Chapter from the book *Coherence and Ultrashort Pulse Laser Emission*
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1. Introduction

Laser-driven acceleration of particle beams is a burgeoning field of research, based on the possibility of creating ultra-large electric fields in plasma, largely exceeding current limits of conventional acceleration technology. Research in this area has led to very significant progression regarding the acceleration of electrons and ions. Laser-driven ion sources have unique properties: high brightness (about $10^{13}$ protons/ions per shot), high current (in kilo-Ampere range), ultra-low emittance, and short pulse duration (less than 1 ps), opening prospects for a broad range of applications. Recent advances in the laser technology have led to even further enhancements in the provision of extremely short and high-intensity pulses, which can further improve the accelerated ion beam specifications particularly regarding maximum ion energy and ion flux which are demanding most of the potential applications. These developments have stimulated an emergence of advanced diagnostics for measuring complex plasma effects.

The absorption mechanisms of laser radiation at the target are the basic processes, which indeed defines the whole ion acceleration scenario. For laser intensities, where the classical normalized momentum of electrons quivering in the laser electric field: $a = 8.53 \times 10^{-10}$ (μm) $I^{1/2}$ (W/cm²) > 1, the electrons become relativistic and the effect of the laser magnetic field is no longer negligible. The perpendicular component of the Lorentz force $e \mathbf{v} \times \mathbf{B}$ couples with the electric force to drive the electrons in the laser propagation direction (Wilks et al., 1992, Lefebvre & Bonnaud, 1997, Krueer & Estabrook, 1985) in contrast to inverse bremsstrahlung and resonance absorption, which causes the quiver motion of the electrons in the laser field. The ponderomotive force drives the electrons with a step- or plateau-like density profile and has a strong directionality along the laser propagation direction. Electron temperatures about 1 MeV have been measured (Malka & Miquel, 1996). The laser energy transfer to the hot electrons can also be out carried by fast plasma waves through the nonlinear ponderomotive force (Tajima & Dawson, 1979) and by laser field itself (Pukhov et al., 1999).
Whereas the ions from the target front will be accelerated normal to the target front surface in the ambipolar expansion of the plasma, the hot electron component created directly by the laser pulse in the plasma plume will propagate through the target. It has typically a divergence between 5°-50°, density of the order of the critical density \(10^{20} - 10^{21} \text{ cm}^{-3}\) and a temperature of the order of the laser ponderomotive potential.

The free motion of this hot electron beam through the target requires a return current that locally compensates the flow of the hot electrons (Passoni et al., 2004). It will be provided by the target material (for metallic target - conduction electrons, insulators - the background free electron population created by field and thermal ionization). Since the density of the background electron population in both cases is of the order of the solid density, much bigger than the fast electron density, the required velocity for current neutralization is small and their temperature is much lower than that of the hot electrons (Tikhonchuk, 2002).

Finally the physical parameters and dynamics of these two electron populations will define the electrostatic sheath field which is created at the vacuum – solid interface and accelerates ions to high energies.

The ions are created and accelerated either at the target rear surface (Snively et al., 2000, Mackinnon et al., 2001, Hegelich et al., 2002) through the self-consistent electrostatic accelerating field generated by fast electrons escaping in vacuum (so-called target normal sheath acceleration—TNSA mechanism) or at the target front surface, illuminated by the laser (Clark et al., 2000a, Maksimchuk et al., 2000, Clark et al., 2000b). Particle-in-cell (PIC) simulations suggest a variety of mechanisms that may be responsible for acceleration at the front surface: formation of multiple collisionless electrostatic shocks (Denavit, 1992, Silva et al., 2004, Wei et al., 2004); a solitary wave produced by shock-wave decay in a plasma slab (Zhidkov et al., 2002); or a mechanism wherein the ponderomotive pressure of the short laser pulse displaces the background electrons, and the ions are accelerated by the electrostatic field of the propagating double layer (Shorokhov & Pukhov, 2004). However, all these mechanisms are relying on ion acceleration in the electrostatic field created due to charge displacement driven by the laser field.

These scenarios are not mutually exclusive. Their relative contributions depend strongly upon the particular target and laser parameters and can contribute to the generation of electrons and, in turn, to ion acceleration mechanisms. Particle-in-cell (PIC) simulations by Wilks et al., (2001), and Pukhov, (2001), and observations by Zepf et al., (2003), and Karsch et al., (2003), show that ions can be produced at the target front and the rear sides simultaneously, even if the generation processes are quite different. Here the laser pulse contrast has a profound effect on accelerated ions and their cut-off energy (Mackinnon et al., 2002, Kaluza et al., 2004, Lindau et al., 2005).

The acceleration is most effective on light ions (specifically protons), which are usually present on target surfaces in the form of contaminants like hydrocarbons and water, or can be present among the constituents of the solid target (e.g. as in plastic targets). The heaviest ion population of the target provides a positive charge, which offers much more inertia and makes the charge separation responsible for the huge accelerating field. Part of this heavy population can also be effectively accelerated, on a longer time scale, if the protons are not enough to acquire most of the energy contained in the electric field, or if protons are removed before the arrival of the laser pulse.

The complex, non-linear nature of laser-driven plasma dynamics and ion acceleration phenomena requires the development of an innovative diagnostic complex allowing...
simultaneous measurements of different plasma parameters (using visible- and XUV-light, X-rays, Gamma-rays, ion and electrons) with high temporal, spectral and spatial resolution together with laser pulse parameters. This requirement is especially important because of both: shot-to-shot fluctuations of laser pulse parameters and inherent shot-to-shot variations in the local target parameters, which can derogate the whole plasma dynamics.

In laser-matter interaction studies one of the important research tasks is to investigate the energy distributions of emerging charged particles, in which the different laser energy absorption mechanisms are hidden and the energy redistribution among the plasma components become apparent. As a basic diagnostic the Thomson spectrometer has been widely and successfully used for analyzing the energy spectra of laser accelerated charged particles. In Fig.1 a typical experimental setup of laser plasma interaction experiments with Thomson parabola spectrometers and, as an example, spectral traces recorded with absolute calibrated micro-channel-plate (MCP) detector (Ter-Avetisyan, et al., 2005) are shown.

Several modifications of the basic spectrometer design allow a comprehensive and precise analysis of ion acceleration. In particular, (i) the simultaneous measurement of ion and electron spectra in the same direction allow to understand the measured particularities in the ion spectra resulting from the evolution of a two-electron component (hot and cold) plasma (Ter-Avetisyan et al., 2004a). (ii) The complexity of the temporal (Ter-Avetisyan, et al., 2005) and spatial characteristics (Schreiber et al., 2006) of laser driven ion source could be demonstrated by precise measurement of the proton/ion trajectories, and its applicability for proton deflectometry (Ter-Avetisyan et al., 2008, Sokollik et al., 2008), and (iii) proton source tomography revealed detailed properties of the laser driven ion source (Ter-Avetisyan et al., 2009a). Latest is crucial in view of planning proton beam steering systems.

The comprehensive set of on-line diagnostics, which are complementary each other and can be used simultaneously, is a very powerful tool for laser plasma interaction studies. In each experiment only various diagnostics would allow unambiguous demonstration of ion acceleration processes in their whole complexity, providing a set of data also for theoretical interpretation.
2. Specific features of accelerated ion and electron dynamic

2.1 Dips in ion emission spectrum and electron dynamics

Several physical mechanisms have been considered for the appearance of high-energy electrons, and have been proposed as a way to understand the generation of ions with kinetic energies of several tens of MeV during the short laser-pulse interaction with dense plasmas, (Malka & Miquel, 1996, Clark et al., 2000b, Forslund & Brackbill, 1982, Fews et al., 1994, Beg et al., 1997, Gitomer et al., 1986). A theory has been developed (Wickens et al., 1978, Wickens & Allen, 1979) for the free expansion of the laser plasma with hot ($T_h$) and cold ($T_c$) electron temperature components, as a way to treat these non-equilibrium effects and to describe the ion energy distribution. It was shown that the energy fraction carried by fast ions depends on the temperature and concentration of the electrons in the plasma. This leads to an ion-emission velocity spectrum whose most notable feature is a pronounced dip in the distribution (Kishimoto et al., 1983). The slopes of the upper ($-\left(\frac{M}{ZkT_c}\right)^{1/2}$) and lower ($-\left(\frac{M}{ZkT_h}\right)^{1/2}$) asymptotes in the ion velocity spectrum makes possible a determination of the effective absolute hot- and cold-electron temperatures (Wickens & Allen, 1981). (Here, $M$ is ion mass, $Z$ is charge state, $kT$ is cold- or hot-electron energy).

The dip in the velocity distribution corresponds to an internal electrostatic sheath appearing due to hot- and cold-electron isothermal expansion, where ions are strongly accelerated in a small region. This dip develops in a region of self-similar flow where the ions experience rapid acceleration due to an abrupt increase in the electric field. This increase occurs at the location in the expanding plasma where most of the cold electrons are reflected, corresponding to a step in the ion charge density (Wickens & Allen, 1981). The depth of the dip as a function of the peak field is a sensitive function of the hot-to-cold electron temperature ratio $T_h / T_c$ in the ion spectra, while the position in the spectrum depends on the hot-to-cold electron density ratio $n_h / n_c$.

In a very short pulse (35 fs) and high intensity laser plasma several groups of electrons with different temperatures can be generated (Zhidkov et al., 2001), which could then cause multiple dips in the ion energy spectra. No hint of this has been observed so far, and therefore detailed measurements of the ion and electron spectra are required to find correlations between these processes.

Here we report on precise measurements of the spectral density distribution of the ion emission from plasmas created by 35 fs laser pulses at intensities of $(0.8 - 1.2)\times10^{19}$ W/cm$^2$. A pulse from a multi-TW Ti: Sapphire laser (Kalachnikov et al., 2002) with a maximum energy of 750 mJ, was focused with an f/2.5 off-axis parabolic mirror onto water droplets of ~20 µm diameter (Hemberg et al., 2000). Measurements were made of ion spatial and energy distributions, X-ray spectral properties, the electron spectrum emitted, and the correlation of maximum electron energies with the cut-off energies of proton and deuteron spectra.

The ion energies have been measured with a Thomson parabola spectrometer, into which the ions enter through a 200 µm aperture. The ions are detected by a 40 mm MCP coupled to a phosphor screen. The signal from the phosphor screen is imaged with a charge-coupled device (CCD–camera). An $^{241}$Am $\alpha$-particle source (energy 5.4 MeV) with known emittance is used to calibrate the setup (Ter-Avetisyan, et al., 2005). This sensitive, calibrated detection technique allows the measurement of an ion spectrum from a single laser shot in absolute terms.

A typical camera picture taken with a single laser shot, showing ion traces from a heavy water droplet, is depicted in Fig.2 and the deduced deuteron spectra is shown in the inset.
Fig. 2. Color image from the MCP-phosphorous screen of an emitted ion spectra (deuterons and oxygen ions, right blob – “zero” point: radiation impact along spectrometer axis) from a heavy water droplet taken from a single laser shot in backward (135° to laser propagation) direction with the Thomson spectrometer. In inset the deuteron spectrum is plotted.

The most interesting features in the picture are the clearly visible dips along the deuteron trace. As mentioned before, the same feature has been observed for proton emission from water droplets, and has been observed in backward (135° to the laser axis) as well as in forward (laser propagation direction) emission. The occurrence of the spectral dips was reproducible in the experiment, although the exact position, depth, and fine structure varied from shot to shot due to small variations in the laser parameters and beam alignment in our setup. This is, to our knowledge, the first observation of these dips in ultra-short (sub 50 fs) high intensity laser-plasma interaction experiments.

The generated hot electron spectrum was measured with a GAFchromic film (HD-810) in a direction transverse to the laser axis using a 0.27 T magnet spectrometer. The film is sensitive to electrons above 10 keV due to its layer characteristic (Busch, et al., 2003). The measured time-integrated hot electron spectrum (Fig.3a) shows a maximum at an energy of about 0.7 MeV with a tail expanding to 2 or 3 MeV.

From the measured electron spectra, one can deduce a hot electron component with a temperature of (0.63 ± 0.03) MeV. This fits well with the energy the electrons can acquire from the ponderomotive force $F_p$ of the laser pulse (Kruer & Estabrook, 1985): $F_p = \frac{dU_p}{dz}$, $U_p(eV) = 9.33 \times 10^{-14} I(W/cm^2) \lambda^2(\mu m)$, where $U_p$ is the ponderomotive energy. This gives a potential energy of 0.6 MeV for our laser intensity, proving a rather efficient laser energy transfer to the electrons. Because up to 20% of the laser energy can be absorbed in energetic electrons (Wilks et al., 1992), a significant number of electrons with energies of several hundreds of keV is produced. The electron impact ionization cross section at the energies 400-500 keV is about $10^{-19}$ cm$^2$ (http://physics.nist.gov/cgi-bin/Ionization/table.pl?ionization=H2O), therefore these highly energetic electrons can cross the target without being significantly slowed. A space-charge field accumulated in the droplet captures the hot electrons with energies below about 200 keV (low energy cut off in Fig.3a). The potential due to these electrons and the estimated electron density is sufficient to create electrostatic acceleration fields of the order of 1 MV/μm (Busch, et al., 2003) which, in turn, can accelerate ions to MeV energies. Electrostatic or magnetic fields around the
target will influence the directionality of ion emission. However, for our spherical target, we expect a relatively isotropic ion emission distribution, which can be shown by measurements (Busch, et al., 2003, Karsch et al., 2003).

A strong correlation between the maximum ejected electron energies and the deuteron cutoff energies could be directly established (Fig. 3b) with the help of a re-designed Thomson spectrometer allowing to measure in one laser shot the emitted ion and electron spectrum in a same direction. For that the second MCP detector was added to that side of the spectrometer where the electrons are deflected. In Fig. 3b, a variation in the maximum energies of the ejected electrons by only a factor of 1.2 changes the deuteron cutoff energy by a factor of about 5. This extreme sensitivity emphasizes the predominant role of the energy transfer to the electrons for the ion acceleration.

![Figure 3a](image1.png)

![Figure 3b](image2.png)

![Figure 3c](image3.png)

Fig. 3. Electrons, ions and x-rays emitted of heavy water micro droplet. a) Hot electron energy distribution (superposition of ~50 000 shots). Slope fits to an exponential decay with a temperature T= 630 keV parameter. b) Correlated maximum energies of emitted electrons and deuterons in same laser shot. c) X-ray emission spectra from heavy water droplet.

The space charge field built up by the trapped hot electrons in the target is responsible for ion acceleration properties (Fig. 3a), therefore, these electrons have been studied further in details. According to a simple bremsstrahlung model (Griem, 1964), hard X-ray emission
from the plasma is defined by the electron density distribution inside the target. For highly energetic electrons crossing the droplet, the target is “thin”, so their bremsstrahlung is weaker and the spectral intensity is constant (Blochin, 1957).

A calibrated X-ray CCD-camera operating in a single-photon detection mode was used for energy-dispersive X-ray measurement (Ter-Avetisyan, et al., 2003). In the experiments, the CCD-camera was mounted at an angle of 90° to the laser propagation direction and at a distance of 100 cm from the plasma source. A 200 nm Zr filter and a beam aperture was used to block the optical light and the scattered X-rays. The resolution of our spectral diagnostics is about 0.5 keV. A typical X-ray spectrum is shown in Fig.3c. The slope of the distribution shows the existence of multi-temperature components, and can be fitted assuming three different effective temperatures of about \((7\pm0.3)\) keV, \((20\pm4)\) keV, and \((33\pm12)\) keV.

Recently, a fluid model based on a single electron temperature approximation was applied successfully for high intensity laser-driven ion acceleration (Mora, 2003). Accurate results could be obtained for the structure of the ion front, the ion energy spectrum, and the cutoff ion energy. In the present letter, on the other hand we explain the dips in the emitted ion spectrum (Fig.2) by relying on the fact that we have an electron spectrum characterized by several electron temperatures. This is the precondition for an application of the fluid model (Wickens et al., 1978, Wickens & Allen, 1979, Kishimoto et al., 1983). Figures 4a and 4b compare experimental proton and deuteron energy distributions with calculations based on the theory of Wilkens et al. (1978). A reasonable fit for the depth and position of the dip in the proton spectrum (Fig.4a) is obtained when the hot-to-cold electron temperature ratio \(T_h/T_c\) is assumed to be about 9.8, and the hot-to-cold electron density ratio \(n_h/n_c\) is about 1/100. Individual electron temperatures \(T_c = 7.5\) keV and \(T_h = 74\) keV compare quite well to the range of temperatures derived from the X-ray emission. Here, \(T_h\) is lower by a factor of about 2, but this can be due to the restricted linearity range \((< 50\) keV\) in the X-ray measurement. Also, if one takes into account that bulk ion energy scales with the hot electron temperature as \(E_{ion} = 4.5\ T_h\) (Wickens & Allen, 1979), a mean ion energy \(E_{ion} = 330\) keV would be derived, in remarkably good agreement with the ion temperature inferred from the ion slope (Fig.4a). This is somewhat different from the original model where the ion energy is predicted to be similar to the hot cf. cold electron energies. A sharp proton
cutoff energy occurs at about 1.3 MeV. Notice that the analytical velocity distribution derived in (Wilkens et al. 1978) breaks down if the temperature ratio $T_h/T_c$ exceeds 9.9. In order to overcome this problem, a more complex electron velocity distribution was included in (Kishimoto et al., 1983) [33].

For a heavy water droplet, presented in Fig.4b where the cutoff energy occurs at about 0.55 MeV, the model with a hot-to-cold electron temperature ratio $T_h/T_c = 7.7$ and an electron density ratio $n_h/n_c = 1/25$ fits the measurement quite well. The individual temperatures are $T_c = 11$ keV and $T_h = 85$ keV. The model shows how small changes in $T_e$ and $n_e$ have large effects on spectral slopes.

From the structure of the emitted ion spectrum such important parameters as hot- and cold-electron temperatures and their density ratio can be determined. Due to the short laser pulse the hot electron population shows a multi-temperature behaviour. This, in turn, can cause multi-dips in the ion spectrum. It is worth noting that the results demonstrated here could open a way to tailor the ion spectra (Nishihara at al., 2001) from short pulse laser-driven plasmas by choosing proper electron distributions appropriate to particular applications.

2.2 Laser pulse contrast and electron dynamic

Two different laser energy absorption mechanisms at the front side of a laser-irradiated foil have been found to occur, such that two distinct relativistic electron beams with different properties are produced. One beam arises from the ponderomotively driven electrons propagating in the laser propagation direction, and the other is the result of electrons driven by resonance absorption normal to the target surface. These properties become evident at the rear surface of the target, where they give rise to two spatially separated sources of ions with distinguishable characteristics when ultra-short (40 fs) high-intensity laser pulses irradiate a foil at 45° incidence. The two, clearly distinguishable branches of electron trajectories have been measured by Čerenkov diagnostics. This correlates with proton emission from two separated sources, which have been resolved with a high-spatial-resolution Thomson spectrometer (Schreiber et al., 2006). The crucial parameters of the experiment are the laser pulse intensity and the contrast ratio.

In the experiments, a 40 fs pulse from a multi-TW Ti: Sapphire laser was focused onto a thin (6 µm) aluminum foil target at 45° with an intensity of about $2 \times 10^{19}$ W/cm². The temporal contrast of the laser pulse was characterized by a scanning third-order cross correlator with a dynamic range of $10^{10}$, having a resolution of 150 fs and a scanning range of ± 200 ps. The pulse shape several ns before the main pulse was controlled by a fast photodiode with temporal resolution of about 300 ps. In typical operating conditions, the amplified spontaneous emission (ASE) pedestal of the laser pulse, several picoseconds before the pulse peak, was at a level of $(0.8 - 5) \times 10^{-7}$ relative to the peak intensity. This is termed “low” contrast. The ASE pedestal could be reduced by driving the Ti: Sapphire laser amplifiers in specific delayed pump modes. This led to a reduction of pulse energy by up to 550 mJ, but it permitted an improvement of the ASE level down to $(1 - 3) \times 10^{-8}$, which is referred to as “high” contrast. In both cases, no pre-pulses were observed.

The Čerenkov method, applied as an electron diagnostic, uses the partial conversion of the electron bunch energy into a flux of photons in a medium where the electron velocity is higher than the light velocity (Stein et al., 2004). A 50 µm tesa foil (polypropylene with chemical composition (- C₃H₆ -)$_n$, index of refraction - 1.49) used as a Čerenkov radiator was attached with very thin Acrylat glue to the target rear, and imaged with an objective ($f = 8$ cm) and a magnification of about 15 to a gated charge-coupled device (CCD) camera. It is
assumed that a 50 µm path length in this low Z substance has a negligible effect on the energy and main direction of the electrons. Propagating through the foil, the electron beam undergoes filamentation (Mancossi et al., 2006), but nonetheless with unaltered beam directions emerging from the target. To block any light from the laser pulse and its harmonics, a 6 mm Schott BG18 filter and a 3 mm VG8 filter were inserted into the beam path. These filters yield a spectral window centered at 510 nm with a half width of 70 nm. A weak and uniformly distributed background signal from transition radiation is omitted as a result. For the medium and the geometry used, the detected Čerenkov light is associated with electrons in the 180 – 240 keV energy interval.

Measurements of the ion energies were carried out with a Thomson spectrometer (Ter-Avetisyan et al., 2005). In order to achieve high spatial resolution, we set up a Thomson spectrometer in a 1:12 imaging mode (Schreiber et al., 2006), providing spatial resolution of about 20 µm. This estimation takes into account the laminarity of the proton beam, and is measured from the spreading of a spectral trace which is a consequence of the divergence of the proton beamlet intercepted by a screen with a 30 µm pinhole.

The Čerenkov medium behind the target made it impossible to use both diagnostics simultaneously for the single laser shot. Therefore, correlations between the data sets are statistically relevant. Due to a 10 Hz repetition rate of the Ti:Sapphire laser, and using online detection systems for both diagnostics, the statistical uncertainties could be minimized.

Figure 5 shows spatially resolved CCD pictures of Čerenkov radiation behind the 6 µm Al target at 45° laser incidence (a - c), and it shows the evolution of the Čerenkov signal as a function of target thickness (d). The arrows inserted in the pictures show the target irradiation and Čerenkov emission geometry. In the pictures, one of the two components of the hot electron current produced is identified as a consequence of hot electrons driven along the target normal due to resonance absorption, and the other component along the laser propagation axis is due to the ponderomotive force. Whereas in Fig.5a both electron components make a comparable contribution to the resulting Čerenkov emission, resonantly and ponderomotively driven electrons are dominant in Figs.5b and 5c, respectively. The appearances of the emission patterns are statistical, and correlated with the statistics of the laser pulse contrast shot-to-shot fluctuation data.

![Fig. 5. CCD pictures of Čerenkov radiation (arrows show emission direction) at 45° laser incidence resulting from electrons propagating: (a) in the laser direction and normal to the target; or (b) perpendicular to the laser direction only; and (c) in the laser direction only. (d) Čerenkov light distributions as a function of Al-target thickness.](www.intechopen.com)
The evolution of the Čerenkov signal as a result of target thickness is shown in Fig.5d. With a 3 µm target the two components are merged together, while at 6 µm they are clearly separated and at the target thickness is 15 µm, further broadening of the electron beams propagating inside the target occurs, and blurs the Čerenkov emission. In the experiments reported in Ref. (Stein et al., 2004), these two groups of separately moving hot electrons at the target rear side also were observed. Here we investigate the dynamics of the hot electron populations, and the consequences for the ion acceleration processes at “low” and “high” laser pulse contrasts.

Fig. 6. A CCD picture of a proton spectrum at 45° laser incidence on a 6 µm Al target, measured in the direction of the target normal. The inset shows proton spectra from a 3 µm target thickness at similar irradiation conditions.

The resonantly and ponderomotively driven electron populations at the target rear side create two spatially separated electrostatic fields, from where the ions/protons can be accelerated. Therefore, one can expect ion emission from two spatially separated sources if the laser pulse contrast is between $10^{-8}$–$10^{-7}$, where both laser energy absorption mechanisms are equivalent. Indeed, the CCD picture of the proton spectrum in Fig.6, measured in the direction of the target normal, shows two parallel proton parabolas, thus confirming the existence of the two sources of proton emission. The lower trace results from the source created by electrons from resonance absorption, and the upper one from the source created by ponderomotively driven electrons. The appearance of the second source (or second proton trace) is in good agreement with the detection of two electron populations by Čerenkov diagnostics (Fig.5a). This feature is never observed at normal laser incidence on the target. Figure 6 also shows that the parabolas are not perfect. This coincides with the previous findings (Schreiber et al., 2006) that the source position could be variable. Note that the two parallel traces in Fig.6 change in a similar manner, while the proton spectrum of a 3 µm thick target (inset of Fig.6) shows an independent character, which indicates a complex source dynamics.

In order to see the differences in the electron acceleration processes and the implications for the following ion acceleration, we performed two-dimensional (2D) particle-in-cell (PIC) simulations of laser irradiation onto targets with different scales of pre-plasmas. The targets are 2 µm thick and have densities of 40 $n_c$. The pre-plasma is assumed to have an exponentially decreasing profile with two scale lengths. For the overdense region where the density is higher than 4 $n_c$, the scale length is 0.1 µm. For the lower density region resulting from an expanding
corona plasma, the scale lengths are 0.3 µm for the small pre-plasma case and 3.5 µm for the large pre-plasma case. The initial electron temperature is 1 keV, and ions are kept immobile. The targets are irradiated by p-polarized laser pulses from the left boundary with wavelengths of 1µm. The laser pulses ramp up in five laser cycles, and sustain a peak intensity of $2 \times 10^{19}$ W/cm² that is uniform in the y-direction. The pulse duration is 40 fs. The boundary conditions are absorbing in the x-direction, and periodic in the y-direction.

![Fig. 7. Electron momentum distribution observed in PIC simulation at the target rear surface for a) “small” L = 0.3 µm scale length pre-plasma case, and for b) L = 3.5 µm “large” scale length pre-plasma case. Laser pulses irradiate the target from the left boundary.](image)

The differences resulting from the dominant acceleration processes are seen from the angular distribution of accelerated electrons. In Fig.7, the angular electron momentum distributions observed in the PIC simulation at the target rear surface are shown for the a) “small” L=0.3 µm scale-length pre-plasma case, and for the b) L=3.5 µm “large” scale-length pre-plasma case. In the small pre-plasma case, ponderomotive acceleration and vacuum heating play dominant roles in energy absorption by electrons. Due to vacuum heating, laser energy is absorbed by low energy bulk electrons that are mainly accelerated in the target-normal direction. High energy electrons generated by ponderomotive acceleration propagate in the laser irradiation direction, and are reflected back toward the target at the specular angle, as can be seen clearly in the figure. For the large pre-plasma case, high energy electrons are mainly accelerated by resonance absorption in the target normal direction and are reflected back also in the normal direction.

These high energy electrons induce a strong magnetic field around the critical surface. In the small pre-plasma case, a magnetic field with uniform intensity is induced along the critical surface. This surface magnetic field prevents low energy electrons from propagating into the target, and makes them flow along the surface (Nakamura et al., 2004). In the large pre-plasma case, a magnetic field is formed via Weibel instability (Weibel, 1959), which is in the target-normal direction. The surface field tends to make electrons flow along the surface, which leads to a uniform structure of the interaction surface. The target-normal magnetic field acts to collimate electron jets and return currents that are periodic along the surface. As a result, the critical density surface is rather smooth in the small pre-plasma case and modulated in the large pre-plasma case.
Fig. 8. Ion density distribution for a) large (L = 3.5 µm) and b) small (L = 0.3 µm) pre-plasma cases. Laser irradiation is from the left boundary, where the spot size is 15 µm, and the spot centre corresponds to y = 8.5 µm at the left boundary. Two arrows in b) indicate the trace of the laser spot centre and the target-normal projection of the spot centre.

These different electron acceleration processes lead to differences in the lateral distributions of the rear side sheath field and proton acceleration as follows. The target size is 2 µm in thickness and 50 µm in width. The targets consist of 50% protons and 50% C\textsuperscript{4+}. Laser conditions are the same as above except that the laser pulses have a spot size of 15 µm with a super-Gaussian distribution. The boundary conditions are absorbing in the x- and y-directions. Ion density profiles at 150 fs after the pulse has ended are shown in Fig.8.

For the large pre-plasma case, the ion distribution is symmetric with respect to the laser axis passing through the laser focal point at the critical surface. Since a large part of the hot electrons propagate in the target-normal direction, the sheath field structure is similar to the normal incidence case. For the small pre-plasma case, however, the proton distribution is non-uniform and asymmetric. As is seen in previous simulations, very energetic electrons are accelerated in the laser propagation direction, and lower energy electrons are generated in the target-normal direction via vacuum heating. These two components result in two acceleration fronts of protons, which are clearly seen in Fig.8b and detected in the experiment. The distance between the two acceleration points depends on target thickness and size of pre-plasma. In PIC simulation, the target is thinner and the density is lower than in the experiments. Thus the separation distance is considered to be larger than is visible in PIC simulation. Also, in Fig.8 we show the angular distributions for pre-plasma scales of 0.3 and 3.5 µm in order to see clear differences, but similar results are seen at much smaller differences also. The important thing is that the dominant acceleration process changes when the scale length becomes smaller than the wavelength.

A PIC simulation of the experimental parameters shows that the dominant electron acceleration process depends on the profile of the pre-plasma. For plasmas where the scale length of the pre-plasma is larger than the laser wavelength, a plasma wave is resonantly excited at the critical density surface, which results in the generation of fast electrons propagating in the target-normal direction (Estabrook & Kruer, 1978). If the pre-plasma scale length is smaller than the laser wavelength, a well-collimated electron beam is accelerated by ponderomotive forces in the propagation direction of the laser (Wilks et al., 1992, Kruer & Estabrook, 1985). Correspondingly, protons are accelerated in a target-normal...
direction from two spatially separated sources. The laser intensity and the contrast determine the laser absorption process and thus they control the entire acceleration scenario. PIC simulations confirm these findings.

2.3 Energy resolved spatial characteristics of laser accelerated protons

As we have seen, interactions of relativistic-intensity laser pulses with targets with and without pre-plasmas are significantly different from the perspective of the dominant electron acceleration processes and the energy coupling to plasmas.

To clarify the proton acceleration process that is uniquely observed for small pre-pulses, oblique irradiation, and in thin targets we incorporate particle diagnostics which provide a microscopic measurement of the proton acceleration with PIC simulations. We found that the laser-accelerated proton source drifts on the rear surface of the target in the direction of projection of the laser wave vector onto the surface. The drift of the proton source is explained by the lateral movement of the sheath field. This moving proton source leads to the observation of a limited range of proton energies at any given point along the target surface.

The proton source was investigated with an experimental setup and geometry similar to those in section 1.2. The ion emission spectrum was measured with an absolutely calibrated Thomson parabola spectrometer (Ter-Avetisyan et al., 2005) set up in magnifying imaging mode (Schreiber et al., 2006). The spectrum is imaged through a 30 μm pinhole, located at a distance of 5 cm from the source, on a detector screen 75 cm behind the pinhole, at 45° laser incidence on a 13 μm aluminum target; see Fig. 9.

![Proton spectrum images](Fig. 9. a), b), c) CCD picture of the proton spectrum at 45° laser incidence on a target measured in the direction of target normal with a magnified imaging ratio of 1:15. The ideal parabola trace is the solid line in the figure a) inset. b) Proton spectrum from a Mylar target. c) Proton spectrum from Al target when proton beam passes through two pinholes. d) Schematic figure of the geometry of two pinhole measurement.)
The striking features of this figure are that the whole low-energy part of the spectrum is shifted from the ideal parabolic trace calculated according to our geometry, whereas the high-energy part obeys the calculated parabolic trace (solid line in Fig. 9a inset) assuming that the ions are emitted from a fixed ion source, and finally that the trace of the low-energy part shows strong oscillations.

The imaging factors of the setup include the geometry and the emitted proton beam characteristics, such as partial beam divergence. In Fig. 9a it is found that the trace spread decreases with increasing proton energy. The trace spread and the partial beam divergence calculated for the present geometry (distance from the source to the detector) decrease from 0.13 to 0.11 mrad when the proton energy increases from 0.2 to 3 MeV. Therefore, in the present geometry, the image covers only the diameter of an 18 μm area on the target with a magnification factor of about 15. The observed phenomena are attributed to the continuous movement of the proton emission source up to about 20 μm. When electron beam filamentation occurs during electron propagation inside the target, as it is the case for insulators (Manclossi et al., 2006, Fuchs et al., 2003), several proton emission points and, correspondingly, multiple parabolic traces would be measured. The proton spectra from 13 and 20 μm Mylar targets taken at a relatively low laser pulse contrast (∼10⁻⁷) indicate many separate proton emission points on the target. In Fig. 9b is given, as an example, a proton spectrum from a 20 μm Mylar target. Here the energy scale is calculated assuming that the source point is in the middle of the right blob in Fig. 9b.

The continuous proton spectrum in Fig. 9a suggests that one proton source point is continuously moving on the surface. In order to give additional proof of this assumption, a second pinhole with a diameter of 150 μm was installed at 35 cm behind the first pinhole (see Fig. 9d), in order to detect only the protons emitted from an area of 20 μm diameter with straight trajectories along this axis. Particles that are emitted from the other parts of the source and even have passed the first pinhole will be blocked by the second one. A continuous decrease of the size of the second pinhole led to truncation of the spectrum and finally only the high-energy part of the spectrum remains, which lies on the expected ideal parabolic trace as shown in Fig. 9c, indicating that they are accelerated from the indicated point source. Here, another interesting point is that the source position from which the high energy protons are emitted does not emit the low-energy ones in the same direction. It has to be mentioned that these phenomena are observed only at 45° laser irradiation case.

2D PIC simulations were carried out to see the temporal evolution of the sheath field on the rear surface. The simulation conditions are as follows. The targets are 13 μm in thickness and 70 μm in width with density of 40 nₑ, where nₑ denotes the critical density for the laser wavelength of 0.8 μm, and consist of electrons and Al³⁺ ions. The proton source is a contaminant layer, which is modelled as a buried proton layer at the rear surface with thickness of 0.1 μm and density of 1nₑ, i.e., the 0.1 μm layer from the rear surface is composed of 39 nₑ of Al³⁺ and 1nₑ of protons, with 40 nₑ electrons. The electrons initial temperature is set at 1 keV, and the ions are initially cold. The system size is 50 μm in the x direction and 70 μm in the y direction and the cell number is 2245 × 3369. 12 particles are used in one mesh for each species and the total number of particles is about 8×10⁷. The density profile of the pre-plasma is assumed to be exponential with two scale lengths. For the overdense region where the density is higher than 3 nₑ the scale length is 0.1 μm. For the lower-density region, lower than 3 nₑ, the scale length is 0.5 or 3.5 μm. A p-polarized laser pulse whose spot diameter is 10 μm irradiates the target from the left boundary with the
Incident angle of 45°. The laser pulse ramps up in five laser cycles and sustains its peak intensity of $2 \times 10^{19}$ W/cm$^2$ for a duration of 40 fs. The laser axis irradiates the target surface at $y \approx 17 \mu m$. On the boundaries, particles are reflected back to the system by reducing their energy to the thermal one, and the electromagnetic fields are damped at the boundaries.

Fig. 10. Temporal evolution of the electron energy density and the longitudinal electric field. The electron energy density is normalized by $n_e m_e c^2$, and observed at a) 140 fs, and c) 220 fs. The electric field is normalized by laser electric field, and observed at b) 140 fs, and d) 220 fs. The target width is 13 µm and is located at 10 µm < x < 23 µm. The black line in b) indicates the laser axis.

The temporal evolution of the longitudinal electric field $E_x$ and electron energy density distribution for the small pre-plasma case (0.5 µm length scale in the lower-density region) are shown in Fig.10. The region where electron energy density is high moves upward; this direction of movement is explained as follows. The high-energy electrons are accelerated in the laser propagation direction by ponderomotive acceleration for the small-pre-plasma case. When they exit from the rear surface, very energetic electrons escape from the target, but a large number of the electrons are dragged back and reinjected into the target toward the front side. As a result, electrons move upward, being trapped along the target and therefore the sheath field also moves in the same direction, as is seen in Fig.10, which results in the movement of the proton acceleration point.

There are two components of the sheath fields showing different time evolutions. The sheath field induced by electrons accelerated in the target-normal direction by vacuum
heating is symmetric around the target-normal position and expands radially, quickly reducing its magnitude. Another component is generated by electrons accelerated by ponderomotive acceleration, with greater magnitude than the previous one, since the ponderomotively accelerated electrons have much higher energy than target-normal electrons as is shown in Fig.11 and also in Ref. (Sheng et al., 2000).

At the early time of irradiation, a rather symmetrically expanded sheath field is induced. Shortly thereafter, a stronger sheath field localized at the ponderomotive position (y ~ 29 μm) is induced, while the symmetric field is weakened by diffusion (Fig.10d). The sheath field is strongest at the ponderomotive position and has a size comparable to the laser spot size.

The temporal evolutions of the maximum of the sheath field intensities at different positions are compared in Fig.12a, where the ponderomotive position (y ~ 29 μm), and 11 and 22 μm upward to the position (i.e., y = 41 and 52 μm) are chosen. As is seen from the figure, the intensity of the sheath field decreases as it propagates upward with velocity roughly close to the speed of light. The energy spectra of accelerated protons observed at those positions with 2 μm width are shown in Fig.12b. In the figure, the time delay of the proton acceleration due to the sheath movement is taken into account. It is seen that protons with the highest energies (2.3 ≤ E ≤ 3.0 MeV) are accelerated at the ponderomotive position by the strong sheath field, and protons accelerated in the upper position by the weakened field have lower energies.

Fig. 11. Angular distribution of laser-accelerated electrons for scale length of preplasma a) 0.5 and b) 3.5 μm.

Since the lateral movement of the region of high electron energy density is due to the lateral movement of ponderomotively accelerated electrons, the scale length of the pre-plasma is crucial for the drift since the dominant acceleration process depends on the scale length. The angular distributions of electron momentum inside the targets are compared for two different scale lengths, i.e., 0.5 and 3.5 μm, shown in Figs.11a and 11b. In the small-preplasma case, the high-energy electrons are well collimated and accelerated along the laser propagation direction by the ponderomotive acceleration. On the other hand, in the large-pre-plasma case, the electrons are dominantly accelerated toward the target-normal direction by the resonance absorption. In this case, the electrons propagating away from the rear surface return to the target in every direction like a fountain, which results in the
symmetric expansion of the sheath field. As a result, in the large pre-plasma case, directional lateral drift of the sheath field and proton source movement are not observed. The target thickness is also an important parameter. The lateral movement of the sheath field becomes less effective as the target thickness increases, since the electron energy density at the target surface decreases due to the expansion of the high-energy electrons into the target. Therefore, the target thickness is chosen to be comparable to or less than the laser pulse length for effective lateral drift of the sheath field. Also, the laser intensity is required to be relativistic so that the ponderomotive acceleration becomes dominant, generating a directional electron beam toward the laser propagation direction. A number of experiments on laser-proton acceleration have been carried out with similar parameters in terms of the laser intensity, irradiation angle, pulse duration, and target material and thickness (Hegelich et al., 2002, Fuchs et al., 2006, Cowan et al., 2004). But lateral drift of the sheath field has not been observed. The critical difference is the level of ASE. In the above cited experiments, the ASE level is mentioned as $\sim 4 \times 10^{12}$ W/cm$^2$, and in our experiments the ASE is reduced to $\sim 1 \times 10^{11}$ W/cm$^2$ by use of a specifically delayed pump mode with a comparable duration.

Thus the amount of energy of the ASE is lowered by roughly $1/40$ in our experiments, which leads to the estimated scale length being lowered by $1/6$. In the numerical simulations by Fuchs et al., (2006), which show good agreement with the experimental results, the scale length is set at 3 μm, which is consistent with the scale length of 0.5 μm in our experimental conditions. Finally, we want to mention the oscillation in the parabolic trace for the low-energy part. This might be attributable to the complex electron transport coupled to self-induced electric and magnetic fields on the rear surface. In the above simulations, a magnetic field of $\sim 30$ MG and electric field of $\sim 1$ TV/m are observed, induced by the lateral transport of high-energy electrons with an estimated current of roughly tens of kiloamperes. This surface current would be disturbed by a Weibel-like instability (Weibel, 1959), whose wave vector lies dominantly in the z direction, which is not taken into account in a two-dimensional (2D) simulation. Its understanding and consideration of 3D effects are left for future work.
In conclusion, we have shown a scenario of proton acceleration by a fast-moving rear surface sheath field. This is observed as a directional shift of a single parabolic line, indicating that the proton emission point is drifting along the surface, which is proved by a two-pinhole measurement. This drift is confirmed by 2D PIC simulations which clarify the mechanism and conditions for the drift. The drift is only observed when intense laser pulses obliquely irradiate targets with small pre-plasmas. In this case, ponderomotively accelerated electrons propagate along the target and induce a comoving sheath field. This drift of the acceleration position leads to a selection of the protons by their energies as a function of the observation point, which might shed light on the control of laser accelerated proton energy.

3. Tomography of an ultrafast laser driven proton source

3.1 Correlation of spectral, spatial and angular characteristics of proton source

Even if the measurements discussed in previous sections show a clear feature of the source, however, those are measurements of the ion emission from a very small area as compared to the whole source extension, which is about a few hundred μm. The complete scenario of the ion acceleration phenomena in its complexity could be given only if the source characteristics as a whole or at least a more extended part of it are investigated. Such understanding is especially important for modelling and ion beam tracing.

In order to image a broader area of the source the principle of tomography was employed. Tomography is an imaging method. The object is imaged section by section (or sectioning). In this work we apply sectional imaging of the proton source by using an array of pinholes in combination with a Thomson spectrometer (Ter-Avetisyan et al., 2009a). A technique which provides sectional images of an object is usually referred to as a tomography, and, in principle, the superposition of tomographic cross sections coupled to a reconstruction algorithm allows the visualization of the internal structure of an object.

Because the laser accelerated proton beam is laminar (Borghesi, et al., 2004) and irregularities at small scale do not disrupt the general beam characteristic it is sufficient to substitute the entrance pinhole of the spectrometer with a multi-pinhole array. It is installed perpendicular to the dispersion direction: parallel to magnetic and electric fields. This way the proton beam is divided into small beam-lets and the obtained spectral images combine the simultaneous record of many independent spectrometers which have the same dispersion constant (Fig.13). Because the source has a finite size and the emission is laminar the spectrometers record the ion spectra corresponding to different emission zones of the source according to their emission angle. This detection principle allows the reconstruction of the source, which we call here proton source tomography. It gives an energy resolved topographic picture of the source.

In the experiment 40 fs pulses from a multi 10 TW Ti: Sapphire laser system were focused down to a 10 μm perfectly round spot onto a 5 μm Ti target. The maximum laser intensity was about $2 \times 10^{19}$ W/cm$^2$. The ASE pedestal of the laser pulse, several picoseconds before the pulse peak, was at a level of $10^{-8}$ relative to the peak intensity.

The proton emission spectrum was measured with a Thomson parabola spectrometer calibrated in absolute terms (see more details in Ter-Avetisyan et al., 2005). The applied magnification (Schreiber et al., 2006), provides additionally high spatial resolution. The spectra were obtained from 21 beam-lets produced with a row of 21 pinholes having 30 μm in diameter each and a period of $d = 530$ μm (Fig.13).

This pinhole mask is positioned parallel to target surface at a distance of $a = 85$ mm, parallel to the magnetic and electric fields of the Thomson spectrometer, and lie in the plane of laser
beam polarization (p-polarized). A magnetic field of about 0.33 T between 4 cm separated poles was applied in the spectrometer. The spectrum was imaged on the MCP detector coupled to the phosphor screen located at a distance of $b = 120$ mm, $c = 275$ mm from the pinholes (Fig.14a). All precautions mentioned in (Ter-Avetisyan et al., 2004b) have been taken for the measurements. Additionally, a careful scan of the magnetic field distribution in all three dimensions between the magnetic poles and outside was carried out. The derived instrument function was conformed with an additional test experiment to exclude any artifact on the spectral traces caused by field inhomogeneities.

At this geometry $\alpha = 2.3^\circ$ is the largest possible angle of protons entering the spectrometer. The restriction comes mainly due to the finite size of MCP detector. The magnetic field disperses the protons acting on their $v_z$ velocity component perpendicular to magnetic field which is $v_z = \vec{v} \times \cos \alpha \approx \vec{v}$. Therefore a possible difference in dispersion for protons passing through different pinholes is negligible and well below our resolution limit. It was not necessary to apply the electric field in order to separate the ions because of the ultra-short and high temporal contrast of the laser pulse, a pure proton beam was produced (Schnürer et al., 2007, Nickles et al., 2007).

A typical spectral image is shown in Fig.14a. As mentioned, this picture combines in principle the record of many independent spectrometers (in our case - 21) located under a different angle to the source and having the same dispersion constant and the bright spots in the right side of the figure are formed by energetic photons passing through pinholes and representing the axis of the spectrometers. The $\phi$ in the right side of Fig.14a are the tilt angles of the measured spectra from the spectrometers axes. The spectrum along the “central axis” has a $0^\circ$ tilt. The spectrometers axes can be exactly defined with the measured...
Fig. 14. (a) The imaged spectra through a row of pinholes are shown. Because the figure is symmetric to $\phi^o = 0$ line, on one half of the figure the dependence on the tilted angle $\phi^o$ from axes is given (right upper side) and on the other half the numbering of the traces (right low side); (b) Energy of the emitted protons as function of target coordinate in the beamlets from 1st up to 8th is depicted; (c) Proton emission angle in each beamlet depending on proton energies; (d) emission angle of protons with 0.5, 1, 2, 3, 4 MeV energies dependent on emission target coordinate.

Energetic photons which are registered over a whole angle of $\pm 4.6^\circ$ from a source with an extension of about 20 µm. This means that initially the laser drives the hot electrons through the target with a divergence angle of about $45^\circ$. Having the axis of each pinhole-spectrometer and the angle of departure of the proton trace from this axis, the coordinate of the proton emission at the target surface and the emission angle can be calculated.

The striking features of Fig.14a are: (i) A clear spectral trace from each pinhole is observed. There are no crossing lines. This confirms that the beams of different energies are strongly laminar. (ii) The spectral traces are tilted from their axes. The “central” trace lies exactly on its spectrometer axis. Symmetrically, on both sides of the “central” trace all spectral traces have a tilt which increases with the distance to the central point with the angle $\phi^o$. Because of the good symmetry in the following figures we will show the spectra located only on one side from “central axes” in order to do not overload them.
The analysis of the experimental data and the reconstruction of proton trajectories are straightforward. With the position of the pinholes along the linear array and the measured coordinates of the “zero points” both the target coordinate and the angle of the emitted protons could be calculated. This was done for different energies contributing to the spectral trace and by applying a simple geometrical relation. However, the scan of the magnetic field showed that the magnetic field lines are slightly curved in x,y and x,z planes and the existence of \( B_y \) and \( B_z \) components tilt the spectral traces. The protons will be deflected in \( \pm x \) direction due to both \( (v_z \times B_y) \) and \( (v_y \times B_z) \), where the \( v_z \) and \( v_y \) velocity component appears inside the magnet due to the dispersion. This was verified in a test experiment where a single proton beam was injected at ten different positions inside the magnet. The resulting instrument function was determined and used to unfold the measured raw data.

In Fig.14b the emitted proton energy is depicted as a function of the target coordinate derived from the 1st up to the 8th beam-let. It can be seen, that at the same target coordinate protons are emitted with different energies, while protons with the same energy arise from different target coordinates. As higher the energy of protons as smaller the region from where the emission occurs.

The proton emission coordinate as a function of the emitted proton energies (Fig.14b) of the \( i^{th} \) beamlet can be fitted with an exponential function as:

\[
x_{Ei} = m_i = n_i \times \exp(-E_i / 0.93)
\]

where \( m_i \) and \( n_i \) are implicit functions of the target coordinates in relation to the pinhole \( i \) ; \( m_i \) is the target coordinate from where the high energy protons have passed through the pinholes and therefore it is defined by the geometry of the pinhole array. It can be found that \( m_i \) is a parabolic function of the period (\( d \)) of the pinhole array:

\[
m_i(\text{mm}) = -0.018 - 0.038d - 0.003d^2 ,
\]

where 0.018 mm is the target coordinate from where the high energy protons have passed through the pinhole number zero.

Similarly, \( n_i \) is also defined by the pinhole array but it shows how strong the target emission coordinate changes with the energy of the protons which are passing through a same pinhole. The \( n_i \) is also a parabolic function of the pinhole array period:

\[
n_i(\text{mm}) = -0.06 - 0.11d - 0.01d^2 .
\]

Therefore, the relation between these two parameters is:

\[
m_i = 0.36 \times n_i .
\]

The proton trajectory in each beamlet depends on proton energy as shown in Fig.14c. The related emission angle of the protons is continuously changing with its kinetic energy. At the same angle only protons with different energies are emitted. Additionally, protons with low energy are emitted at a smaller angle compared to protons with high energy. The emission along the symmetry axis of the source is unique; the protons emitted under \( 0^\circ \) to the target normal are bearing any energy according to the spectral distribution.

The dependence of the proton emission angle on energy (Fig.14c) in different beamlets can be fitted with an exponential function as:

\[
\theta_{n,E_i} = \alpha_n - \beta_n \times \exp(-E_i / 0.93)
\]

where \( \alpha_n \) is the emission angle of measured highest energy protons passing the \( n^{th} \) pinhole.

The \( \alpha_n \) is a linear function from the pinhole array period: \( \alpha_n = -0.02 + 0.65d \), showing a linear increase of the emission angle of high energy protons with the target coordinate and \( 0.02^\circ \) is the opening angle of the beam which is passing through the pinhole number 0.
(Fig.13). The parameter $\beta_n$ shows how strong the emission angle of protons changes if they are passing through the same pinhole with different energies. The $\beta_n$ is the parabolic function of the pinhole array period ($d$) and can be expressed as $\beta_n = -0.04 - 0.07d + 0.005d^2$.

It means that going with increasing distance to the centre and from one pinhole to the next one the angle increases in respect to a similar change of the energy.

The emission angles of protons with the same energy but with different emission coordinates in relation to the 16 beamlets which are symmetrically located on both sides of the “central axes” are shown in Fig.14d. For each proton energy the data can be fitted with the Lorentz function and it can be found that the width of the source ($\Delta x$) is an exponential function of the proton energies: $\Delta x \sim E^{0.5}$.

With these relations one can reconstruct the proton trajectories as they are emerging from the target. One can see in Fig.15a, where as an example 0.5 and 4 MeV proton trajectories are shown, that protons with a same energy are accelerated as an expanding laminar beam. The emission angle increases with the target coordinate (or the distance from the source centre) and higher energies belong to a large emission angle if the same target region is analyzed. Additionally, the measured high energy protons are emitted from a smaller target region than the lower energetic once.

![Reconstructed proton trajectories](image)

Fig. 15. a) Reconstructed proton trajectories as they are emerging from the target. As an example are shown 0.5 and 4 MeV proton trajectories. b) Simulated angular spread of proton emission depending on proton energy for 40 fs and 500 fs laser pulses.

The discussion above makes clear, that each beam-let is formed by an unique combination of energy, target coordinate and emission angle of the protons. The low energy protons are emitted with a smaller angle than the high energetic ones (Fig.15a). At first glance this observation seems to be in contradiction with a statement in (Cowan et al., 2004) that the angular envelope of the protons with increasing proton energy is decreasing. There are two things which make a decisive comparison to other experiments and its conclusions difficult. First, there are no data known to us from the literature with a similar resolution in order to make a direct comparison concerning the emission of the central part of the beam as we performed. Second, due to the present limitation of the observed range of angles we did not look to the maximum extension of the source as a function of energy. The latter one is in other works mainly attributed to the source size. If one calculates the ratio between the emission coordinates (source size) and the emission angle as a function of the ion kinetic energy one finds a qualitative similar functional dependence of our data and those from...
other work. Nevertheless a final conclusion for different experimental parameters realized in different work should be drawn from data with similar resolution. However, the discussed features unambiguously follow directly from the experimental findings. Also recent experiments showed (Roth et al., 2005) that the highest energy protons are emitted in the central, high density portion of the sheath distribution, which agrees with the present results (Fig.14b). Nevertheless, it is likely that both the used long pulse (350 - 850 ps) and high laser energy (20 - 30 J) (Cowan et al., 2004), in contrast to our ultra-short pulse (40 fs) with “low” energy (0.7 J), and more importantly the high temporal laser pulse contrast (10^{-7} - 10^{-8}) (Nickles et al., 2007) are the decisive parameters for the proton source formation and emission characteristics of the accelerated particles.

In order to look particularly to proton acceleration scenarios in case of long and high energy laser pulses in comparison to short and low energy laser pulses 2D particle-in-cell (PIC) simulations were performed. The simulation box had a size of 150 µm × 150 µm. The 10 µm thick and 150 µm long target was located at the coordinate 12.0 < x(µm) < 22.0. The pre-plasma was set 0.5 µm in front of the target and composed of Al^{3+} cold ions and 500 eV electrons with a density 20 n_c. The n_c denotes the critical density. A proton contamination layer was buried within a distance of 0.5 µm from the rear surface. The laser with a wavelength of 0.8 µm and focused to 10 µm was irradiating the target under 0°. The laser pulse durations were set as 40 fs and 500 fs and had Gaussian profiles both in space and time. The electromagnetic field was damped at the boundary of the simulation box, and the particles were reflected with thermal energy.

The simulation results of the proton energy dependence on the emission angle are shown in Fig.15b. The full simulation time was 900 fs for the short, and 1400 fs for the long laser pulse. The difference is apparent: For the 500 fs laser pulse irradiation the angular spread of the accelerated protons is gradually increasing with decreasing proton energies, as it was observed in (Cowan et al., 2004). This is in contrast to the case of the 40 fs laser pulse irradiation where the higher energetic protons have the largest angular spread, and the emission angle decreases with the proton energy. In the long pulse case, the sheath field accelerates protons for roughly 500 fs, where the acceleration is described by hydrodynamic plasma evolution (Mora, 2003). In short pulse case the maximum sheath field is sustained only about 40 fs while protons are about to be accelerated. When the proton acceleration starts, the sheath field is still expanding and the accelerating front has a large curvature, which results in larger angular spread for higher energetic protons. The simulated energies and the angular spreads are quite comparable to that presented here and to the experimental results in (Cowan et al., 2004).

Additionally, results of simulation for the angular behaviour of protons emitted from different target coordinates are similar to those shown in Fig.15b for both 40 fs and 500 fs laser irradiation cases. Therefore, one can conclude, that the observed features in the present experiments is an unique property of the ultrashort and high contrast laser pulse acceleration scenario.

On base of the found interconnections between the target coordinate, emission angle and energy of emitted protons, one can constitute the following rules:

- The proton emission is directed to the target normal and it is symmetric to the laser axis.
- Protons with different energies are emitted such that: as higher the proton energy as smaller the source size but as bigger the emission angle in relation to the source size.
Protons with the same energy are emitted from different target coordinates such that: as far away from the centre as larger the emission angle.

Protons which are emitted from the same target coordinate but with different energies obey to the following: as higher the energy as larger the emission angle.

3.2 Correlation of spectral, spatial and angular characteristics of proton source

The measurements discussed in section 1.4 were made around the central symmetry axis of the source. Due to the limited size of the detector only protons with 0.5 to 4 MeV energies emitted within a 2-3 degree angle were analysed. In order to acquire an understanding about the whole source behaviour, broader proton energy ranges have to be covered. Additionally, it is of interest and necessary to explore to what extent the measured proton source properties near the central symmetry axis are applicable to the whole and much more extended proton source. Particularly in view of planning proton beam steering systems it is necessary to know up to which point the measured energy dependence of the angular emission characteristic is preserved.

Here, the investigation of the source emission characteristics was extended at larger angles from the central symmetry axis and in a rather large range of proton kinetic energies from 0.06 MeV up to 4 MeV.

The measurement of the proton emission spectrum was carried out similar to section 3.1. Being restricted by the size of the detector a good compromise between the requirements of high magnification and of an extended spectral range was found by locating the pinhole array at a distance of about \( a = 30 \text{ mm} \) from the target surface and the detector screen at \( b = 195, \ c = 255 \text{ mm} \) from the pinholes (Fig.13). The inset of Fig.13 shows the imaging geometry which allowed a complete characterisation of the source in the whole spectral range.

In our previous section 3.1 the pinhole array was aligned in such a way that the central symmetry axis of the plasma crossed the central pinhole. In the measurements reported here we applied an imaging geometry with higher magnification and, distinctively, the pinhole array was shifted along the Y axis (i.e. parallel to the target surface and away from the ion beam central axis) (see inset of Fig.13). This shift, of about 2 mm, gave a corresponding shift of about 40 mm for the positions of the “zero” points on the detector. The observation angle extended up to 4.77 degrees relative to central symmetry axis of the plasma. In fact, with this geometry we imaged a source area centred at about 70 \( \mu \text{m} \) from the source centre.

The respective spectral traces cover the high energy part of the spectra (Fig.16a) in the same way as in section 3.1 but extend the source imaging region to cover energies down to 0.2 MeV protons. Fig.16a looks very similar to Fig.14a in section 3.1 where a lower magnification was applied. The data analysis confirmed that the observed spatial and angular characteristics of the emitted protons are exactly the same as in the case of axis-symmetric detection (section 3.1) and can be treated in a similar manner. The tilts of the spectra from their axes are still symmetric relative to the zero degree trace (i.e. the trace due to the pinhole on-axis with the interaction point). For the 45° incidence on target as employed in the experiment the focus is elliptically shaped and has two main symmetry axes and therefore one should expect the source area to show also this elliptical symmetry. We have measured along the short main axis of the elliptically shaped source area. As a result also the tilts of the trajectories for the corresponding energies from the main axis are symmetric relative to the “central” trace. The data analysis was carried out by treating the signal observed as the result of 21 independent spectrometers as defined by the pinholes.
Fig. 16. a) Spectral traces of a row of pinhole images: On the right side of the figure the tilt angle $\phi$ of the spectral traces from the central symmetry axes corresponding to $\phi = 0$ line (target normal) and respective numbers of beam-lets (in brackets) are given. b) Proton emission angle in each beam-let depending on proton energies in beamlets from 1st up to 4th is depicted. c) Emitted proton energy as function of target coordinates in beamlets from 1st up to 4th. d) Emission angle of protons with 0.2, 0.5, 1, 2, 3, and 4 MeV energies dependent on target emission coordinate is exhibited.

Each spectrometer axis was defined by the coordinate of the “zero” point and the coordinate of the corresponding pinhole (Fig.13). If protons within the observed energy range are all emitted from the same source point the projection of their spectrum on the X-axis of the detector (Fig.13) should be a point, i.e. the line describing the spectrum should be along the Y axis. The measurement showed instead that the lines described by the spectra in the detector plane are tilted with respect to the Y axis i.e. the projection on the X axis is different for different energies (Fig.16a). From the X coordinate of the projection for a particular energy the corresponding pinhole coordinate and assuming straight propagation of the particles, the coordinate on the target surface from where the corresponding proton is emitted (inset of Fig.13) can be calculated.

The “zero” points coupled with the position of the corresponding pinhole, are used as a reference to define the axes of the spectrometers. When using MCP detectors, the “zero”
points can be due to X-rays (Ter-Avetisyan et al., 2009b) and neutral particles (Busch, et al., 2003, McKenna et al., 2007) which are undeflected by the magnetic field in the spectrometers. The data analysis shows that the trend observed in section 3.1 of the proton emission angle decreasing with decreasing proton energy is preserved in these measurements (Fig.16b). Additionally, higher energy protons are emitted from a smaller target region (Fig.16c) with higher divergence (Fig.16d) while the proton source for lower energies becomes larger and has a lower divergence. These trends confirm the assumption that “each source point behaves similarly” which allows one to characterise the general source behaviour independently from the specific area of the source under observation. Therefore a similar approach for the calculation of the proton emission trajectories (section 3.1) has been applied.

![Proton Trajectories](image.png)

Fig. 17. Reconstructed proton trajectories as they are emerging from the target. As an example a) proton trajectory passing through 1 and -1 pinholes are shown. The virtual source position in front of the target is deduced by linear interpolation of the proton trajectory lines (dashed lines). b) The virtual source position in front of the target for different proton energies is shown.

The trajectories of protons with different energies, which pass for example through the pinholes +1 and -1 are deduced from the spectral traces and shown in Fig.17a. One can adopt a virtual source concept to describe the behaviour of a laminar ion source, as discussed in (Borghesi, et al., 2004). If one assumes that the propagation of the proton beam after the acceleration process is ballistic and there is no ion interaction within the beam, the proton trajectories are straight lines (inset of Fig.13) and one can trace back these trajectories to a virtual source (VS_p) in front of the target as shown in Fig.17a (dash lines).

The virtual source position in front of the target changes for different proton energies (Fig.17b), which means that the protons with different energies are emitted with a different curvature of the accelerating sheath field. In the inset of Fig.13 the virtual source points for protons with different energies, where $E_{p1} > E_{p2}$, are shown. This hints at a change of the sheath field curvature during the acceleration process.

As a next step measurements with a larger displacement of the observation axis were realized (i.e. the pinhole array was shifted sideways so that the central pinhole was further away from the interaction axis). This set of measurements was aimed to explore the emission characteristics far from the source centre. Furthermore, the measurement was extended to protons with even lower energy. A displacement of the observation axis of about 1 mm from the central source axis was set, which corresponds (for the central pinhole
of the array) to an observation angle of about 4.88 degree relative to the central symmetry axis of the plasma. The measured proton spectra are shown in Fig.18a. Due to the limited size of the detector the “zero points” are not visible in this case. As the “zero point” coordinates are needed for the trajectory reconstruction now the deflecting electric field of the Thomson spectrometer was switched on in separate shots to perform an energy calibration by using deflection of protons in an applied electric field. From the parabolic traces the corresponding “zero points” were extrapolated and these extrapolated coordinates have been used to analyze the measurements for the respective pinhole and spectrometer setting. The proton emission angle depends on proton energies as shown in Fig.18b. The data show clearly (Fig.18b) the continuous decrease of the proton emission angles relative to target normal with decreasing proton energies. This tendency holds down to proton energies of about 0.14 MeV which are emitted along the target normal; therefore one can say that they are “collimated”. The proton beam at energies lower than 0.14 MeV is

Fig. 18. a) The imaged spectra through a row of pinholes are shown. On the right side the numbers of beam-lets are given. b) Proton emission angle in each beam-let depending on proton energies in beam-lets is depicted. c) Emitted proton energy as function of target coordinate and (d) emission angle of protons with 0.06, 0.08, 0.1, 0.15, 0.2, 0.25 and 0.3 MeV energies dependent on emission coordinate is exhibited. $\theta_0 = 0$ is the angle of target normal.
convergent and in the detector plane one can see the crossing of trajectories at about 0.12 MeV (Fig. 18b). For such low proton energies the source size becomes as large as a few mm (Fig. 18c). Concerning this largely extended source area we thus found that the beam becomes converging (Fig. 18d) as much as the proton energy decreases. On basis of this measurement geometry the proton trajectories are calculated and traced back to the target surface (cf. Fig. 19a).

To our knowledge this is the first observation showing that a proton beam driven by an ultra-short laser pulse consists of a divergent, a “collimated” and a converging component, with the divergence varying continuously as a function of energy.

The structure of the transverse electric field obtained in 2D PIC simulations performed at the conditions as in section 3.1 gave some qualitative indication of possible reasons for the observed divergence-to-convergence behaviour of the proton beam. The simulation starts at t=0 and the laser peak reaches the target surface at t = 120 fs. The structure of the transverse electric field is plotted in Fig. 19b. The bell-shaped red lines (4 are visible) represent iso-density contour plots of protons in the accelerated bunch.

Fig. 19. a) Reconstructed proton trajectories as they are emerging from the target with the energies 0.06, 0.08, 0.1, 0.15, 0.2, 0.25 and 0.3 MeV and passing through the 1st, 2nd, and 3rd pinholes are shown. b) 2D PIC simulation results: transverse component of sheath field at t = 500 fs (the parameters of the simulation are explained in the text).

The protons propagate from the left to the right. At the ion front we observe transverse field components which are opposite with respect to the y = 75 symmetry line: the field is directed up for y > 75 (red colour code) and down for y < 75 (colour code blue). The transverse field is most intense at the acceleration front which causes radial deflection and angular spreading of the higher energy protons. Behind the ion front we observe weaker field strength and finally a change in the field polarity (at x < 25): For the region y > 75 we observe now light blue coded areas (i.e. field directed down) and for y < 75 yellow ones (field directed up), respectively. Thus the slower protons, which are behind the fast ion front, experience a transverse field component which can in principle result in converging trajectories, as observed in the experiment for rather low energetic protons.

The situation might be different in the case of ions accelerated by long (ps) laser pulses, where the longitudinal momentum gained by the ions is higher and transverse fields may be less effective in spreading the high energy ions.
Summarizing the emission properties of a proton beam accelerated by a high contrast ultra-short laser pulse have to be understood as follows. A target source point emits protons within a broad range of energies. Taken two energies $E_1$ and $E_2$ such that $E_2 < E_1$, the relation of the proton emission angles is $\theta_{E_2} < \theta_{E_1}$. Any point located at a distance $d$ from the target rear surface and located within the total beam cone will be crossed by the trajectories of ions with different energies which are stemming from different target-source coordinates. This means, only a certain target area ($S$) is contributing to the ion spectrum which is measured at some point in the beam cone and at a certain distance from the target rear surface. As a result, the spectrum of the protons in that point can be controlled by changing the proton source area. It might be that our results apply also to the results of Ref. Schwoerer et al., (2006), where a proton beam with a small energy spread was detected when the proton source area was restricted.

The data also indicates that the proton beam is emitted from the target so that for high energies it is divergent and becomes convergent for low energies (below 0.2 MeV). 2D PIC simulations provide indications on how the effect of field components transverse to the beam propagation axis could lead to these features. It will be interesting to test in future experiments how this behavior will scale if the cut-off energies in the ion beam are significantly enhanced using a laser driver providing much higher energy and intensity. Additionally comparative investigations with longer driver pulses may clarify whether (as it is likely) the divergence behavior measured here is an exclusive feature of short pulse interactions.

4. Conclusion

In this article recent studies of phenomena in relativistic proton acceleration have been reviewed. Experimental results have shown unique properties of protons accelerated by ultrashort laser pulses, which opens prospects for a broad range of applications (Borghesi et al., 2006).

Significant advances in laser technology are likely to expect for the next years, leading to further enhancement of both the intensity of the extremely short pulses and the average power. These developments will surely stimulate the elaboration of new ideas and more advanced diagnostic developments for measuring the effects not even thought of today. All of this will open up new research areas, pushing current activities to new frontiers, and generate further excitement in the field of laser-matter physics.

5. References


In this volume, recent contributions on coherence provide a useful perspective on the diversity of various coherent sources of emission and coherent related phenomena of current interest. These papers provide a preamble for a larger collection of contributions on ultrashort pulse laser generation and ultrashort pulse laser phenomena. Papers on ultrashort pulse phenomena include works on few cycle pulses, high-power generation, propagation in various media, to various applications of current interest. Undoubtedly, Coherence and Ultrashort Pulse Emission offers a rich and practical perspective on this rapidly evolving field.

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