient from the pressure field is more difficult (Barrere, 1990; Renard et al., 2001). Even if local pressure gradient are not fully perpendicular to main flow direction (Figure 2), this effect is small and we consider that macroscopic pressure is constant on planes perpendicular to the main flow direction (established flow in an isotropic medium). Thus, we calculate mean pressure on planes perpendicular to the main flow direction at several locations, and we estimate the slope of the mean pressure variation by linear regression. We have chosen the coefficient of determination $R^2$ of the linear regression as a pertinent parameter and we keep our 5% criteria to establish the REV size. We made these calculations for different sizes of a randomly located box in the medium and we studied the influence of the box volume on the coefficient of determination $R^2$ of the linear regression.

Fig. 2. Physical RVE determination. (a) velocity. Hollow symbols: standard deviation; Filled one: Maximum error. (b) Hollow symbol: pressure gradient; filled ones: regression coefficient. Calculations using either Finite Volume or Lattice Botzmann approach.
Figure 2.a shows the influence of the box size on standard deviation and on the maximum difference of mean velocity. To establish RVE for the mean velocity value, we used the velocity field obtained from the computations (§3.3). No clear influence of the Reynolds number on RVE size can be identified for both methods on the studied range. We observe that for simulations, a box of 3 dp side seems to be sufficient to define the mean velocity for these Reynolds numbers.

Figure 2.b presents the estimation of the pressure gradient by a linear regression and its coefficient of determination $R^2$, for different volumes and different Reynolds numbers. The estimate of the pressure gradient is quite constant for a box 3 pore diameters in size and the associated coefficient of regression $R^2$ is good (> 0.99). As a result, 3 pore diameters are sufficient to establish pressure drop Rve.

3. Single-phase flow

3.1 Flow law

It is well known that flows at very low flow rates through a porous medium are governed by Darcy’s law (Darcy, 1856).

$$\frac{dP}{dz} = \frac{\mu}{K} u$$

(1)

Where $dP/dz$ is the pressure gradient along the main flow z-direction, $\mu$ the dynamic viscosity, $u$ is Darcy’s or the seepage velocity and $K$ (m²) is the permeability (or Darcy’s permeability) of the medium.

For homogeneous porous media, a nonlinear relationship between the pressure drop and the flow rate characterize “high-velocity” flows. At high Reynolds number (strong inertia regime), the empirical Forchheimer equation is used to account for the deviation from Darcy’s law (incompressible fluid) (Eq.2) or extended to compressible fluid and expressed as a function of mass flow rate (Eq.3).

$$\frac{dP(z)}{dz} = \left(\frac{\mu}{K} u + \beta\rho u^2\right)$$

(2)

$$\frac{dP(z)\rho(z)}{dz} = \left(\frac{\mu}{K} \eta + \beta\eta^2\right)$$

(3)

Where $\rho$ (kg.m⁻³) is the fluid density, $\eta$ (kg.m⁻².s⁻¹) the mass flow rate and $\beta$ (m⁻¹) the inertia factor or the non-Darcy flow coefficient. In this formulation the Brinkman correction is neglected. That means that the pressure drop is considered as the sum of two terms: viscous ($u$, Darcy law) and inertia ($u^2$) terms.

Several authors have shown that the onset of the non-linear behavior (that is sometime called the weak inertia regime) may be described by a cubic law (Firdaous et al., 1997; Mei & Auriault, 1993; Wodie & Levy, 1991):

$$\frac{dP}{dz} = \frac{\mu}{K} u + \gamma \frac{\rho^2}{\mu} u^3$$

(4)
Where $\gamma$ is a dimensionless parameter for the non-linear term. Comparing equations (4) and (2) shows up that $\beta(u) = \frac{\gamma \rho \mu}{\mu}$ could be described as a velocity dependent inertial coefficient. This expression is proposed to describe flow in porous media at intermediate Reynolds number (typically $10 < \text{Re} < 10000$). This equation was obtained by numerical simulations in a two-dimensional periodic porous medium, and by using the homogenization technique for an isotropic homogeneous 3D porous medium. In spite of the numerous attempts to clarify the physical reasons for the non-linear behavior described above, neither Forchheimer equation (2) nor the weak inertia equation (4) have received any physical justification (Fourar et al., 2004). The pressure gradient across the foam is thus a function of system geometry (porosity, pore and ligament size...), as well as physical properties of the fluid phase (viscosity, density). On the other hand, for all three formulations of pressure gradient through the porous media, $K$, $\beta$ and $\gamma$ are intrinsic characteristic of the solid matrix alone and are, thus, independent of the fluid nature.

3.2 Experimental set up

The experimental approach is based on stationary pressure profile measurement in a channel filled with metallic foam of various grade or material and crossed by controlled flow rates. Several foam samples with different characteristics (grade from 5 up to 100 PPI) of copper, nickel, or allied nickel are studied. This experimental set-up is designed, to study the impact of the solid matrix on flow phenomena in the foam in both single-phase and adiabatic two-phase flow conditions. This apparatus consists of three main parts: test section, fluid loop and data acquisition system as shown on Figure 3. Because of the manufacturing methods, many types of foam are produced as flat sheets. Thus, the thickness of samples, about 5 up to 10 pores here, may not be sufficient to insure validity of the hypothesis that an equivalent homogeneous material could describe them. However, our results show nothing that could invalidate this assumption and all available literature data use this hypothesis. For tested cases, sample thickness along the main flow axis is not lower than 2.5mm for the 100PPI ($D_p=500\mu m$) and 2.5cm for the 10 PPI samples ($D_p=5000\mu m$).

![Fig. 3. Experimental set-up for single-phase and adiabatic two-phase flow laws characterization (Bonnet et al., 2008).](www.intechopen.com)
The test section (250 mm length, 50 mm wide and adjustable height) is instrumented with 12 pressure sensors (Sensym®, sensitivity 2.6 µV per Pa) placed every centimetre along the main flow axis. Additional pressure sensors are placed along 3 lines perpendicular to the flow direction to assess the one-dimensional nature of the flow. Foam samples (whose lengths vary from 130 up to 200 mm) are placed in the central part of the channel in order to keep a tranquilization zone upstream and downstream of the sample. Test section is placed horizontally in order to avoid uncertainties due to hydrostatic effects (Madani et al., 2007).

The liquid fluid loop is constituted by a storage tank (50 l capacity) and a variable velocity gear pump which can give a constant flow rate in the range of 0–10⁻⁴ m³ s⁻¹ independently of pump downstream conditions. Constant air flow (range 0-4 10⁻³ Nm³ s⁻¹) is obtained by using a compressor and a pressure regulation valve. The test section is connected, downstream, to a separator which is installed for the two-phase flow experiments. The liquid flows by gravity down the storage tank while the air is simply released to atmosphere. A weighted tank could be inserted in the liquid loop to assess the mass flow rate. Liquid flow rate is monitored (upstream of the test section) using two turbine flow meters (Mac-Millan®) for optimal accuracy over the full range of experiments. The first one works in the range of 3.33 10⁻⁵ - 8.10⁻⁵ m³s⁻¹ and the other one in the range 1.6 10⁻⁶ - 3.33 10⁻⁵ m³s⁻¹. The weighting device arranged in downstream of the test section has a sensitivity of about 1 g and a capacity of 3 l. Air flow is monitored upstream of the test section using three mass flow meters (Aalborg®) respective operating range: 0-50, 0-100 and 0-250 Nl/min. An accuracy of about 0.1 % overall flow rate range is thus obtained. Pressures, temperature and inlet flow rate of both fluid (air and water) are continuously monitored.

The same experimental procedure is used for all tests. Before each series of measurement, the foam sample was flooded a long time ensuring initial wetting (water) or drying (air), and established flow. The fluid is then, maintained on circulation for about half an hour after system has reached a stationary regime. Hydrodynamic (null flow) profile is checked before experiment in order to eliminate all offset between pressure sensors. For each measurement, an averaging procedure (averaging time 1 minute, data acquisition 500 Hz) is used to reduce measurement noise, after checking stationary behavior of pressure and flow rate signal. Accuracy of pressure measurement is better than 5 Pa (Madani et al., 2007).

![Fig. 4. a. Variation of permeability versus pore diameter. Dashed lines bracket extreme values. K = k .Dp². b. Variation of inertia coefficient versus inverse pore diameter. Dashed lines bracket extreme values. β = b . Dp⁻¹. From (Bonnet et al., 2008).](http://www.intechopen.com)
After each measurement series, the flow is stopped and the hydrostatic pressure profile is measured anew and compared to the previous hydrostatic one. In this way we could ensure that pressure sensors bias has not changed with the time. Gravity and capillarity driven flow through cell edges during the manufacture of metallic foams induce material property gradients (tortuosity, cell size...) and cells themselves are not spherical (Brun et al., 2009). Slight anisotropy of geometrical parameters is observed for our sample. Nevertheless at this stage of the study we neglect these effects. Measurement of full permeability and inertial coefficient tensor is, yet, difficult and the precision of our set-up in the studied configuration doesn’t allow measurement of transverse pressure gradient with an accuracy compatible with the objectives of this work (Renard et al., 2001).

### 3.3 Numerical simulation

Foam meshes have been obtained by reconstruction of tomographic images. We imaged cylindrical samples of 40 mm diameter and 15 mm thickness. High-resolution microtomography acquisition was performed on the ID19 beam line of the ESRF. Sample size was maximized while respecting the data-volume constraint and X-ray image resolution. We thus acquired a large number of cells while efficiently detecting struts (E. Brun et al., 2009). We have measured several useful morphological parameters such as specific surface, porosity, pore diameter distribution and cells orientations from 3D images analysis using iMorph (Brun et al., 2009; Brun et al., 2008).

The sample size (15 mm in all directions) is sufficient (i.e. greater than Rve) to define macroscopic parameters. The computational domain is divided in three parts: Inlet zone, test section and outlet zone to avoid bias product by back conduction and fluid recirculation. Volume mesh (~1 million cells with a mean size of about 0.2 mm and a minimal one of 0.05 mm) is generated from actual solid surface using StarCCM4+ mesher. It is composed from core polyhedral meshes in both solid and fluid phases with additional prism layers mesh in fluid phase in the vicinity of solid surfaces. Boundary conditions are: imposed temperature on one lateral wall and adiabatic on the others. Inlet temperature and pressure are imposed. Other walls are symmetry planes.

![Simulation of heat and mass transfer in a real metal foam](image)

**Fig. 5.** Simulation of heat and mass transfer in a real metal foam: Both plane sections show velocity magnitude. Solid matrix surface and streamlines are colored by respectively solid and fluid temperature. ERG 20PPI. (Hugo et al., 2010)
The Navier-Stokes equations and energy balance equation are solved using a finite volume method (StarCCM+). These equations are solved at the pore scale and give access to velocity and pressure fields in the fluid phase and temperature in both, solid and fluid phases. Local heat fluxes across the solid matrix surface are also determined. Numerical simulations are performed for a wide Reynolds number range ($10^2$ – $10^4$). On Figure 5 the two plane sections show velocity magnitude. Important velocity gradient could be observed locally while a constant averaged value is obtained in a cross section normal to principal fluid flow direction. Solid surface is colored with its temperature. A sharp gradient exists near the cooled wall while near the other side; fluid and solid temperature are roughly identical. This indicates that solid matrix allows heat conduction to take place between the heated wall and the fluid core like a classical fin. Finally, we can observe that the fluid flow is not very tortuous but struts lead to a local deformation of the thermal boundary layer. This indicates that boundary layers will not develop near wall channel. Also, some eddies could be located in the wake of struts. These phenomena govern heat transfer enhancement and pressure drop increase.

To establish parameters $K$ and $\beta$ numerically, simulations must be performed for several values of Reynolds. $K$ and $\beta$ are then computed by fitting pressure gradient versus superficial velocity data with the Forchheimer model. Results are then compared to those obtained experimentally. (Kim et al., 2001; Tadrist et al., 2004) give experimental data for pressure losses in similar metal foam (ERG) for liquid and gas flows (Table 1 and Figure 6). For clarity, data are shown by a friction factor, defined by (5), versus the Reynolds number.

$$f = \frac{\Delta P}{L} \frac{D_p}{0.5 \rho U^2} = \frac{2D_p^2}{K.Re} + 2\beta D_p$$

At macroscopic scale, mean velocities are indeed representative of global fluid behavior. Nevertheless, according to Reynolds number values, velocity gradients and preferential paths may appear. For Reynolds near unity, velocity field is very homogeneous, and struts wakes are very small (Similar to Stokes regimes around cylinders). For higher Reynolds, large eddies and recirculations are observed in the struts wakes. The flow may become un-stationary and wake interactions between struts may appear. A strut in the wake of the previous will exhibit poor heat performance. Preferential high velocity path will cause rather important pressure gradient. Some high velocity vectors exist just upstream of struts. This is a typical 3D effect, the flow get around the struts in the third dimension. Global heat exchange limitation and strong inertia effects intensity at high Reynolds can be explained by these phenomena. On the other hand, low tortuosity of pore space associated to the relatively small specific surface of the solid matrix could not explain heat transfer performance and inertia effect intensity.

On Figure 6, experimental data from (Tadrist et al., 2004) for two pores diameters (3 and 4.5mm) are compared to numerical results with a good agreement. For all pore diameters, friction factor is described by a unique curve. Equation (2) associated to these results demonstrates that both permeability and inertia coefficient evolve with the pore diameter only for these structurally similar foam samples. For a given Reynolds, to conserve a constant friction factor, permeability should be proportional to the squared pore diameter and $\beta$ to the inverse of the pore diameter as (Bonnet et al., 2008) has shown experimentally on several metal foams. Virtual Samples (VS) were created to verify this behaviour (Table1).
Fig. 6. Friction Factor versus Reynolds. Characteristic length: Pore diameter. Good agreement with experiments from Tadrist et al. (dashed line) is obtained.

Figure 7 shows a 3D representation of the pressure field on a plane section along the main flow axis for incompressible fluid. Sharp pressure gradient are observed locally near each struts and in their wake and near each throats. However on a plane section, a mean pressure gradient can be observed at the sample scale. This shows that the global pressure drop is due to two phenomena: Viscous effect on the solid surface and in the path of each throat; inertial effect in the wake of each strut due to eddies formation.

Fig. 7. 3D representation of pressure filed on a plane section along the main flow axis. Local sharp variations of pressure at throat vicinity are observed, but the averaged pressure gradient is constant. ERG 20PPI
<table>
<thead>
<tr>
<th>Sample</th>
<th>Pore diameter</th>
<th>Strut Diameter</th>
<th>Porosity ε</th>
<th>Specific surface (S_P) [m²/m³]</th>
<th>Permeability K [m²]</th>
<th>Inertia coefficient β [m⁻¹]</th>
</tr>
</thead>
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<tr>
<td>Ni 100</td>
<td>500</td>
<td>4429</td>
<td>0.92</td>
<td>680</td>
<td>1.38E-09</td>
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<td>0.87</td>
<td>5303</td>
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<td>266</td>
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<td>ERG40</td>
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<td>680</td>
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<td>Kelvin Cell</td>
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<td>0.87</td>
<td>250</td>
<td>2.00E-06</td>
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<tr>
<td>CTIF stoch.</td>
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<td>*</td>
<td>0.75</td>
<td>800</td>
<td>6.83E-08</td>
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</table>

Table 1. Summary of various metal foam sample morphological and flow law properties. Greyed values: Pore scale direct numerical simulation. *Stochastic CTIF foam is not composed of a struts network (Dairon & Gaillard, 2009). VS samples are Virtual Samples created by homothetic transform of ERG 20PPI.

The friction factor versus Reynolds curve exhibits two behaviors separated by a transition zone. For Reynolds smaller than 50, viscous effects are predominant. Pressure drop increases linearly with the velocity. For high Reynolds (greater than 2000) inertia effects dominate the flow behavior. The pressure drop increases as the square of velocity. For Reynolds between 50 and 2000, there is a transition zone where, both, viscous and inertial effects govern pressure losses. Overall Friction law is well described by the Forchheimer model. Inertia coefficients and permeability obtained from numerical simulations are summarized in Table 1 and compared to experimental data. Foam pore diameters in (Tadrist et al., 2004) study have been determined latter by (Brun, 2009). (Kim et al., 2001) only gives foam grade; pore diameter are not exactly determined. However, flow law parameters for 40PPI foam given in both experimental studies are quite close. This indicates that the grade is clearly not relevant as pore size estimator. Moreover, both numerical and experimental data lead to the same dependence of β in function of K. Several authors have proposed to use squareroot of \(\sqrt{K}\) as pore size estimator but K is usually difficult to measure accurately. This is particularly true in case of high pore size foam (> 5 mm).
3.4 Heat transfer

Direct experimental measurement of volume heat transfer coefficient is not easy for fluid flow crossing metal foam. Generally authors propose global heat transfer coefficient of a channel filled by a porous media (Kim et al., 2001). There are few works dealing with local heat transfer coefficient between fluid and solid phase (Serret, Stamboul, & Topin, 2007). However wall heat transfer coefficient is an averaging on different transport and diffusion properties on a known channel or heat exchanger geometry and can thus be used only in these cases.

In the following section, we propose different analytical and numerical models to rely this coefficient and experimental or simulation data. Models can be used to determine heat transfer coefficient from data or to predict heat exchanger performance from the knowledge of thermal properties. Heat transfer law is also determined from direct numerical simulation performed on the real foam geometry (Hugo et al., 2010).

Experimental set up described above is modified to perform heat transfer measurement. Thermocouples are added to measure local temperature along the main flow axis. Fluid flow can be heated before the channel or heat flux can be imposed on the channel wall. Two protocols are studied:

- In the first case, the metal foam is heated by hot air flow and then cooled by air at ambient temperature. Transient outlet temperature signal is used with a 0D analytical model to evaluate heat transfer coefficient.
- In the second case, fluid flow at ambient temperature is imposed at the inlet. Heat flux is imposed on the channel wall. Temperature at the outlet is measured at steady state. A 2D two temperature model (non local thermal equilibrium (Moyne, 1997)) allows one determining numerically the heat transfer coefficient.

3.4.1 0D analytical model

Metal foam is considered as thermally thin body and its temperature is considered as homogeneous and equals to $T_m$. Air flow temperature $T_a$ is imposed at the channel inlet.

$$
\left(1-\varepsilon\right) \cdot \left(\rho \cdot C_p\right)_{\text{solid}} \cdot \frac{dT_m}{dt} + h_{\text{vol}} \cdot \left( T_m - T_f \right) = 0
$$

(6)

$$
T_f = \frac{T_{\text{in}} + T_{\text{out}}}{2} = T_{\text{in}} + \frac{P_{\text{ex}}}{2 \cdot m \cdot C_p_{\text{fluid}}}
$$

(7)

Where $\varepsilon$ (-) is the porosity, $\rho$ (kg/m$^3$) the metal density, $C_p$ (J/kg/K) the metal heat capacity, $\eta$ (kg/s) is air mass flow rate and $h_{\text{vol}}$ (W/m$^3$/K) the volume heat transfer coefficient.

Fluid temperature profile is considered as linear through the channel. A mean air temperature $T_i$ is defined by (8).

$$
P_{\text{ex}} = h_{\text{vol}} \cdot V \cdot \left( T_m - T_f \right) = \left(1 - \varepsilon\right) \cdot V \cdot \left(\rho \cdot C_p\right)_{\text{solid}} \cdot \frac{dT_m}{dt}
$$

(8)

Previous equations lead to the following differential equation on foam temperature:
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\[
(1 - \varepsilon) \cdot \left( \rho \cdot C_p \right)_{\text{solid}} \left( 1 - \frac{V}{2 \cdot (m \cdot C_p)_{\text{fluid}}} \right) \frac{\partial T_m}{\partial t} + h_{\text{vol}} \cdot (T_m - T_{\text{in}}) = 0
\]

(9)

\[
T_m = A \cdot \text{Exp} \left( -\frac{t}{\tau} \right) + B
\]

(10)

The solution (10) of this equation shows that foam temperature and, thus outlet temperature is decreasing exponentially with the same characteristic time \( \tau \). For a constant inlet temperature, the measurement of the outlet temperature in function of the time (Figure 8) allows one determining the heat transfer coefficient with relation (12).

![Graph showing exponential decrease in temperature](image)

Fig. 8. Experimental fluid temperature temporal decrease along the main flow axis during sample cooling. An exponential decrease is observed. Aluminium foam (porosity 75%)

\[
h_{\text{vol}} = \frac{(1 - \varepsilon) \cdot \left( \rho \cdot C_p \right)_{\text{solid}} \left( 1 - \frac{V}{2 \cdot (m \cdot C_p)_{\text{fluid}}} \right)}{\tau}
\]

(11)

The main limit of this method is the limited range of usable sample thickness. The foam sample must be large enough to establish fluid boundary layers and be representative volume (RVE) and small enough to respect the thermal thin body hypothesis. However, as most foams are produced as flat sheets, this point is not critical for many applications.

3.4.2 Numerical model

In the case of geometry that doesn’t allow using the 0D model, a 2D numerical method based on a non equilibrium model between solid and fluid phase could be used. Equations (13) and (14) describe this model:
Fluid velocity considered here is the macroscopic one and is considered constant in the channel and the previous equations system is solved by a 2D finite volume method. We present, in this case, results obtained for the second experimental set up configuration (state measurement, heated wall).

The knowledge of effective thermal conductivity for both phase and dispersion of the fluid phase is needed to use this model. As the thermal dispersion in the fluid phase is often not precisely known (Delgado, 2007), the stagnant fluid phase effective conductivity is used in present work. Dispersion phenomena is thus impacting the heat transfer coefficient value.

### 3.4.3 Local results

In order to gain a better interpretation of global heat transfer performance, a local Nusselt and also heat transfer coefficient along the fluid flow are deduced from the simulation by dividing the test zone in numerous thin boxes perpendicular to the main flow axis. In each box, mean temperatures of both fluid and solid phases as well as exchanged heat flux are determined.

![Figure 9](https://www.intechopen.com)

Fig. 9. Local (diamonds) and integrated (dashed line) Nusselt number along the main flow axis. Characteristic length: Strut diameter. ERG 20PPI

Figure 9 shows local and integrated Nusselt number variations along the main flow axis. Nusselt number decreases slightly along the flow direction and its averaging reaches a quasi-constant value after 3 pores diameters. But its behavior differs from the empty channel case. No clear entrance zone is observed. High amplitude oscillations around the global decreasing trend with a one-pore period are observed. Local Nusselt maxima and a
minima are located at every half pore diameter. Cells present a staggered arrangement and Nusselt increases in the vicinity of throats. The cell arrangement along the main flow axis limits global thermal and flow boundary layers formation. (Madani et al., 2005) have experimentally shown similar results. For application purpose, pore size should be chosen according to the (empty) channel boundary layer characteristic length. 

Like a fin, foam efficiently contributes to heat transfer only on relatively short distance from the heated wall. This active length is defined as the distance where fluid and solid phases reach the same temperature (difference less than 5%).

On Figure 10, one could see that active length is close to 1.5Dp. Above this distance from the heated wall, heat flux is close to zero. We determine the local heat flux exchanged between fluid and solid phases. Below y*=y/Dp=0.5, heat flux are very high. The heat flux decreases roughly exponentially above 1 pore diameter.

![Fig. 10. Solid-fluid heat flux at foam surface, temperature of both fluid and solid phase versus the distance from the heated wall. x*=1.62. ERG 20PPI](www.intechopen.com)

### 3.4.4 Macroscopic results

Usually, heat transfer coefficient is presented as Nusselt number versus Reynolds number calculated with pore diameter as characteristic length. The following values are obtained for Kelvin Cell foam:

\[
\text{Nu} = \alpha \cdot \text{Re}^n \text{Pr}^{1/3} \tag{14}
\]

Where Pr is the fluid Prandtl number. Values of \(\alpha\) are generally between 0.3 and 1.5 and values of \(n\) between 0.3 and 0.7 (Kim et al., 2001; Lu, Stone, & Ashby, 1998; Serret et al., 2007). Numerical and experimental results are in good agreement at low Reynolds number.

Uncertainties on temperature and specific surface measurement can lead to a global error of about 15% on the volume heat transfer coefficient for 0D model. For 2D model, Finite volume method solver, mesh and effective thermal conductivity can lead to an error of about 20%. For high Reynolds, results are differing. RANS model (k-epsilon) on the direct numerical simulation may not be adapted to turbulent flow through metal foam.
Fig. 11. Comparison experimental 0D model Nusselt number (square) and pore scale direct numerical simulation (diamond). Laminar flow and CTIF copper Kelvin’s cells foam. \( n=0.55, \alpha=1.06 \)

Fig. 12. Comparison of experimental 2D model Nusselt number (diamond) and pore scale direct numerical simulation in turbulent regime (triangle). Dashed line: Laminar flow simulation. CTIF copper Kelvin’s cells foam.

Globally, using foamed channel allows one to achieve very high heat transfer performance and thus to design efficient heat exchanger. Nevertheless, this is obtained at the cost of additional pressure losses. These latter are discussed in the following paragraph.

4. Adiabatic two-phase flow

Numerous studies have focused on two-phase flow through porous media (glass packed beds, sintered fiber beds, etc) (Attou & Boyer, 1999; Carbonell, 2000; Jamialahmadi et al.,
2005). This type of flow is frequently encountered in many fields, such as petroleum engineering, nuclear safety, etc. Many questions remain to be answered in order to fully understand the physical mechanisms that are involved when two fluids flow concurrently through porous media. The correlations that make it possible to predict two-phase flow laws can be used only for the experimental conditions in which they have been established (strong influence of the porous geometry, sensitivity to configuration, etc).

Fig. 13. a. Two-phases flow pressure profile. Nickel sample 100PPI. b. Biphasic pressure gradient versus total mass flux variations for several air mass fluxes. Copper sample 60PPI. Adiabatic air-water flow.

As far as we know, only a few studies have focused on gas-liquid flow through metallic foams. (Madani et al., 2004; Madani et al., 2005; Topin et al., 2006) proposed an original study of n-pentane flow through copper with “liquid/vapor” phase change (40PPI, Dp = 1500 μm). The authors studied the influence of the welding of the foam sample with the heated channel wall. Pressure profiles in convective boiling experiments were measured. The heat transfer coefficient was obtained and compared to the one obtained under similar conditions in the case of smooth-tube, honeycomb-like structures and sintered bronze ball bed. The results illustrate how two-phase flow heat transfer is improved by using Metal Foam. (Stemmet et al., 2007) studied adiabatic co-current two-phase (water/air) flows in metallic foams. They showed that the relative permeability model by (Saez & Cabonell, 1985) can be used to describe the saturation (named in this paper liquid hold up) in structured solid foam packing. They proposed a correlation between the mass transfer coefficient and the rate of energy dissipation. They also studied water-air flow in the particular case of counter-current flows. The flooding points were determined. In these conditions, three types of flow regimes were identified: low liquid holdup regime: trickle flow regime, high liquid holdup: bubble flow regime and high liquid holdup: pulsing regime. For these three regimes, the liquid holdup increased with the decreasing pore size. The authors concluded that solid foam packing could be used satisfactorily for gas-liquid counter-current flow.

4.1 Pressure drop
The gas quality of the flow is our experiments vary from 0.5 up to 25 % and the void fraction (evaluated from a no-slip model) is in the range 80 up to 99%. The compressibility effects should thus appear clearly on two-phase pressure profile as the mixture is mainly composed of gas. Due to density variation with local pressure the mixture velocity should increase
from inlet to outlet producing an increasing pressure gradient. But, as experimental results are correctly modeled by linear approximation, it should exist an antagonist effect (void fraction variation probably) that mask this behavior (Figure 13). Figure 13 illustrates the influence of air flow rate on biphasic pressure gradient. For a given total mass flux the pressure loss is proportional to air flow rate. In other words, pressure gradient is proportional to flow quality. The curvature of these curves is inversely proportional to the quality of the flow. This indicates that viscous effects depend more strongly on quality than inertial one.

![Figure 13](image_url)

**Fig. 13.** Biphasic multiplier versus quality. Adiabatic two phase flow, various foam samples (200µm<D<5000µm). Comparison with tube correlation

### 4.2 Biphasic Multiplier

It does not exist, yet, agreement on a model of biphasic flow in porous media (Fourie & Du Plessis, 2002; Grall, 2001; Jamialahmadi et al., 2005; Kaviany, 1992). Thus in order to compare our results to reference cases we choose, considering the very high porosity of the foam to compare to two-phase flow in tube. The flow is established in the studied zone and is globally one-dimensional. Taking into account the precise structure of the two-phase flow is not yet possible as both slip velocity and void fraction could not be measured. Consequently we suppose that the mixture behave as an incompressible homogeneous fluid with null slip velocity. The pressure losses of the mixture are thus described using the biphasic multiplier approach (Wallis, 1969), with x flow quality (gas mass flux/total mass flux)

\[
\frac{dP}{dz} = -\left(\frac{dP}{dz}\right)_{L+G} = \left(1 + x \left(\frac{\rho_1}{\rho_g} - 1\right)\right) \left(1 + x \left(\frac{\mu_1}{\mu_g} - 1\right)\right)^{-\gamma} \tag{15}
\]

Using the experimental values biphasic multiplier are simply calculated by forming the ratio of biphasic pressure drop over single-phase one. An adjustment of exponent (\(\gamma \sim 0.7\)) of the
viscosity term appearing in the biphasic multiplier expression allows modeling all experimental data with reasonable agreement. Figure 14 present the comparison of experimental results with the correlation proposed by Mac Adams ($\gamma = 0.25$) for laminar flow in tubes (Wallis, 1969). All experimental data are roughly located on a unique curve similar to the literature correlation. Nevertheless a slight influence of pore size is visible on this figure. When pore size increase the biphasic multiplier seems to be closer to the value obtained for tube. But more experimental data are needed to interpret this effect. This approach has been applied with reasonable agreement in convective boiling case, using biphasic multiplier given by Mac Adam correlation (Madani et al., 2004).

### 4.3 Martinelli parameter and quality impact

Figure 15.a presents the experimental values of reduced two-phase flow pressure gradient in function of Martinelli parameter. This ratio between the two- and single-phase liquid flow pressure gradients is defined by equation (18). The values of the single-phase liquid flow pressure gradient are deduced from single phase flow measurement data using equation (17). Indeed, the single phase flow laws and the associated parameters for metallic foams had previously been determined (Bonnet et al., 2008).

\[
\chi^2 = \frac{\mu_L}{K} + \beta \rho_L u_L^2 = \frac{\mu_L}{K} \eta_L + \beta \eta_L^2
\]

(16)

Globally, the experimental points are gathered on a relatively narrow band between the Martinelli curves $c=5$ and $c=10$. As expected, $\phi$ values versus $\chi$ are not superimposed on a single curve. Figure 15-b shows a detailed view of Figure 15-a. At a constant value of $\phi$, the extreme values of $\chi$ could differ by 60% Moreover, these variations are not due to experimental uncertainties but are the consequence of quality variation. Indeed, single phase flows in foams being inertial (Forchheimer), several quality values can be obtained for a fixed $\chi$. 

![Fig. 15. a) Two-phase multiplier versus Martinelli parameter. Experimental values for sample NC4753 and extreme Lockhart Martinelli correlation. b) detailed view $\chi$ values versus $\chi$ are not superimposed on a single curve.](image-url)
The values of $\phi_l$ range from 1 to 10 when $\chi$ ranges from 0.1 up to 100. For a given $\chi$, the experiment shows that values systematically increase with quality (Figure 16). In terms of pressure gradient, the deviation between the model predictions and experimental results is always smaller than 25%. Thus these approaches are suitable for design or engineering purposes.

Let us notice that for a sheer Darcy flow, the relationship between quality $X$ and Martinelli parameter $\chi$ is bijective. Unfortunately, at constant $\chi$, the experimental data available did not allow us to determine any analytical expression correlating $\phi_l$ with quality. As a result, the use of any function of $\chi$ alone would only give an approximation of two-phase pressure gradient.

![Fig. 16. Two-phase multiplier versus Martinelli parameter for sample pore sizes in the range 400-2000 µm. Experimental values and comparison with two literature correlations. No clear difference between samples is observed.](image)

5. Convective boiling

5.1 Experimental set-up
The boiling mechanisms in copper foam and the evaluation of the impact of the solid matrix on flow and heat transfer phenomena were experimentally studied. It consisted of 2 rectangular channel (10x50x100 (resp.200) mm) that contained a 40 PPI grade copper foam. The smallest one is welded to the wall, as the other is just inserted in the channel A liquid (i.e., n-pentane, low toxicity, low boiling point: 36 °C at atmospheric pressure, low phase-change enthalpy) flowed through the porous media vertically from the bottom to the top (Figure 17). The channel was instrumented with 40 thermocouples and 15 pressure sensors (Madani et al., 2004; Madani et al., 2005). Before each experiment, we apply repeated Boiling-cooling sequences in order to eliminate non-condensable substances, and then flow is imposed at the desired flow rate (0- 80 kg m$^{-2}$ s$^{-1}$). After stationary regime is reached, heating power (range 0 – 25 Wcm$^{-2}$) is applied. All data are continuously monitored. When stationary regime is reached temperature and pressure profiles are recorded as well as flow rate, heating power...
Fig. 17. Experimental set-up for boiling experiments (Madani et al., 2004).

5.2 Pressure drop model
Figure 18 presents a comparison of calculated and measured pressure profile obtained for one flow rate and two different heating power in case of convective boiling of n-pentane (Madani et al., 2004). The model predicts with a good accuracy the pressure profile at moderate heating power. On the other hand a clear discrepancy between experiment and model is observed at higher heat flux. This is probably due to flow regime transition at high vapor quality. Globally, the model predicts with reasonable accuracy (20% error max) the global pressure drop of the channel but is not usable to determine local pressure profiles.

Fig. 18. Measured an calculated pressure profile in convective boiling experiments (Madani et al., 2004)
5.3 Boiling heat transfer

The boiling curve (Figure 19) shows the heat flux as a function of the wall superheat ($\Delta T$: temperature difference between the wall and the fluid) in log-log scale. This curve was measured for two cases (i) the foam welded to the wall and (ii) the foam just inserted in the channel. The onset of boiling starts at very low superheat ($\Delta T \sim 0.1$ and $1^\circ C$, respectively) compared to the “empty” channel whose $\Delta T$ is about $10^\circ C$. The heat flux strongly increases when the superheat increases. The fluid velocity has no influence on the heat flux, even at low superheat and very low fluid velocity ($10^{-40} \text{ kg m}^{-2} \text{ s}^{-1}$). The critical heat flux, for which the walls dry out (formation of an insulating vapor film on the walls leading to an overheating), was not reachable with our set-up, and so, largely exceeds $30 \text{ kW.m}^{-2}$ even at lowest tested velocity.

Performances of copper foam were compared to other fibrous materials. The boiling curve obtained in the same conditions for bronze sintered fibers, which are known for their high thermal performances (Tadrist et al., 2004) is similar to the foam inserted at low superheat. However, when the superheat exceeds $10^\circ C$, the heat flux is far smaller than the one obtained in the foam.

The high performance of the foam is linked to its open structure that permits an easy evacuation of the vapor formed near the wall. This improves the heat transfer and avoids the phenomenon of dry out. Moreover, the pressure drop generated in the foam is 10 times smaller than those in the sintered fibers for the same heat transfer and velocity conditions.

We present, on Figure 20, channel global heat exchange coefficient in boiling condition. Local thermal disequilibrium associated with (partial) dryout of the wall is observable for very low mass flux values for heat flux density greater than $10 \text{ Wcm}^{-2}$. For all other tested configurations the heat exchange coefficient decreases slightly with heat flux density. For a given velocity the heat transfer coefficient is proportional to the heat flux in the studied boiling regime. This indicates a stable behavior (no risk of burn-out) of any biphasic heat exchanger working in these conditions of heat and mass flux.

![Fig. 19. Boiling Curve: copper foam compared to sintered bronze fibers. *: inserted; x: welded; stars: bronze fibers (Miscevic et al., 2002)](www.intechopen.com)
6. Conclusion

We have discussed effective foam transport properties needed for heat exchanger design. Size and determination method of representative elementary volume were given. Both pore scale and macro-scale numerical simulations were used in conjunction with specific experimental set up to achieve this comprehensive study. We have shown that 5 pores are needed to get an accurate representation of metal foam for geometrical parameters as well as pore diameter, specific surface or porosity, and for physical properties (Pressure, Darcy scale velocity ...). Experimental set-up and direct numerical simulation have been presented to determine single- and two-phase flow laws as well as single-phase and boiling heat exchange coefficients.

7. References


The theoretical analysis and modeling of heat and mass transfer rates produced in evaporation and condensation processes are significant issues in a design of wide range of industrial processes and devices. This book includes 25 advanced and revised contributions, and it covers mainly (1) evaporation and boiling, (2) condensation and cooling, (3) heat transfer and exchanger, and (4) fluid and flow. The readers of this book will appreciate the current issues of modeling on evaporation, water vapor condensation, heat transfer and exchanger, and on fluid flow in different aspects. The approaches would be applicable in various industrial purposes as well. The advanced idea and information described here will be fruitful for the readers to find a sustainable solution in an industrialized society.

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